

# Dark matter model comparison

Pat Scott

**Imperial College  
London**

on behalf of the GAMBIT Collaboration

[gambit.hepforge.org](http://gambit.hepforge.org)



# Many models, many constraints

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Scalar singlet

Fermion singlet

Vector singlet



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- axion-like particles
- self-interacting DM
- asymmetric DM
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Ultimately, we want to use all of the **left** to choose between the options on the **right**.



# GAMBIT: The Global And Modular BSM Inference Tool

[gambit.hepforge.org](http://gambit.hepforge.org)

- Fast definition of new datasets and theoretical models
- Plug and play scanning, physics and likelihood packages
- Extensive model database – not just SUSY
- Extensive observable/data libraries
- Many statistical and scanning options (Bayesian & frequentist)
- *Fast* LHC likelihood calculator
- Massively parallel
- Fully open-source

ATLAS

LHCb

Belle-II

Fermi-LAT

CTA

CMS

IceCube

XENON/DARWIN

Theory

F. Bernlochner, A. Buckley, P. Jackson, M. White

M. Chrzęszcz, N. Serra

F. Bernlochner, P. Jackson

J. Conrad, J. Edsjö, G. Martinez, P. Scott

C. Balázs, T. Bringmann, M. White

C. Rogan

J. Edsjö, P. Scott

B. Farmer, R. Trotta

P. Athron, C. Balázs, S. Bloor, T. Bringmann,

J. Cornell, J. Edsjö, B. Farmer, A. Fowlie, T. Gonzalo,

J. Harz, S. Hoof, F. Kahlhoefer, S. Krishnamurthy,

A. Kvellestad, F.N. Mahmoudi, J. McKay, A. Raklev,

R. Ruiz, P. Scott, R. Trotta, A. Vincent, C. Weniger,

M. White, S. Wild



**31 Members in 9 Experiments, 12 major theory codes, 11 countries**



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# But then how to compare different models?

- Bayes factors?  $B = \mathcal{Z}_1/\mathcal{Z}_2$



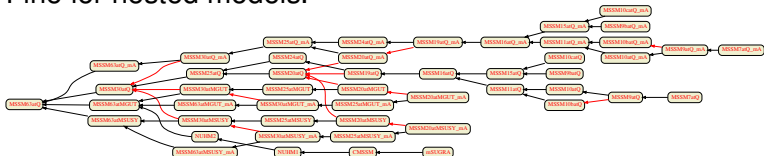
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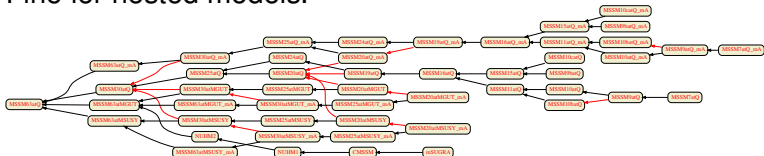
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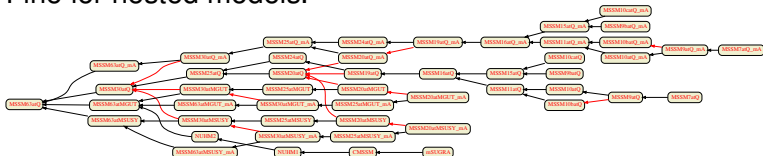


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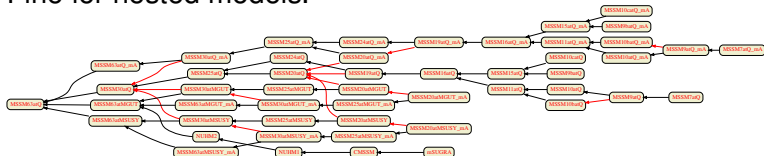
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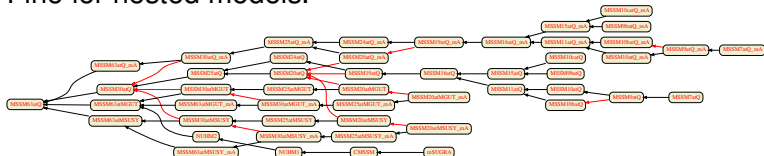
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- Entropic priors? (e.g. [arXiv:0906.5609](https://arxiv.org/abs/0906.5609))  
Is this the same as minimising the K-L divergence?



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  - Can help with determining *dof* of test statistic at least.
  - Also useful for saying how well a given idealised experiment *could* distinguish models.
  - But how to rigorously use for discriminating between models given real data?

