

# FAZST-Femto-Atto-ZeptoSecond Science & Technology

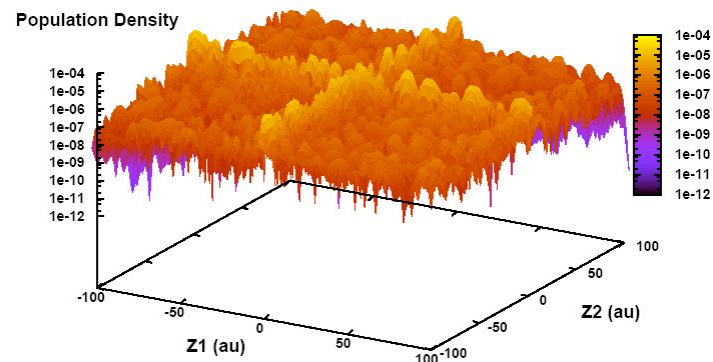
Andre D Bandrauk, FRSC, FAAAS  
Canada Research Chair

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<http://pages.usherbrooke.ca/adbandrauk>

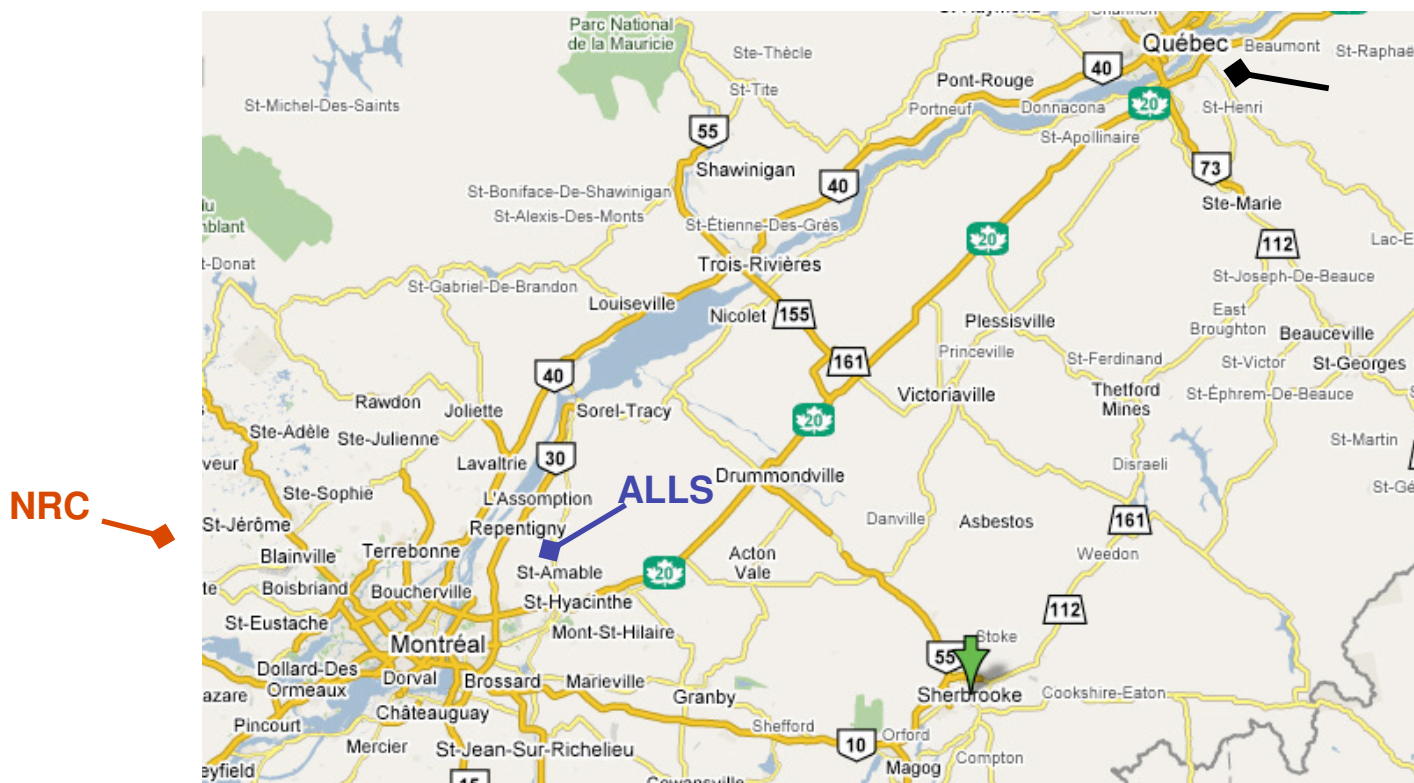
$\text{H}_2 (X^1\Sigma_g^+)$ :  $I=3 \times 10^{15} \text{W/cm}^2$ ,  $\lambda=800 \text{nm}$ ,  $T=6$  cycles



# “Molecules in Intense Laser Fields – Femto to Atto to ZeptoSecond Dynamics”

and / or

## “FAZSST-Femto-Atto-ZeptoSecond Science & Technology”



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Potential energy :  $V_o : \frac{e^2}{a_o} = 1 \text{ Hartree} = 27.2 \text{ eV},$  (1)

Electric field  $E_o : \frac{e}{a_o} = 5 \times 10^9 \text{ V/cm},$  (2)

Intensity  $I_o = cE_o^2 / 8\pi = 3.5 \times 10^{16} \text{ W/cm}^2,$  (3)

Distance  $a_o = 0.0529 \text{ nm},$  (4)

Time :  $t(a_o) = 24 \text{ as}, 2\pi t_o = 152 \text{ as}$   
 $t(mc^2) = 1.3 \text{ zeptos}$

**Table I**

**Evolution of Laser Parameters [1]**

Time (s)		Intensity (Watts/cm <sup>2</sup> )		Year
Nano	10 <sup>-9</sup>	Giga	10 <sup>+9</sup>	1980
Pico	10 <sup>-12</sup>	Tera	10 <sup>+12</sup>	1985
SERS				
Femto	10 <sup>-15</sup>	Peta	10 <sup>+15</sup>	1990
1 a.u. : 24 x 10 <sup>-18</sup>		$I_o = 3.5 \times 10^{+16}$		
Atto	10 <sup>-18</sup>	Exa	10 <sup>+18</sup>	2005
Zepto	10 <sup>-21</sup>	Zetta	10 <sup>+21</sup>	2009
Yocto	10 <sup>-24</sup>	Yotta	10 <sup>+24</sup>	?

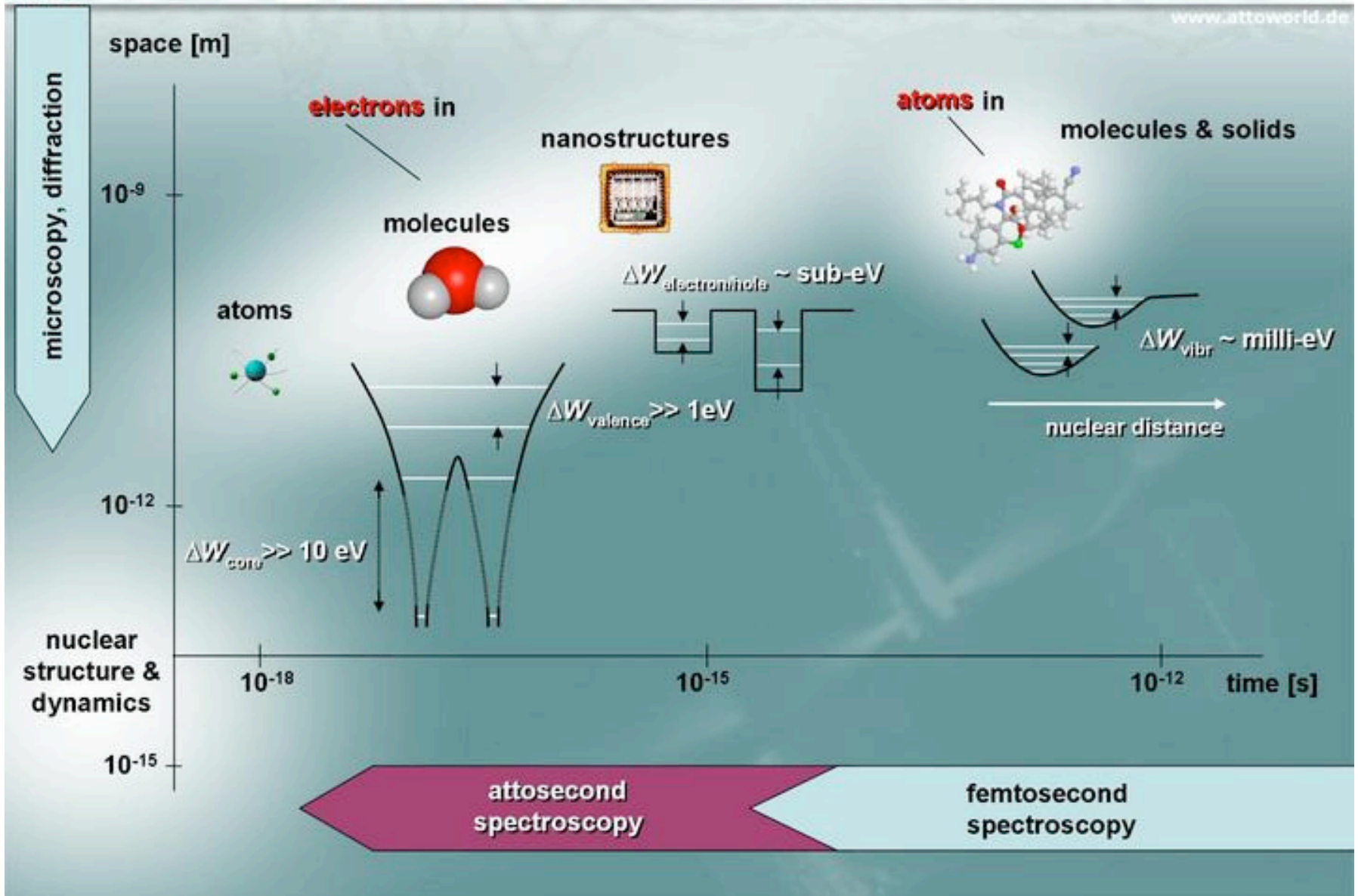
**10<sup>29</sup> - Schwinger Limit**

The intensities discussed in the present article,  $10^{14} \geq I \geq 10^{15} \text{ W/cm}^2$  correspond to fields approaching the internal Coulomb potentials of atoms and molecules ( $V_o$ , equations (1-3), thus inducing considerable distortions of intermolecular potentials. In the dressed state representation these radiatively induced distortions creating LIMP's as discussed above lead to *bond softening* via laser-induced avoided crossing of molecular potentials [26-27]. At such intensities, one needs to consider further ionization and the remaining molecular ion potentials become LIMP's in the presence of intense laser pulses. The molecular ions, bound or dissociative can also undergo Above Threshold Dissociation, ATD, [20], [26-27].

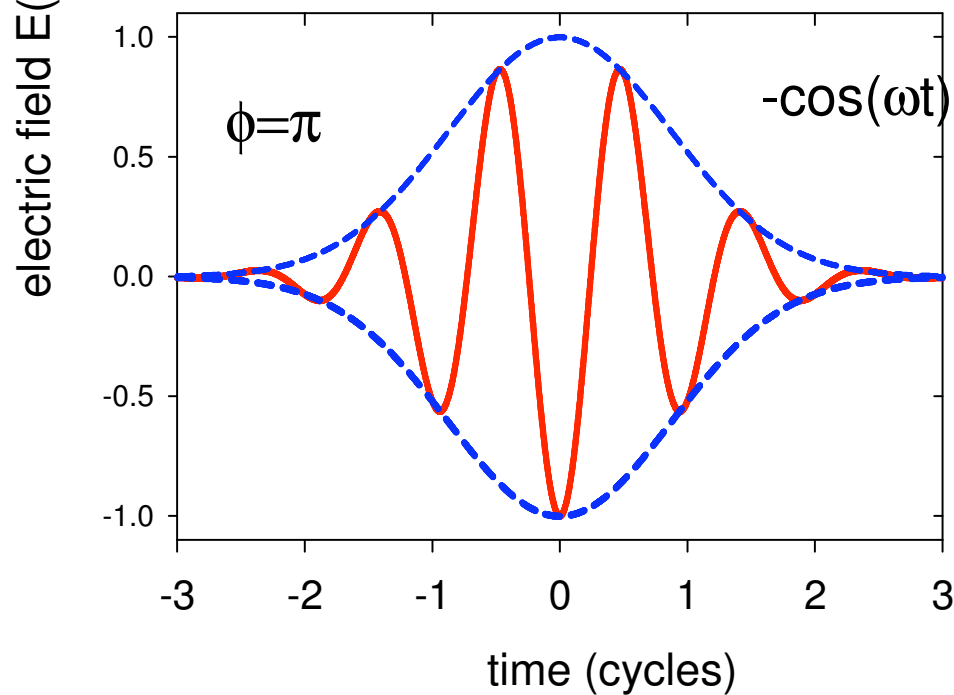
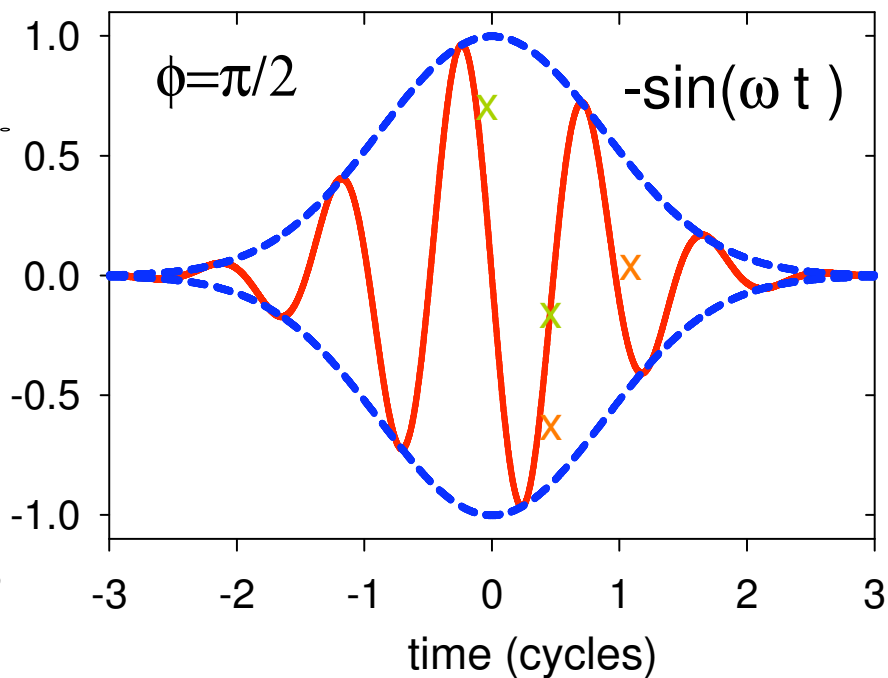
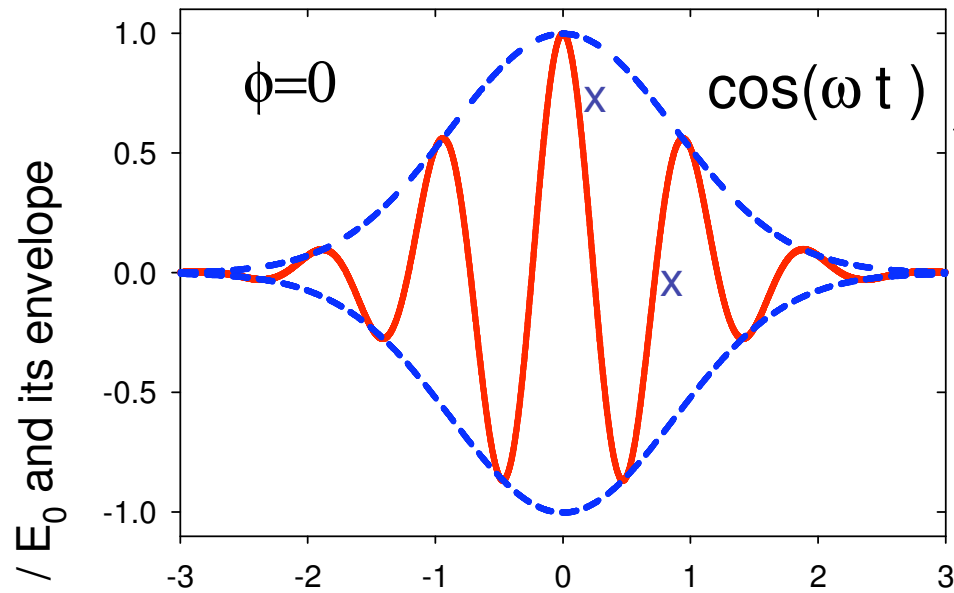
Schwinger limit ~ 10\*\*29 W/cm2)

Sunlight: 0.12 W/cm2

structure and dynamics in the microcosm





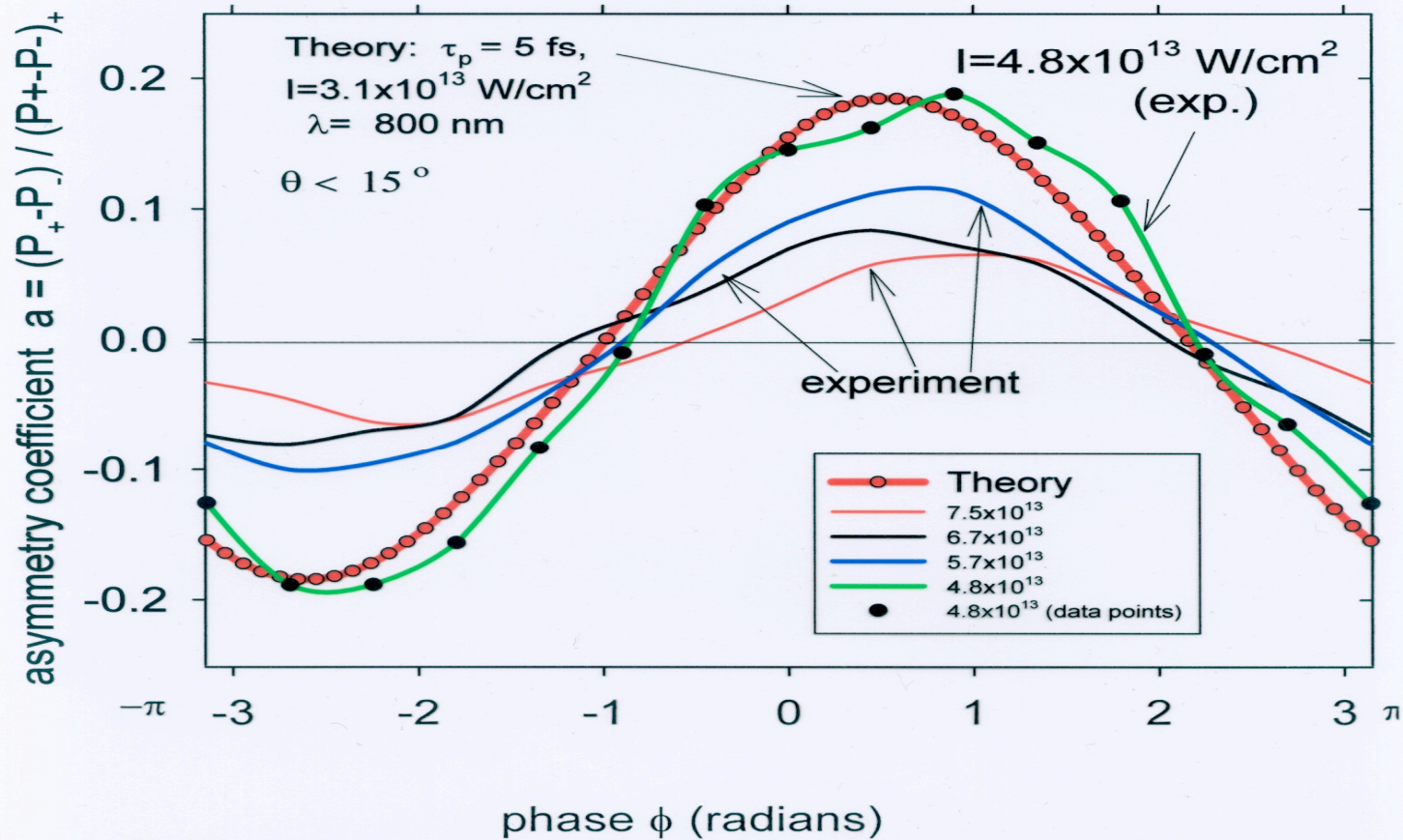


1 cycle = 2.66 fs  
 for  $\lambda = 800$  nm

$$E(t) = \varepsilon_0(t) \cos(\omega t + \Phi)$$

F Krausz, Science 305,1267(2004)

Experimental asymmetries (Garching).  
F. Lindner, Ph.D. Thesis.  
 $\lambda=760$  nm,  $\tau_p=5$  fs .



•Phys. Rev. A, 70, 013815 (2004)

•Opt. Lett. 29, 1557 (2004)

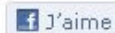


## Science

# Exciting electrons

Chemistry rarely grabs the limelight. But in 2011 it will try to

Nov 22nd 2010 | from PRINT EDITION



One sugar, please





## MAXWELL – SCHROEDINGER

MAXWELL

Classical      Quantum

$$\frac{\partial^2 E}{\partial z^2} - \frac{1}{c^2} \frac{\partial^2 E}{\partial t^2} = \frac{4\pi}{c^2} \frac{\partial^2 P}{\partial t^2}$$

$P = \text{Medium Polarization} = P(E)$

(1<sup>st</sup> Order  $P = \alpha E$ )

SCHROEDINGER

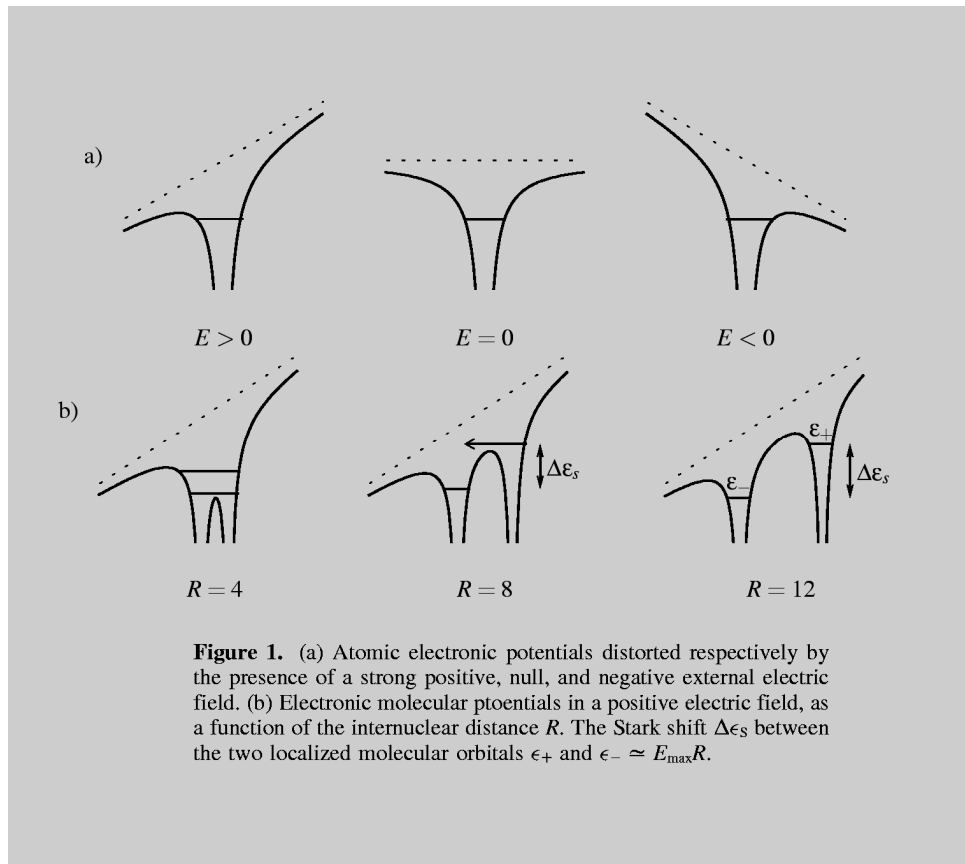
$$i\hbar \frac{\partial |\psi\rangle}{\partial t} = (\hat{H}_0 + \hat{V}(t)) |\psi\rangle$$

$$P = P(E) = n_0 \langle \psi | \hat{\mu}_0 | \psi \rangle$$

$$|\psi\rangle = \sum_j c_j e^{iE_j t / \hbar} |\Psi_j\rangle$$

$$V_{ii} = -P_{ii} (e(z,t) \cos(kz - \omega t))$$





P. B. Corkum, PRL,  
71, 1994 (1993).

T. Zuo and A. D. Bandrauk,  
PRA, 52, R2511 (1995).

# Recollision physics

Paul B. Corkum

A technique that uses light to create particle collisions that create light is poised to provide unprecedented access to the inner workings of atoms and molecules.

Paul Corkum is a professor of physics at the University of Ottawa and director of attosecond science at the National Research Council Canada, both in Ontario.

In 1906 Ernest Rutherford discovered that  $\alpha$  particles deflect as they pass through a mica film. That experiment, which helped Rutherford identify the atomic nucleus, was a dramatic demonstration that collisions between particles could tell us about the structure of matter. Now, a century later, high-energy collisions between subatomic particles have revealed the fundamental building blocks of our world—quarks, muons, and so on—and lower-energy collisions have been central to understanding and harnessing nuclear physics.

Just over 50 years after Rutherford's experiment, the laser was demonstrated. Since then, optical physics, which deals with interactions between light and matter, has developed powerful methods for exciting, probing, and controlling matter and its dynamics. The precision of optical experiments has reached the point where some of the most fundamental questions of particle physics can be tested better optically than by collisions.

Although optical and collision physics are traditionally considered separate disciplines sharing little, if any, overlap, the emerging field of recollision physics unites the two. In a recollision, the oscillating field of a laser pulse causes an electron to accelerate away from an atom or molecule and then, upon reversal of the field, career back into its parent ion. Whereas traditional collision physics relies on large accelerators and magnets to arrange the collision, in recollision physics it is the laser field that provides the acceleration and the atom itself that provides the electron with which it is

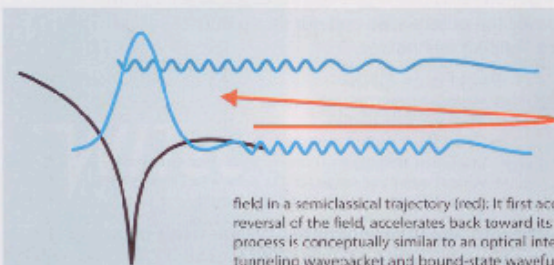
probed. Through recollision, optics gains access to the well-developed capability to probe the structure of matter via collisions (the focus of this article) and collision physics gains access to the capability to excite, probe, and control matter with light.

## Two coherence transfers

Consider an atom illuminated by a pulse of coherent IR light. If the light is intense enough, roughly  $10^{13}$  W/cm<sup>2</sup> or higher (see box 1), then at each crest of the oscillating electromagnetic field, the valence-electron wavefunction will partially ionize, so-called tunnel ionization. Strictly speaking, tunneling is a DC phenomenon. However, Leonid Keldysh showed nearly half a century ago that multiphoton ionization can approximate tunneling in atoms and solids when IR light is used.<sup>1</sup> Thus, I will speak of laser tunneling, or simply tunneling, throughout the paper. Through tunneling, the coherent light pulse splits the electron wavefunction into two mutually coherent parts—the bound-state wavefunction and the tunnel-ionized wavepacket. (See figure 1.)

Once the electron has tunneled, the resulting wavepacket—now in the continuum, freed from the pull of its parent ion—is driven in a semiclassical motion by the laser field. The classical approximation of subcycle electron motion has a long history in plasma physics.<sup>2</sup> It is useful when many photons are involved.

What happens next depends on the polarization of the light pulse. If the polarization is circular, then as soon as any portion of the wavepacket emerges from the atom or mole-

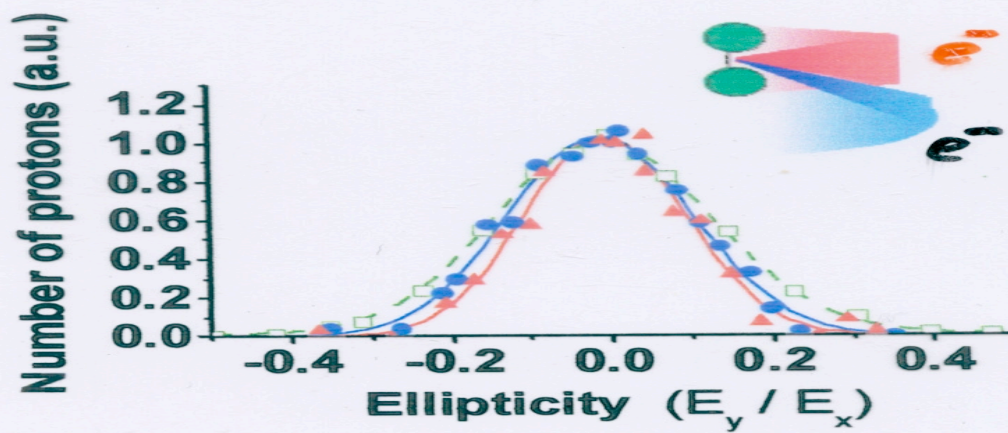
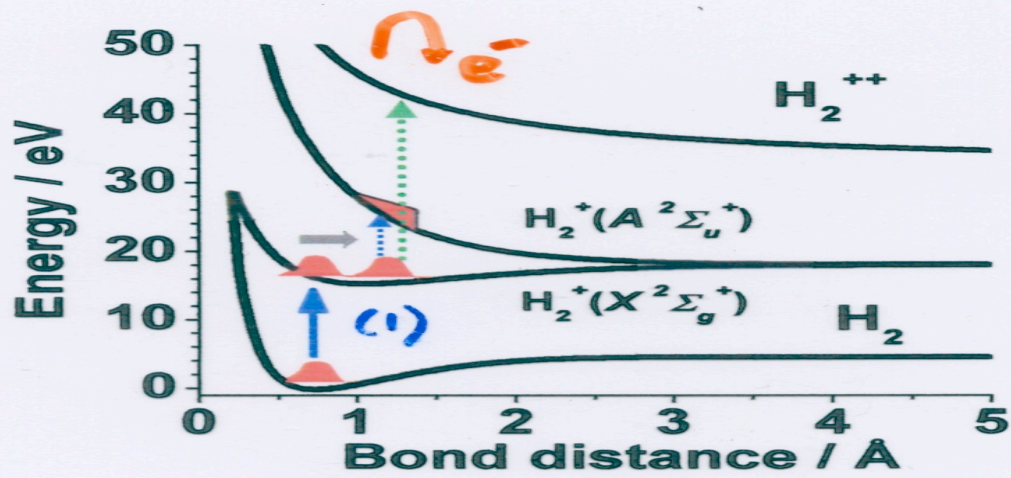


**Figure 1. The basics of recollision.** In the first step, an intense pulse of coherent IR light skews the potential well (black) of an atom or molecule's electron. That allows the bound-state electron wavefunction (blue, sketched as a Gaussian) to tunnel and split, creating a wavepacket in the continuum. There, the wavepacket is driven by the oscillating laser

field in a semiclassical trajectory (red): It first accelerates away from the atom and then, upon reversal of the field, accelerates back toward its origin, recolliding with its parent ion. The process is conceptually similar to an optical interferometer. The relative wavelengths of the tunneling wavepacket and bound-state wavefunction are illustrated approximately to scale.

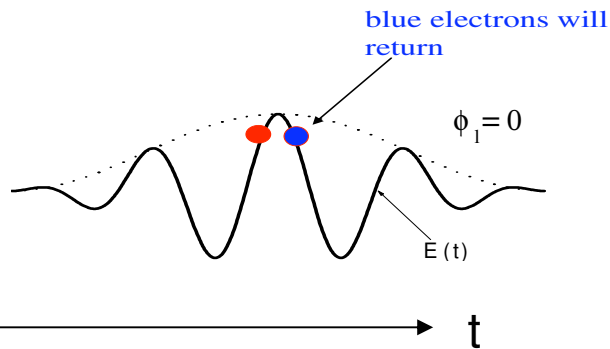
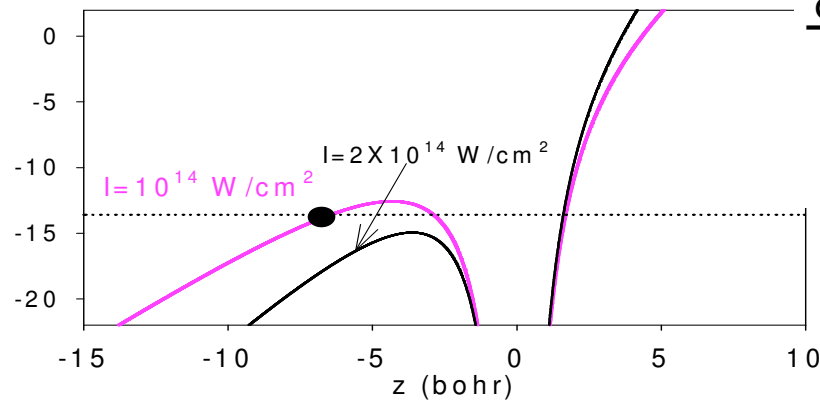
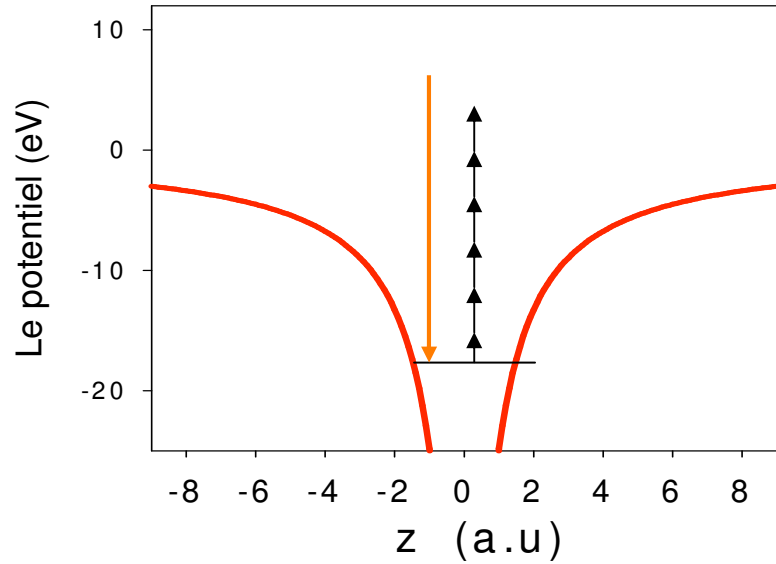




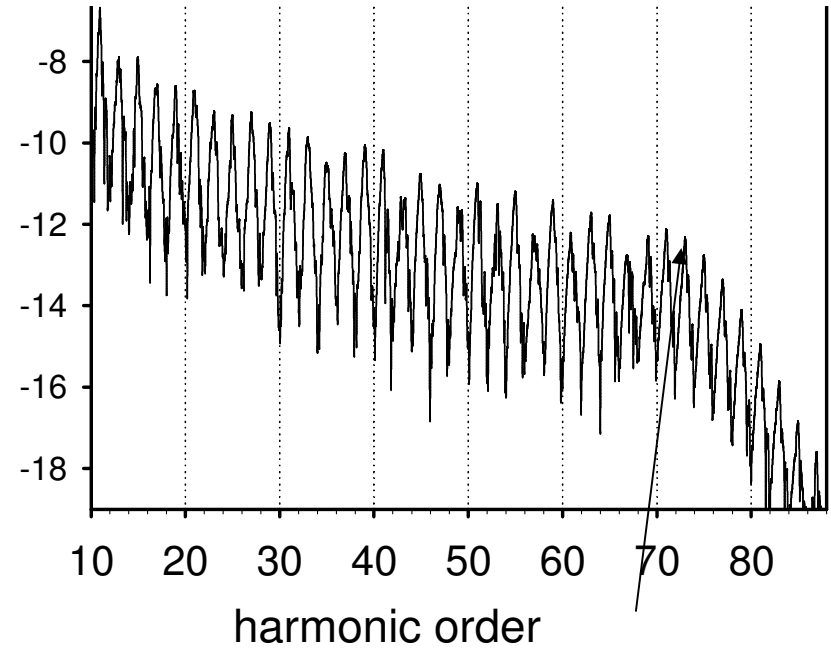


Nature 417. p. 917 (2002)

$$V(z, \rho) = -e^2 / [z^2 + \rho^2]^{1/2}$$



log<sub>10</sub> power spectrum



Cutoff at:

$$n_{cut} = [I_p + 3.17 U_p] / \omega_L, \quad U_p = \frac{I / I_{at}}{4 \omega_L^2},$$

$$I_{at} = 3.51 \times 10^{16} \text{ W/cm}^2.$$

ADB et al, J Mod Opt 52,411(2005)

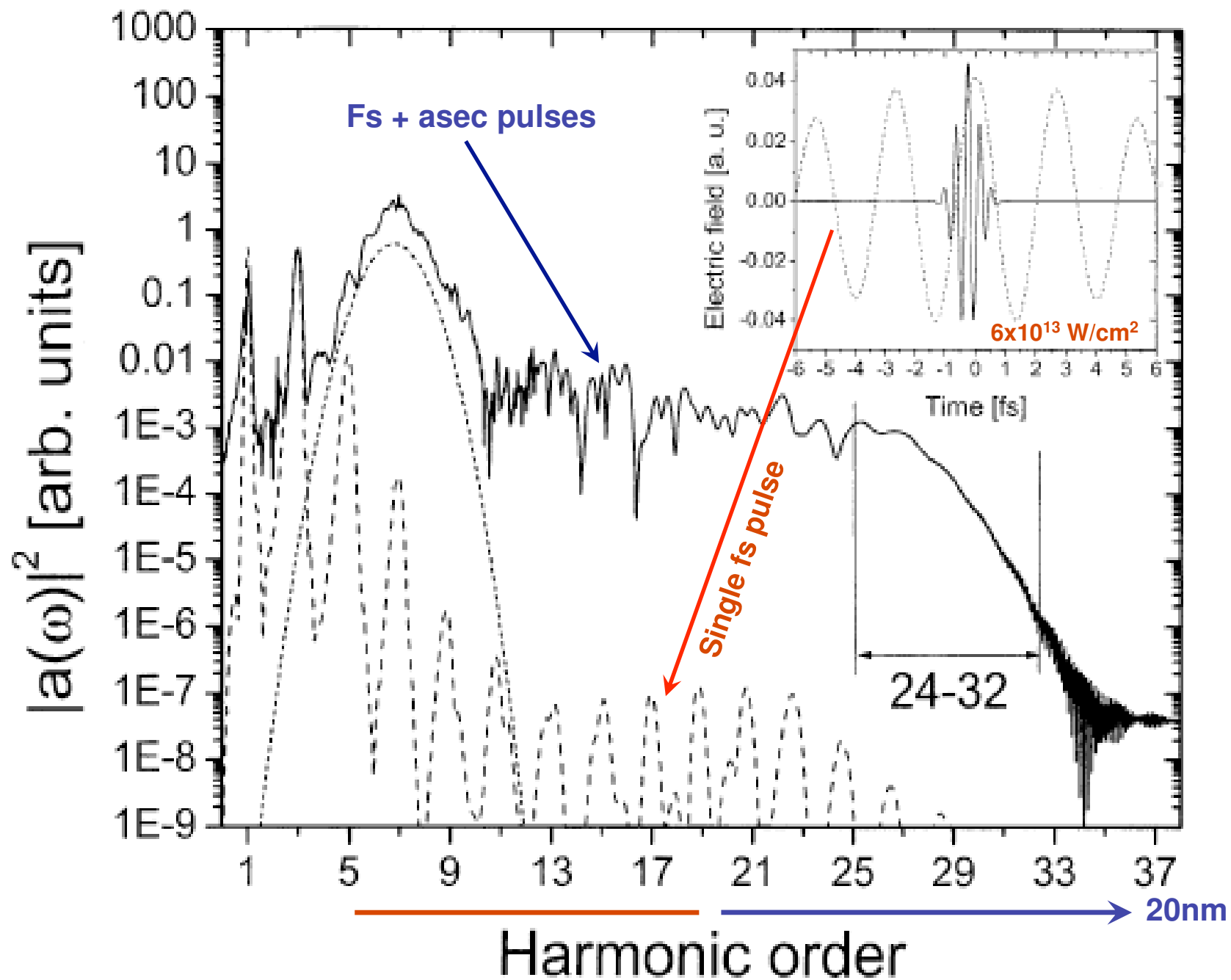
(Vo > 0)

Semi-classical model, by P. Corkum

(Vo = 0)

(1993).





Step 1: get spectrum

$$a(t) = \langle \psi(t) | -\delta H / \delta r | \psi(t) \rangle$$

$$a(\omega) = \frac{1}{2\pi} \int_{-\infty}^{+\infty} a(t) e^{-i\omega t} dt$$

Step 2: select frequency region between  $\omega_1 < \omega < \omega_2$

Step 3: come back to time domain

$$\tilde{a}(t) = \int_{\omega_1}^{\omega_2} a(\omega) e^{i\omega t} d\omega$$

$$\Delta \omega = \omega_2 - \omega_1$$

$$\tau = \frac{1}{\Delta \omega} \rightarrow \text{atto second} = 3 \text{ Angstroms} (10^{-8} \text{ cm}) / c (3 \times 10^{10} \text{ cm/s})$$

# Model

Coupling of macroscopic Maxwell's equations with many TDSE's.

Lorin, Chelkowski, Bandrauk, *Comput. Phys. Comm.* vol. 177 (2007)

$$\left\{ \begin{array}{l} \partial_t \mathbf{B}(\mathbf{r}, t) \\ \partial_t \mathbf{E}(\mathbf{r}, t) \\ \nabla \cdot \mathbf{B}(\mathbf{r}, t) \\ \nabla \cdot (\mathbf{E}(\mathbf{r}, t) + \mathbf{P}(\mathbf{r}, t)) \\ \\ \mathbf{P}(\mathbf{r}, t) = n(\mathbf{r}) \sum_{i=1}^m \mathbf{P}_i(\mathbf{r}, t) \\ i \partial_t \psi_i(\mathbf{r}', t) \end{array} \right. = \begin{array}{l} -\nabla \times \mathbf{E}(\mathbf{r}, t) \\ \nabla \times \mathbf{B}(\mathbf{r}, t) - 4\pi \partial_t \mathbf{P}(\mathbf{r}, t) \\ 0 \\ 0 \\ \\ n(\mathbf{r}) \sum_{i=1}^m \chi_{\Omega_i}(\mathbf{r}) \int_{\mathbb{R}^3} \psi_i \mathbf{r}' \psi_i^* \\ -\frac{\Delta_{\mathbf{r}'}}{2} \psi_i + \mathbf{r}' \cdot \mathbf{E}_{\mathbf{r}_i} \psi_i + V_c \psi_i, \\ \forall i \in \{1, \dots, m\} \end{array}$$

The numerical model is the one presented in [19], where the gas domain is divided in small cells of gas denoted by  $\Delta v$  (corresponding the  $\Omega_i$ 's of Section 2) and in which we solve 1 TDSE, representing the  $n\Delta v$  molecules of the cell. In practice 3d Maxwell's equations are solved in parallel with  $\sim 140,000$  1d TDSE's, see Fig. 5 and [17]. We then represent at

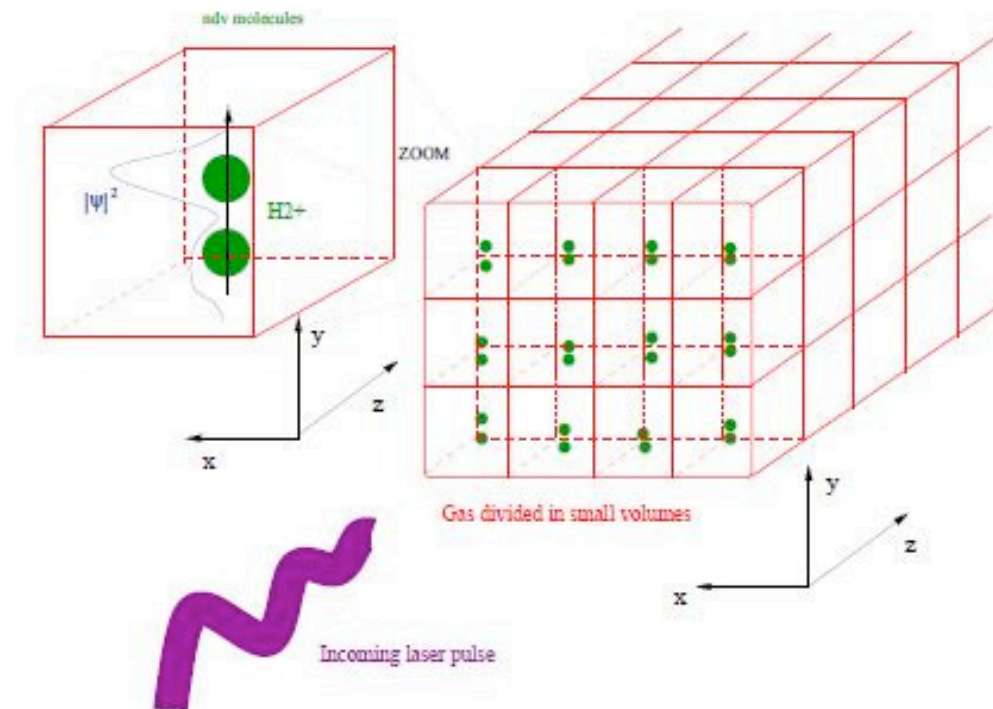


Figure 5: Numerical geometry



# Improvement of the model I - microscopic approach

Another approach is presented in [Lorin, Bandrauk, Chelkowski, Num. Methods for Partial Diff. Eq., \(2008\)](#). A method to transmit free electron from a molecule to another. Based on a particular choice of boundary conditions (Volkov)

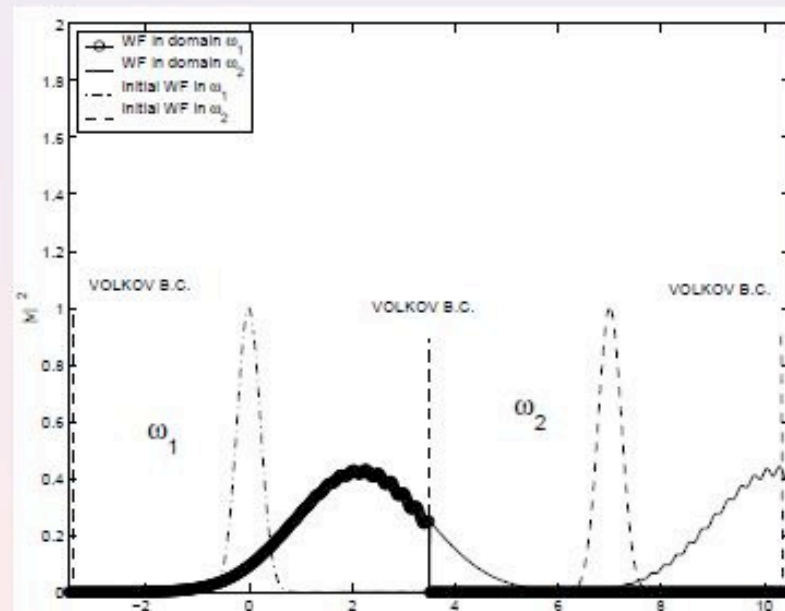


Figure: Free electron transmission



Results I -  $I \sim 2 \times 10^{16} \text{W}\cdot\text{cm}^{-2}$ ,  $n_0 \sim 3 \times 10^{20} \text{mol}\cdot\text{cm}^{-3}$

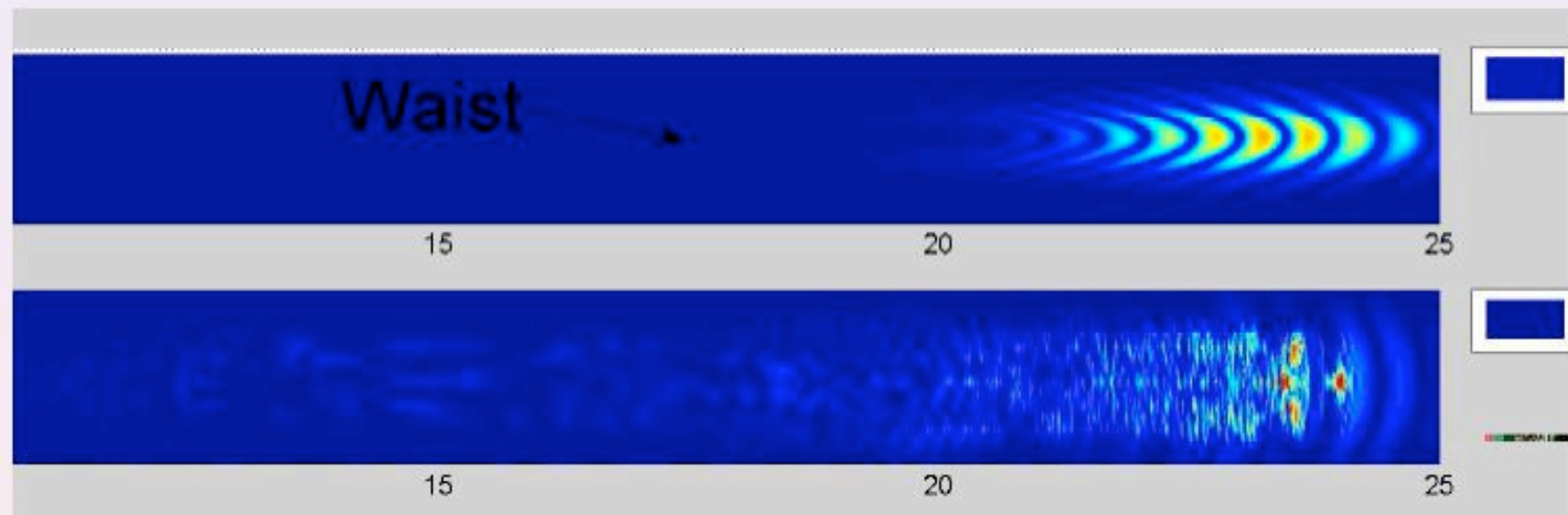
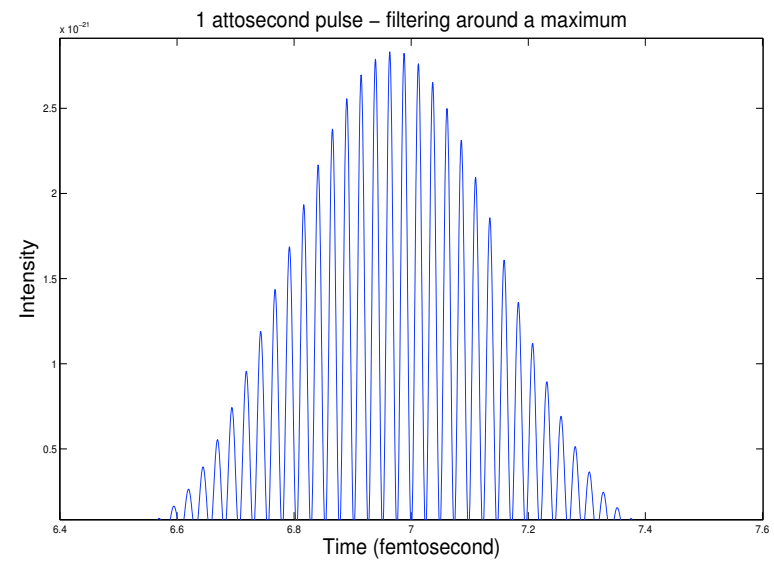
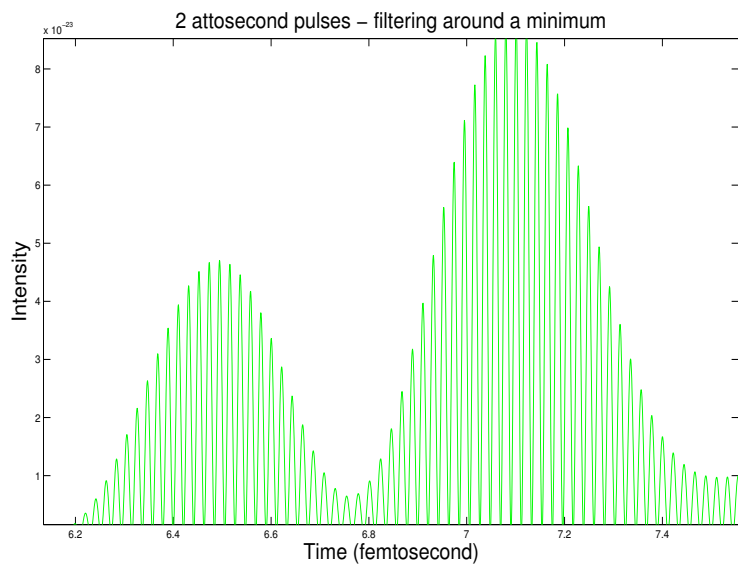
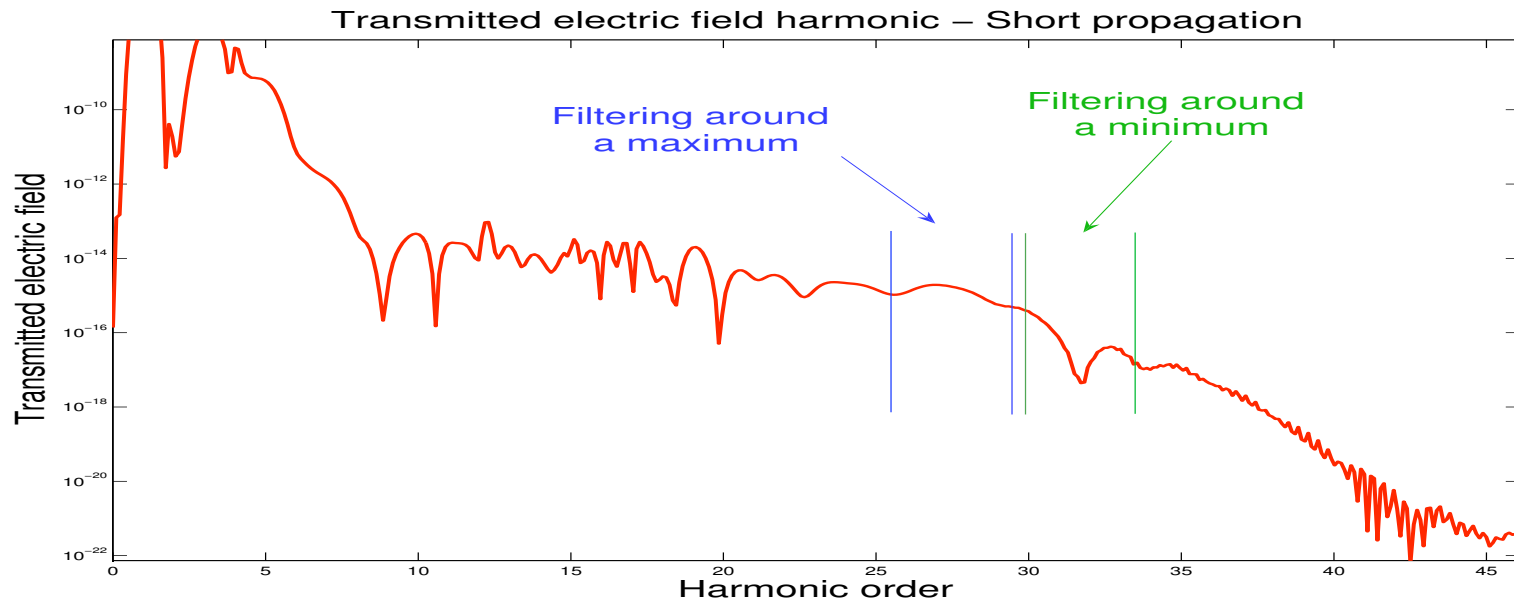
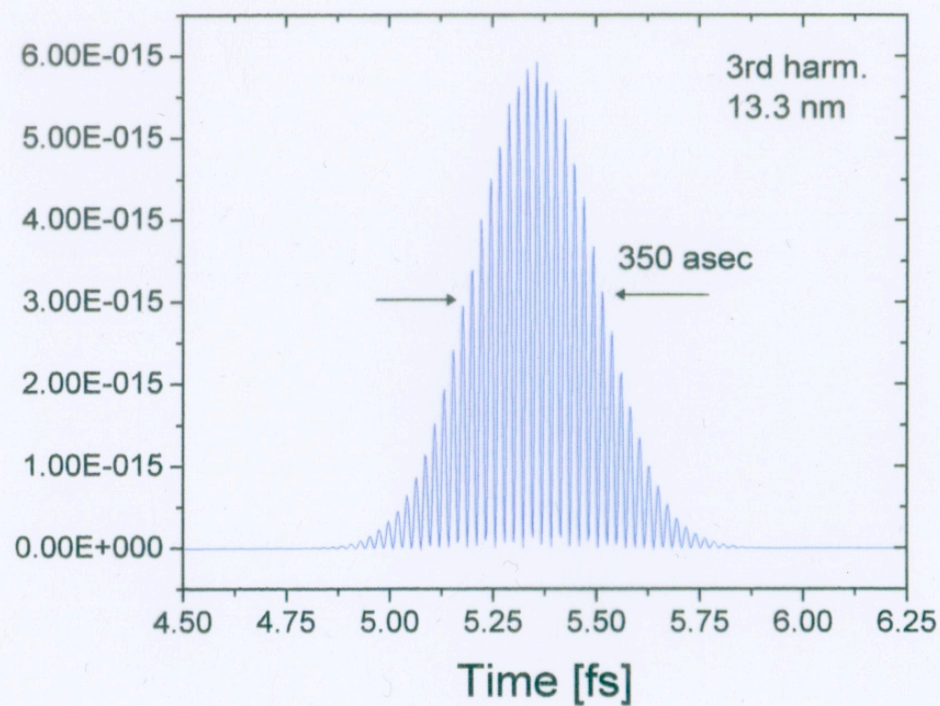
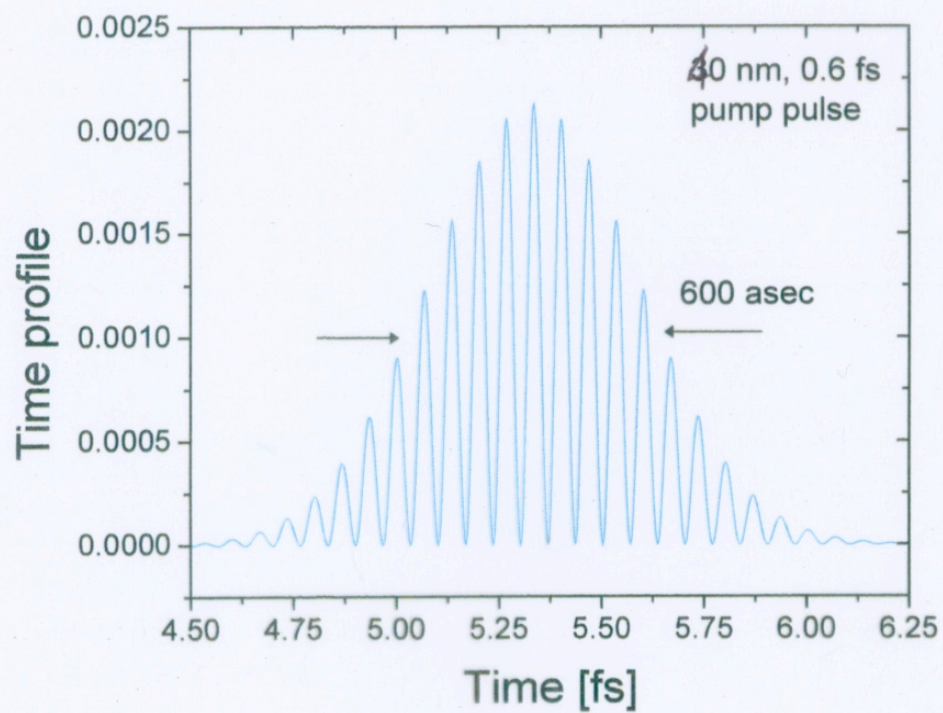


Figure:  $|E_y|^2$  -  $4.5\mu\text{m}$  after the waist in vacuum and gas



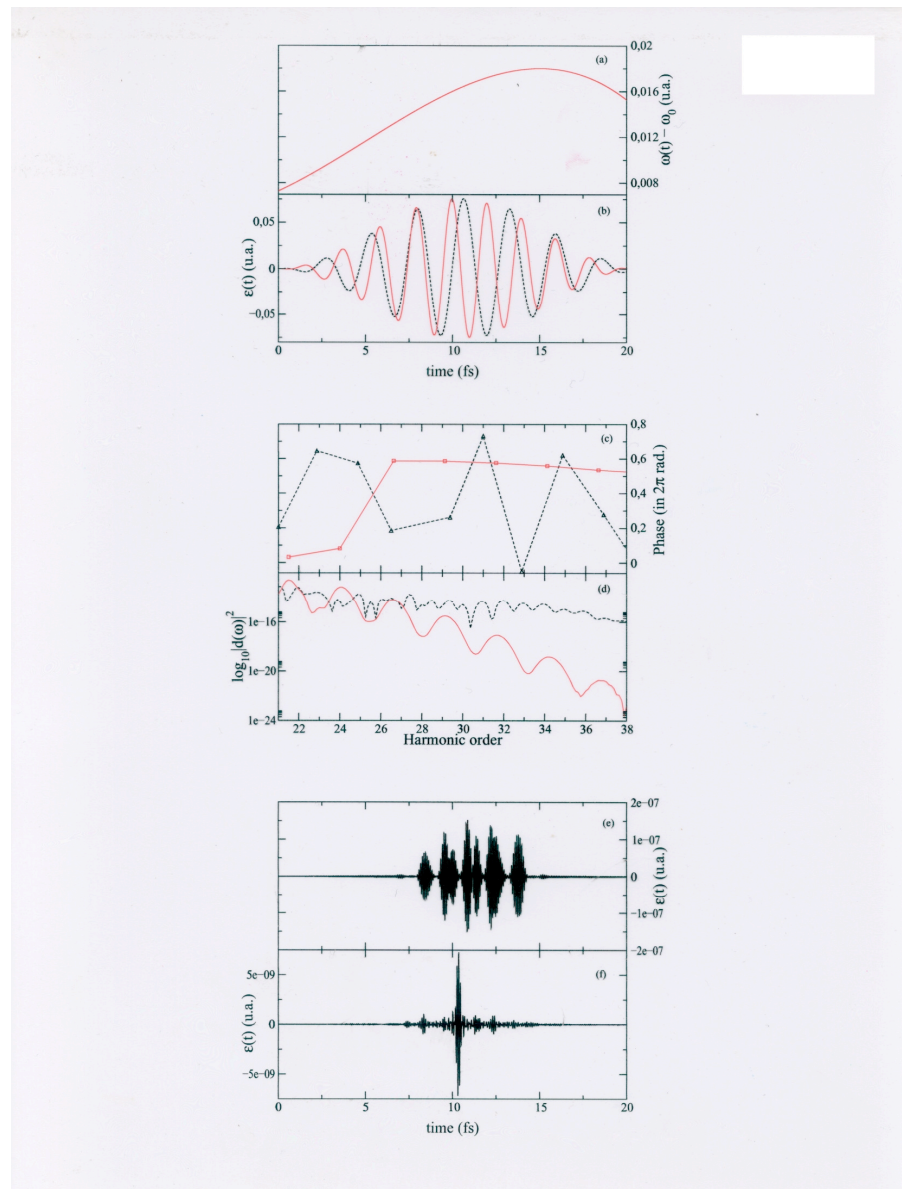
Two (minimum) or one (maximum) attosecond pulses

Frequency-up conversion, 1st -->3rd harmonics



ADB et al, J Molec Str. 735,203(2004)

Goulielmakis, Krausz (2009-2010)



Yedder, LeBris, Chelkowski, Bandrauk, PRA 69, 041802 (2004)

((Bartels.Murnane.Rabitz.PRA 70.043404(2004))



LQ11676

Effect of Nuclear Motion on Molecular High-order Harmonics  
and on Generation of Attosecond Pulses in Intense Laser Pulses

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Abstract

We calculate harmonic spectra and shapes of attosecond pulse trains using numerical solutions of Non-Born Oppenheimer time-dependent Schrödinger equation for 1-D H<sub>2</sub> molecules in an intense laser pulse. A very strong signature of nuclear motion is seen in the time profiles of high order harmonics. In general the nuclear motion shortens the part of the attosecond pulse train originating from the first electron contribution but it may enhance the second electron contribution for longer pulses. The shape of time profiles of harmonics can thus be used for monitoring the nuclear motion.

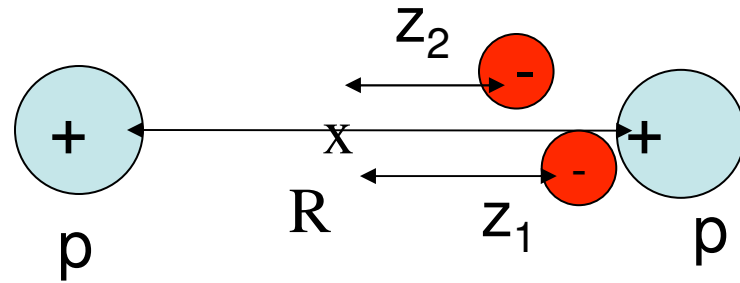
PACS numbers: 42.65.Ky, 42.65.Re, 42.50.Hz, 32.80.Rm

Phys Rev Lett( 2008,)101,153901

J Phys B 42,075602 (2009)



La dynamique de 4-particules:  
 $p+p+e^-+e^-$  décrite par l'éq. de  
 Schrödinger solutionnée numé-  
 riquement



Équation de Schrödinger dépendant de temps pour une molécule  $H_2$

exposée au champ laser intense décrit par :  $E(t)=\epsilon(t) \cos(\omega_L t)$

(polarisation linéaire)

a.u.  $e = \hbar = m_e = 1$ )

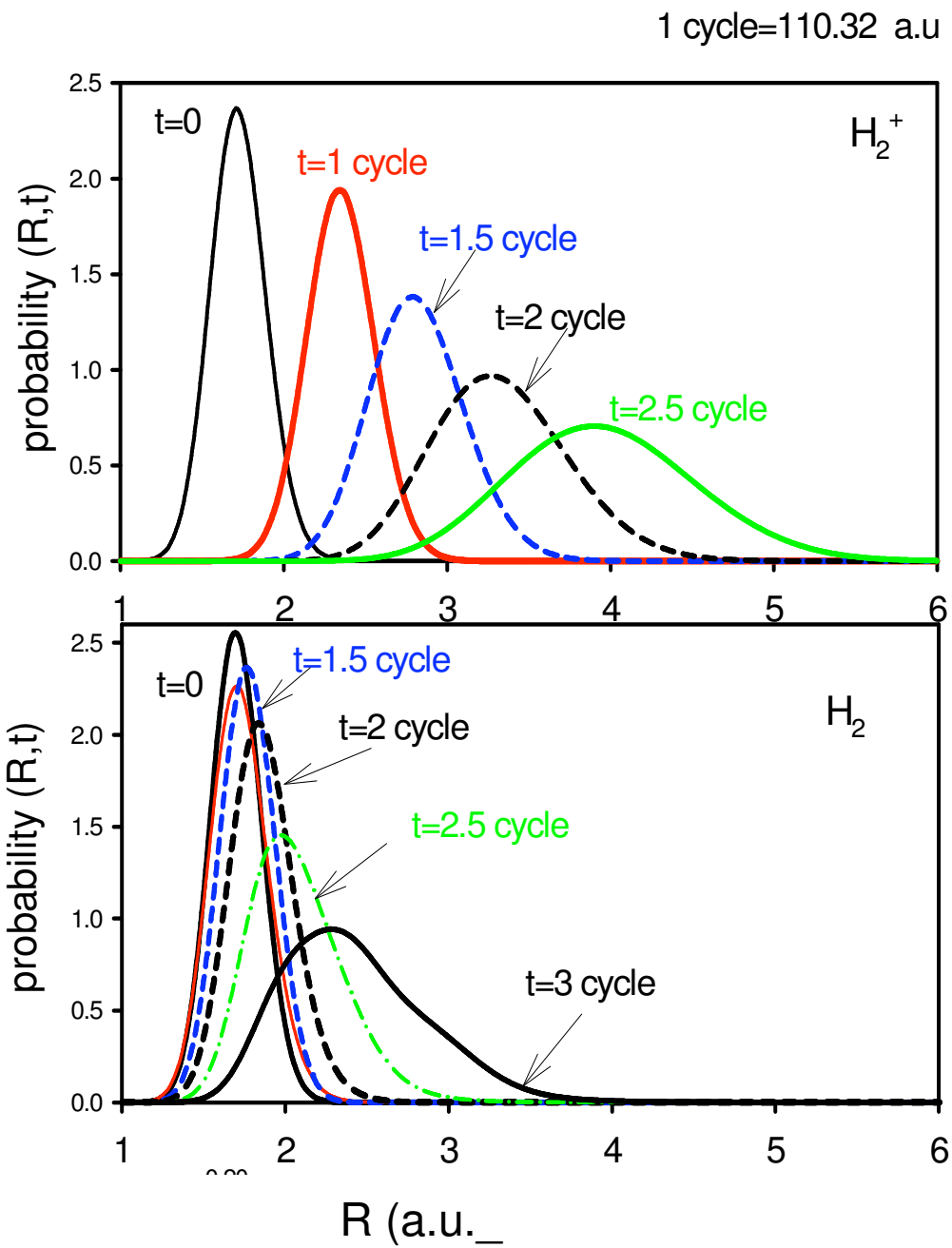
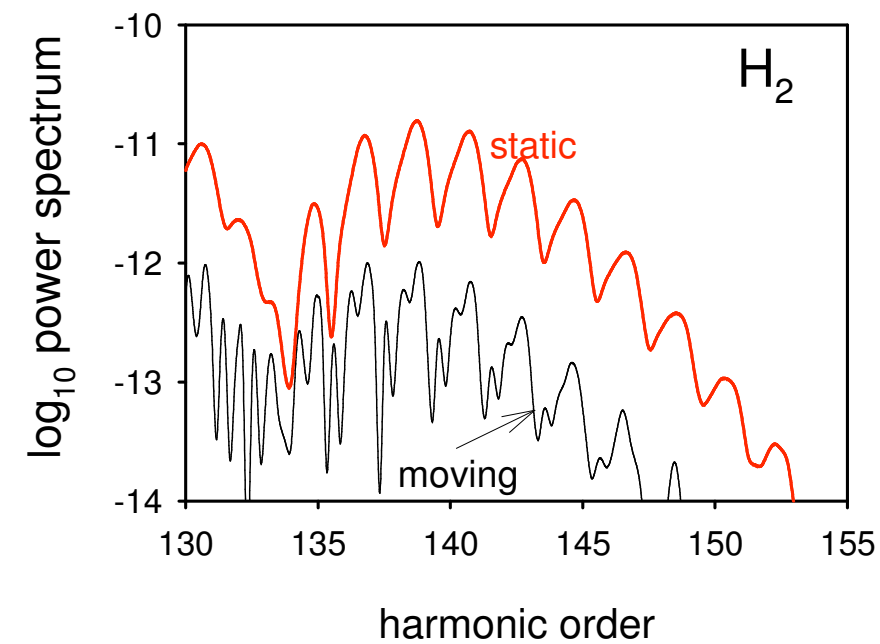
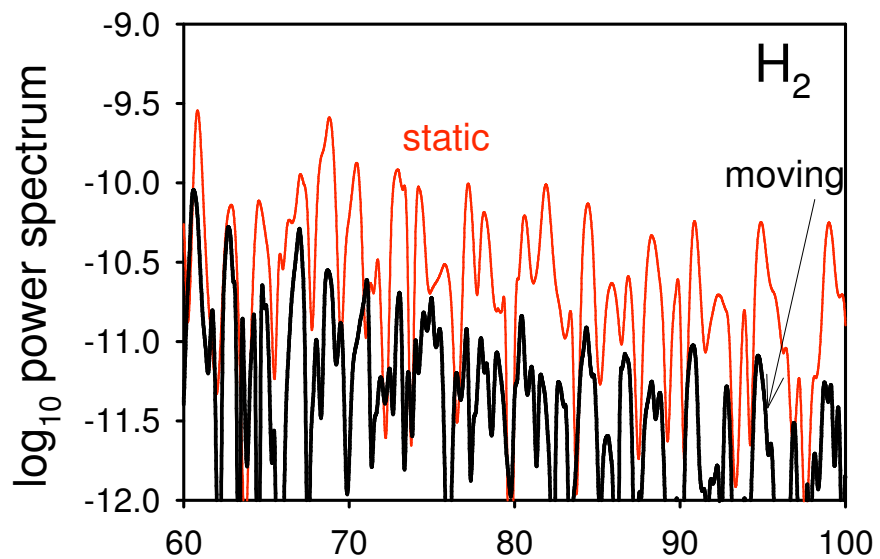
$$i \frac{\partial \psi(z_1, z_2, R, t)}{\partial t} = [H_e + H_N + V(z_1, z_2, t)] \psi(z_1, z_2, R, t), \quad (1)$$

$$H_e = \sum_{i=1}^2 \left[ -\frac{1}{2} \frac{\partial^2}{\partial z_i^2} - \frac{1}{[(z_i + R/2)^2 + c]^{1/2}} - \frac{1}{[(z_i - R/2)^2 + c]^{1/2}} \right] + V_{rep}(z_1, z_2) \quad (2)$$

$$V_{rep}(z_1, z_2) = \frac{1}{[(z_1 - z_2)^2 + d]^{1/2}}, \quad ; H_N = -\frac{1}{2M} \frac{\partial^2}{\partial R^2} + \frac{1}{R} \quad (3)$$

$$V(z_1, z_2, t) = (z_1 + z_2) \epsilon(t) \cos(\omega_L t) \quad (4)$$

$$d(t) = \langle z_1 + z_2 \rangle = \int_{-\infty}^{\infty} dz_1 \int_{-\infty}^{\infty} dz_2 \int_0^{\infty} dR \psi^*(t)(z_1 + z_2) \psi(t)$$

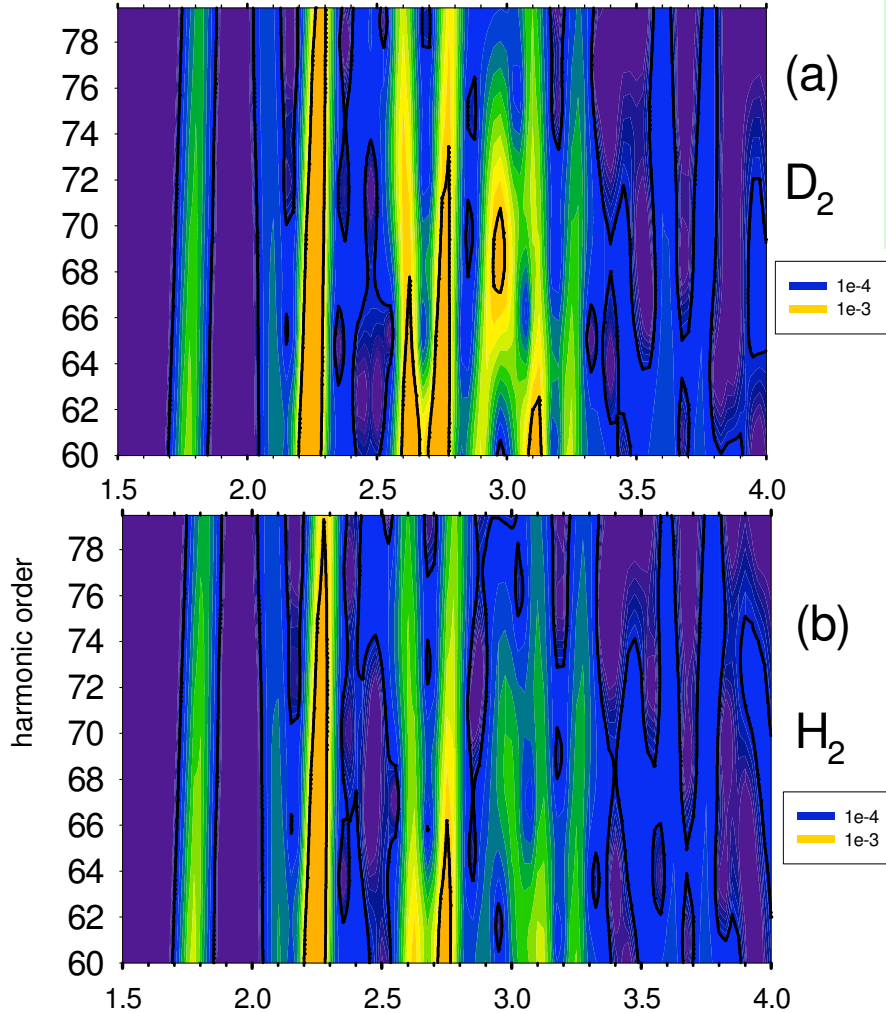


Analyse en temps-frequence  
de Gabor (ondelettes):

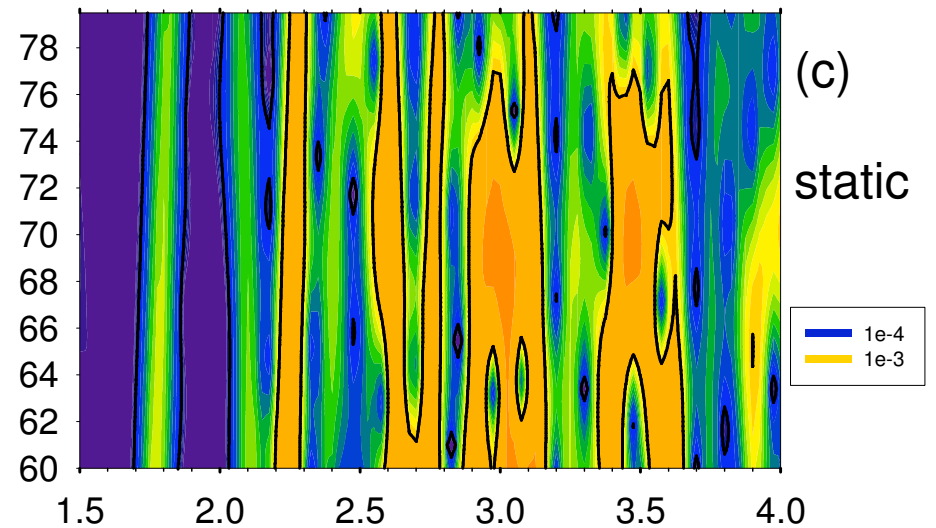
$$= d_G(t, \omega) = \int_{-\infty}^{\infty} dt' G(t, t') \exp(-i\omega t) d(t)$$

$$G(t-t') = \exp\left[-\frac{(t-t')^2}{2\sigma_0^2}\right], \quad \sigma_0 = 0.1 \text{ fs}$$

$$d_G(t, \omega) = \text{cte} \int_{-\infty}^{\infty} d\omega' e^{-b(\omega-\omega')^2} e^{i\omega' t} d_F(\omega')$$



$|d_G(t, \omega)|$  - profile temporaire des  
impulsions atto dans un train,  $\Delta\omega \sim 5-10 \omega_L$



temps (periodes du laser  $T_{\text{las}}$ ) ,  $T_{\text{las}} = 2.67 \text{ fs}$

$T_v(H_2) \sim 7 \text{ fs}$

$$V = \frac{1}{R} - \sum_{j=1}^2 \frac{1}{\sqrt{(z_j - R/2)^2 + a}} + \frac{1}{\sqrt{(z_j + R/2)^2 + a}}$$

$$a_{el} = \frac{d^2}{dt^2} \overline{z(t)} = -2E(t) - \left\langle \frac{\partial V}{\partial z_1} + \frac{\partial V}{\partial z_2} \right\rangle = -2E(t) - \langle F_+ + F_- \rangle$$

$$a_R = \frac{d^2}{dt^2} \overline{R(t)} = -\left\langle \frac{1}{R^2} \right\rangle - \left\langle \frac{\partial V}{\partial R} \right\rangle = -\left\langle \frac{1}{R^2} \right\rangle - \frac{1}{2} \langle F_+ - F_- \rangle$$

where

$$F_{\pm} = \sum_{j=1}^2 \frac{z_j \pm R/2}{[(z_j \pm R/2)^2 + a]^{3/2}}$$

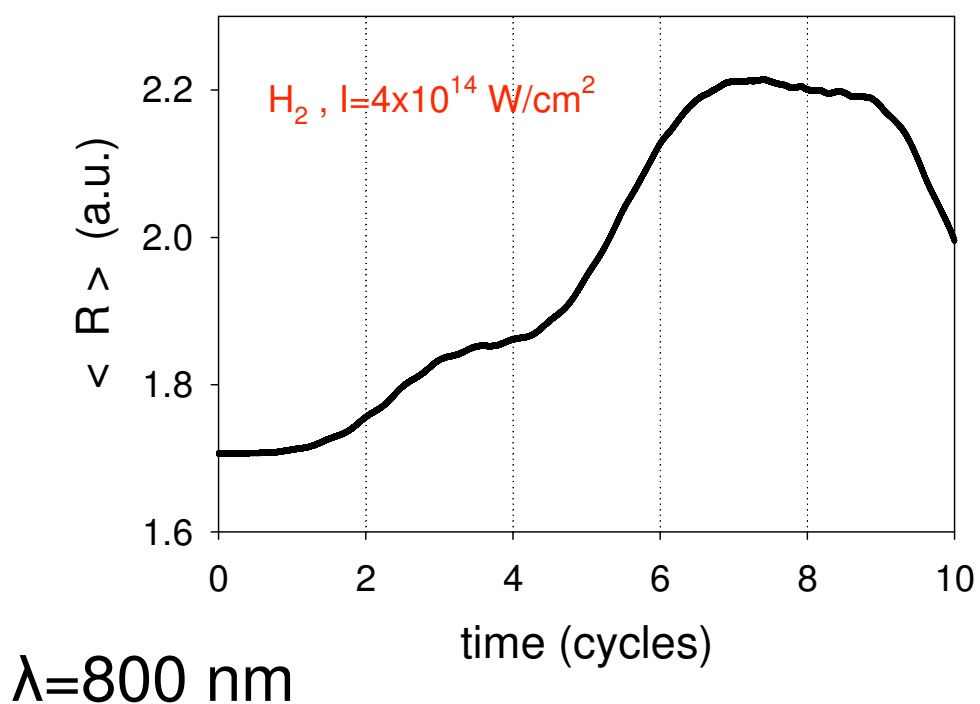
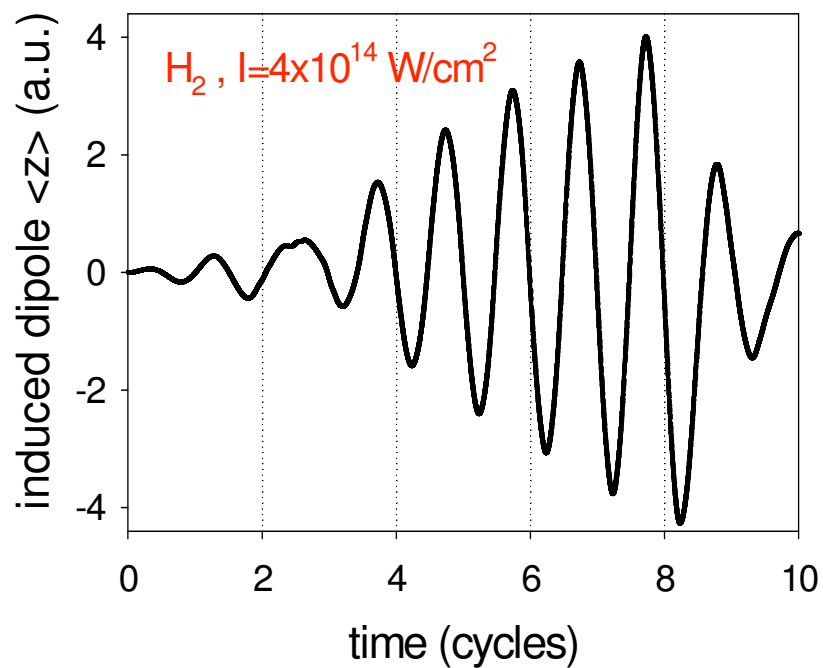
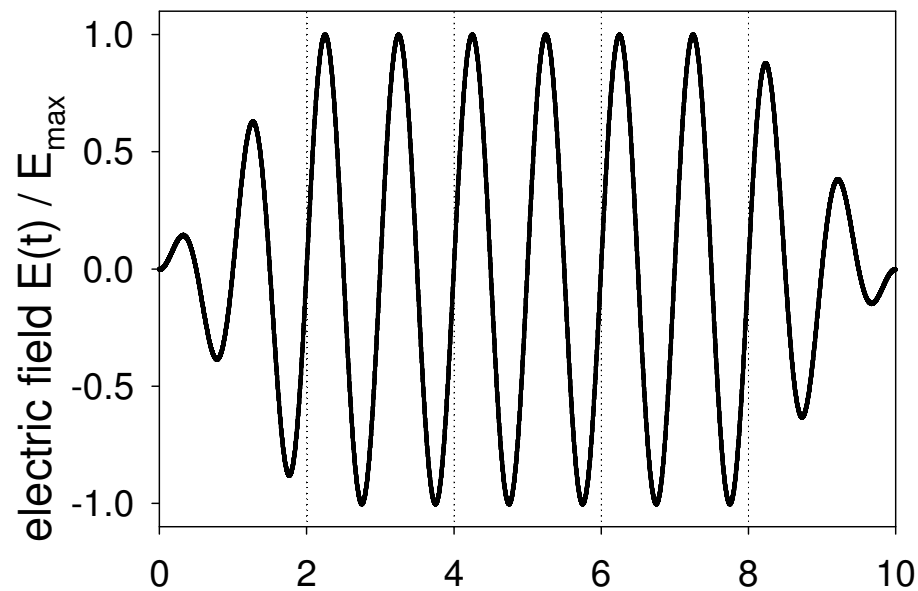
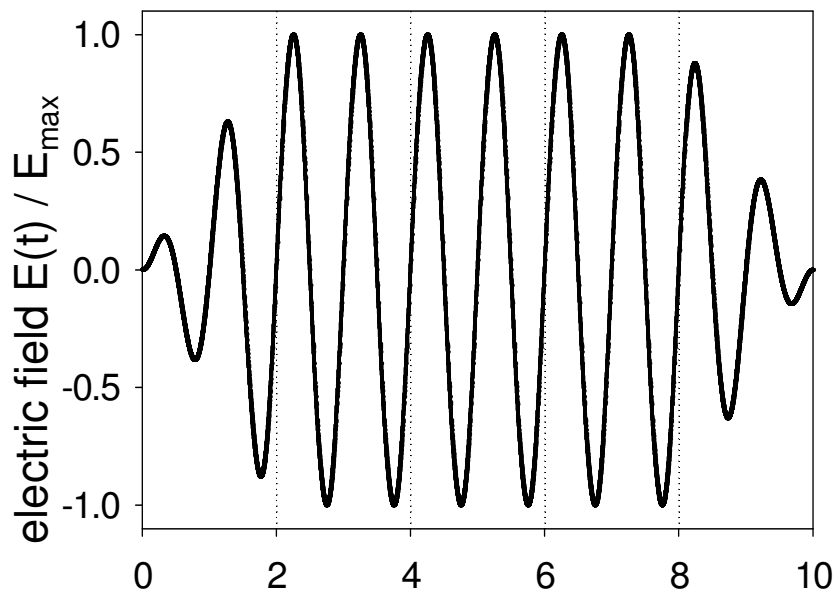
Thus, very similar expressions determine electron and proton acceleration.  
For electrons:

$F_+ + F_- = f_{el}(z_1, z_2)$  is an odd function with respect to the inversion

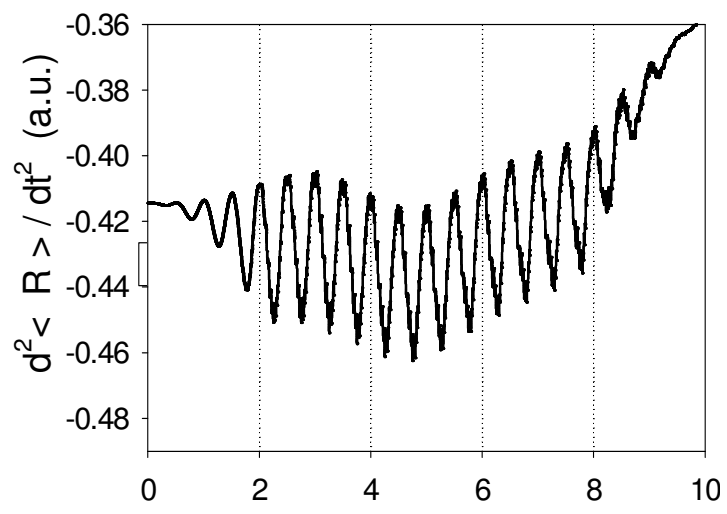
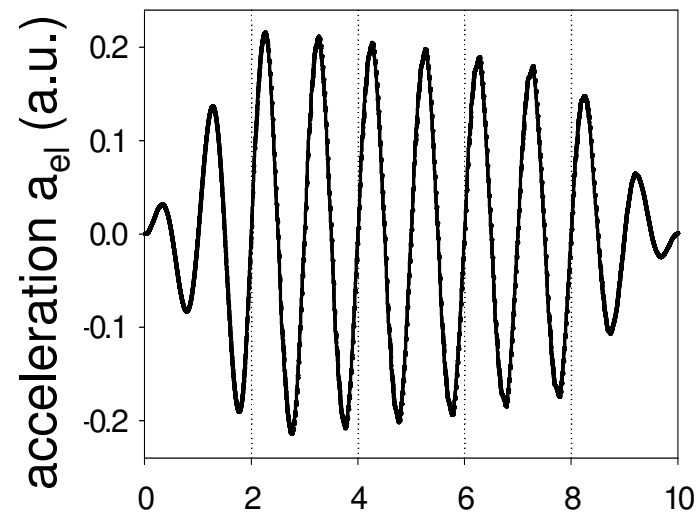
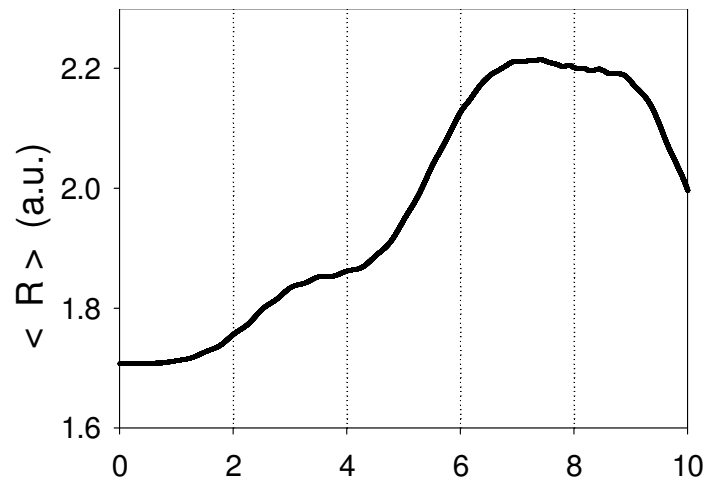
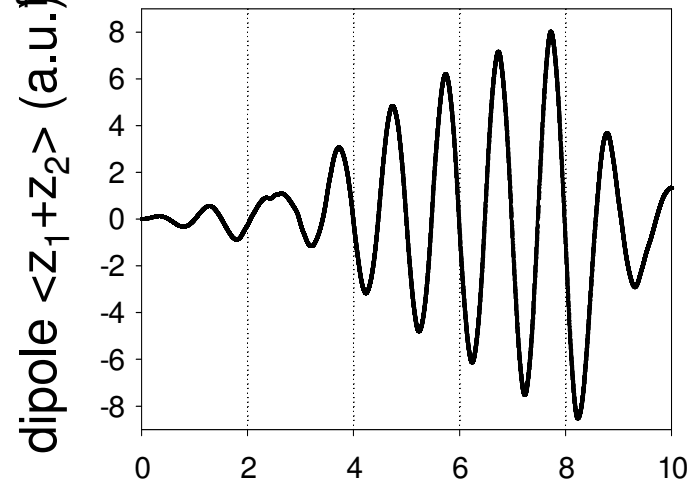
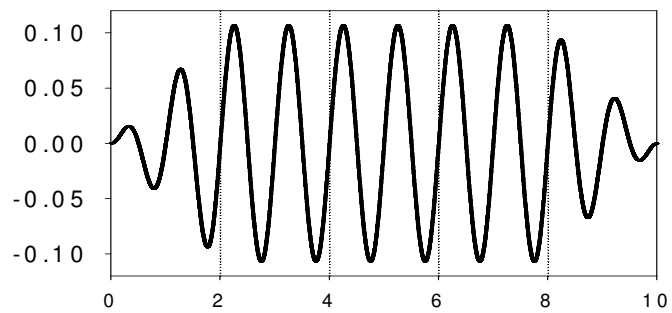
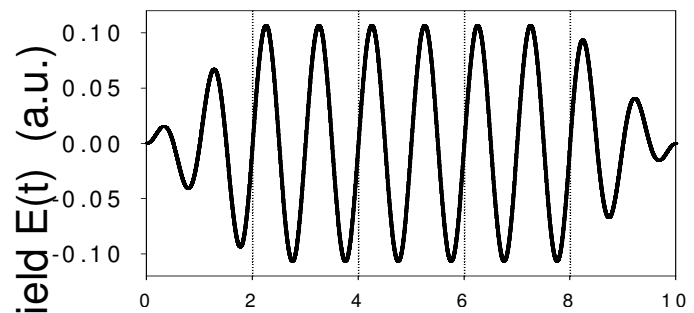
$z_1 \rightarrow -z_1, z_2 \rightarrow -z_2$  leading to odd harmonics, whereas for protons

$F_+ - F_- = f_{prot}(z_1, z_2)$  is an even function with respect to the inversion

$z_1 \rightarrow -z_1, z_2 \rightarrow -z_2$  leading to even harmonics.

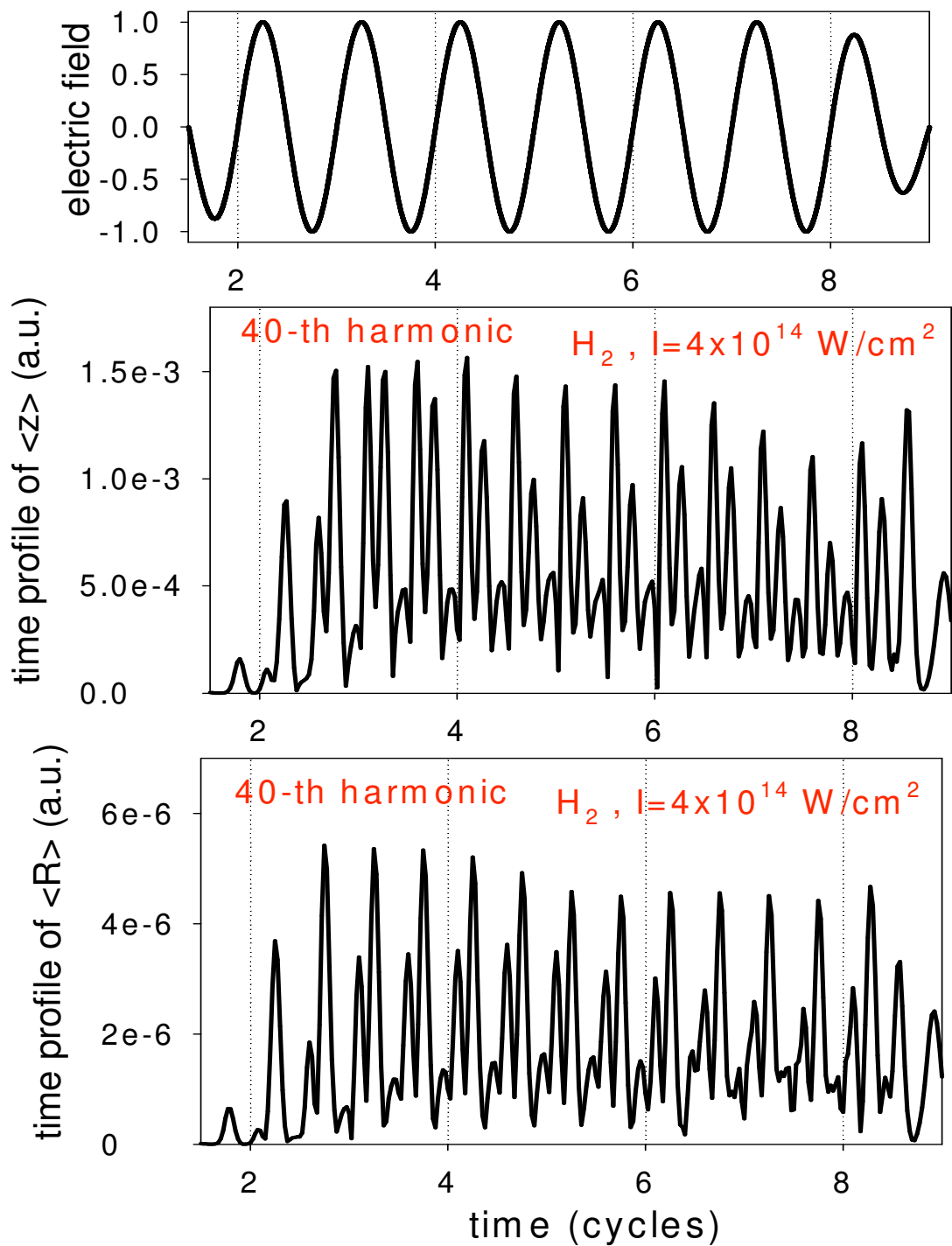






time (cycles)

time (cycles)



$\lambda=800 \text{ nm}$

# To exploit attosecond technology

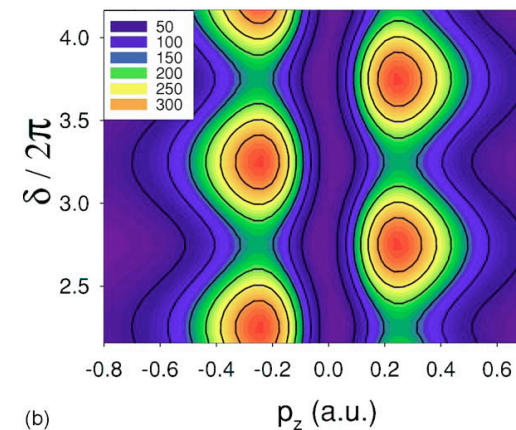
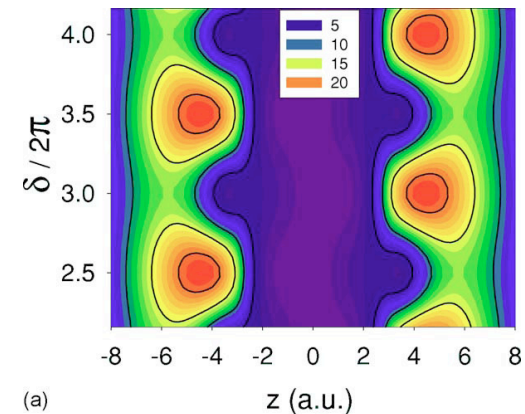
FP1

## Measuring electron wave packets

1. Attosecond pulses are fast enough to observe electron wave packets.
2. Electron wave packets are resolved through changes to the photo-electron spectrum as a function of pump-probe time delay.
3. The attosecond pulse projects the momentum distribution into the continuum.

Yudin et al, Phys Rev A 72, 51401(R) (2005)

“Observing Electron Motion in Molecules”  
SChelkowski, ADB J. Phys. B39, S409 (2006)



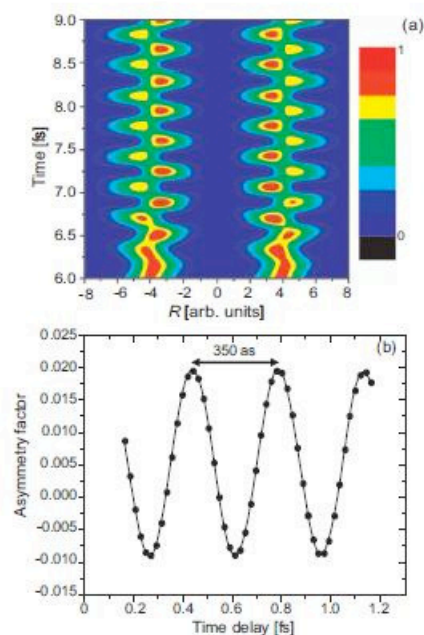


FIG. 53. (Color) Proposal for inducing attosecond electron wave-packet dynamics by a 0.8-fs, 115-nm VUV pump pulse in  $\text{H}_2^+$  and probing it with a time-delayed 0.1-fs, 20-nm XUV pulse (Bandrauk *et al.*, 2004). Both pulses are polarized parallel to the molecular axis. (a) Contour plot of the electron probability distribution along the molecular axis for an internuclear distance of eight atomic units vs pump-probe delay. (b) Asymmetry factor  $(P_- - P_+) / (P_- + P_+)$  vs delay, where  $P_+$  and  $P_-$  represent the probability of observing the electron liberated by the XUV probe in the positive or negative direction (along the molecular axis), respectively. Adapted from Bandrauk *et al.*, 2004.

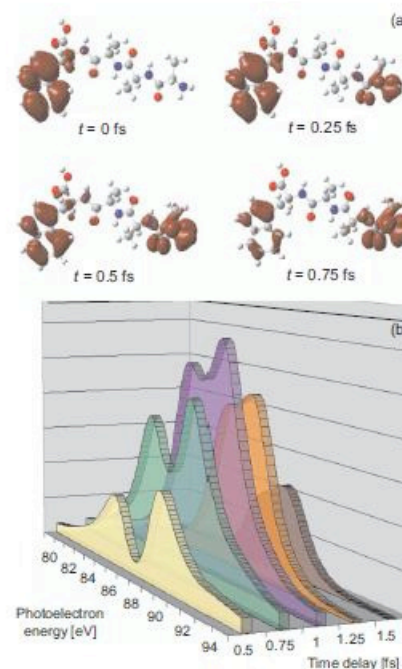
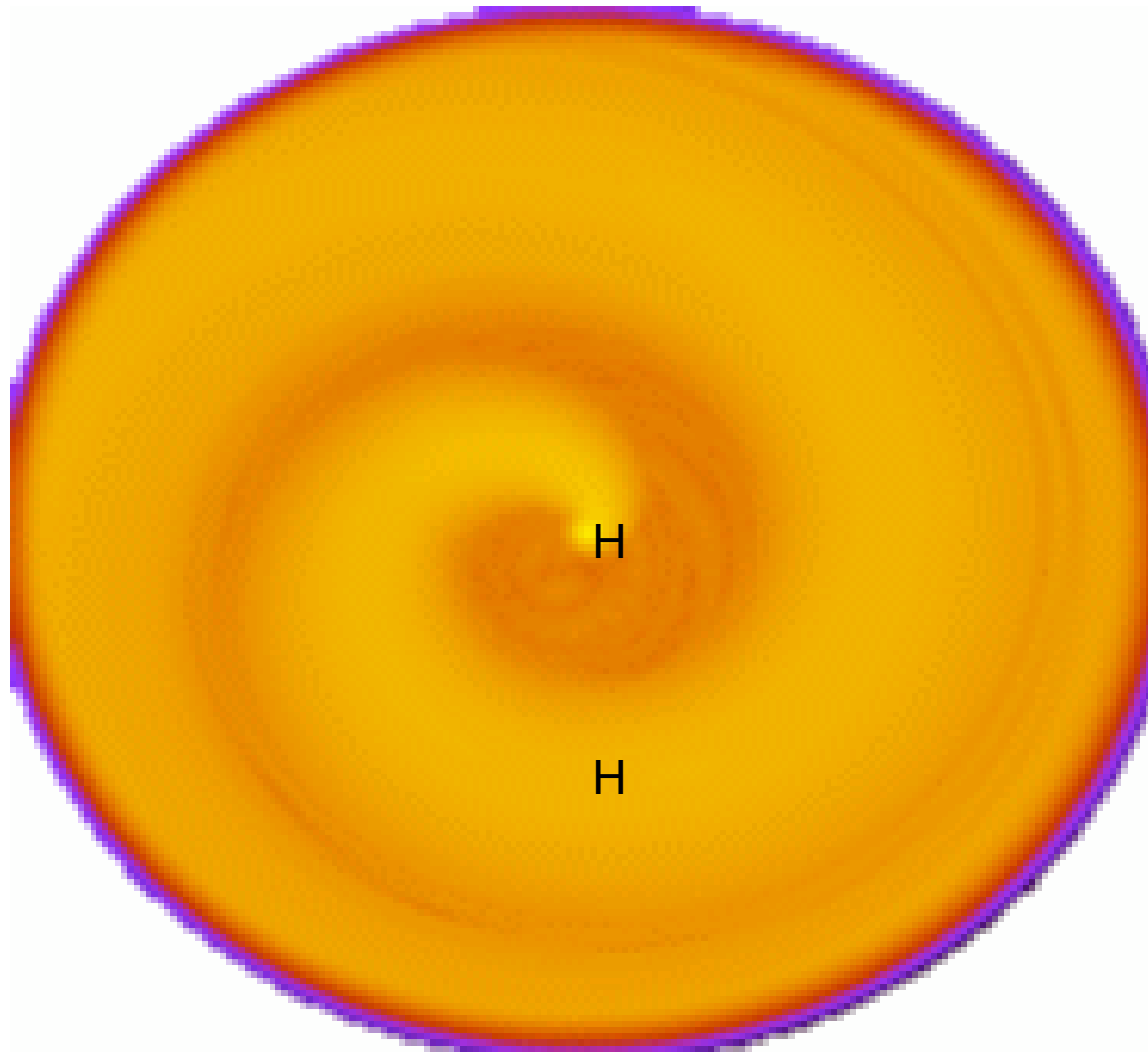


FIG. 54. (Color) Computed ultrafast positive charge (hole) migration in a tryptophane-terminated tetrapeptide (Remacle and Levine, 2006a, 2007). (a) The hole density shown in red indicates that the charge swings across the entire peptide from the aromatic amino acid on the left to the N end on the right within less than one femtosecond, following excitation of the electronic wave packet on an attosecond time scale. This hyperfast charge migration is proposed to be probed by measuring the kinetic energy distribution of photoelectrons released by a time-delayed sub-fs XUV pulse. (b) A series of such freeze-frame spectra calculated for a 250-as, 95-eV probe pulse at different pump-probe delays. From Remacle and Levine.

Circular polarization Excitation at 800 nm  $I=10^{14}$  W/cm<sup>2</sup>



Electron Whirlpool – Tourbillon Electronique –  
Elektronischer Wirbel ( J Manz- FU Berlin )



## II. THEORETICAL MODELS

In linearly polarized recollision with parent ions, maximum harmonic energies are given from the initial zero velocity ionization model by  $I_p + 3.17U_p$  [3–6], whereas collision with neighboring ions gives harmonic energies up to  $I_p + 8U_p$  [9–12]. For circularly polarized laser pulses of maximum amplitude  $E_0$ , corresponding to intensity  $I_0 = c\epsilon_0 E_0^2/2$  and frequency  $\omega_0$ ,

$$E_x(t) = E_0 \cos(\omega_0 t + \phi), \quad E_y(t) = E_0 \sin(\omega_0 t + \phi), \quad (1)$$

the classical field equations of motion [ $\ddot{x}(t) = -E_x(t)$ ,  $\ddot{y}(t) = -E_y(t)$ ] give the laser-induced velocities [we use atomic units (a.u.)  $e = \hbar = m_e = 1$  throughout]

$$\begin{aligned} \dot{x}(t) &= -\frac{E_0}{\omega_0} [\sin(\omega_0 t + \phi) - \sin \phi], \\ \dot{y}(t) &= -\frac{E_0}{\omega_0} [\cos \phi - \cos(\omega_0 t + \phi)], \end{aligned} \quad (2)$$

with initial velocity conditions  $\dot{x}(0) = \dot{y}(0) = 0$ , and displacements,

$$\begin{aligned} x(t) &= -\frac{E_0}{\omega_0^2} [\cos \phi - \cos(\omega_0 t + \phi) - \omega_0 t \sin \phi], \\ y(t) &= -\frac{E_0}{\omega_0^2} [\omega_0 t \cos \phi + \sin \phi - \sin(\omega_0 t + \phi)]. \end{aligned} \quad (3)$$

Both the time-dependent energy from Eq. (2),

$$\begin{aligned} K_e(t) &= \frac{1}{2} [\dot{x}^2(t) + \dot{y}^2(t)] \\ &= \left(\frac{E_0}{\omega_0}\right)^2 (1 - \cos \omega_0 t), \end{aligned} \quad (4)$$

with maximum value  $8U_p$  at  $\omega_0 t_c = (2n + 1)\pi$ , where  $t_c$  is collision time, the ponderomotive energy of electron in circularly polarized laser fields  $U_p = E_0^2/4\omega_0^2$ , and the corresponding maximum electron displacement (transfer) to a neighboring ion from Eq. (3),

$$R_n = \sqrt{x^2(t_c) + y^2(t_c)} = \frac{2E_0}{\omega_0^2} \sqrt{1 + \left(n + \frac{1}{2}\right)^2 \pi^2}, \quad (6)$$

for integer  $n$ , are independent of the CEP,  $\phi$ . For  $x$ -aligned molecules,

$$\begin{aligned} x(t_c) &= R_n = -\frac{2E_0}{\omega_0^2} \left[ 1 + \left(n + \frac{1}{2}\right)^2 \pi^2 \right] \cos \phi, \\ y(t_c) &= 0, \end{aligned} \quad (7)$$

where  $\tan \phi = -(n + \frac{1}{2})\pi$ .

With a two-color circularly polarized laser field,

$$\begin{aligned} E_x(t) &= E_0 [\cos(\omega_0 t + \phi_1) + \cos(2\omega_0 t + \phi_2)], \\ E_y(t) &= E_0 [\sin(\omega_0 t + \phi_1) + \sin(2\omega_0 t + \phi_2)], \end{aligned} \quad (8)$$

the CEPs  $\phi_1$  and  $\phi_2$  determine the optimal values of  $K_e(t)$  and  $R(t)$  for MHOHG. The corresponding laser-induced

velocities are

$$\begin{aligned} \dot{x}(t) &= -\frac{E_0}{\omega_0} [\sin(\omega_0 t + \phi_1) - \sin \phi_1 + \cos(\omega_0 t + \phi_2) \sin \omega_0 t], \\ \dot{y}(t) &= -\frac{E_0}{\omega_0} [\cos \phi_1 - \cos(\omega_0 t + \phi_1) + \sin(\omega_0 t + \phi_2) \sin \omega_0 t], \end{aligned} \quad (9)$$

and the displacements are

$$\begin{aligned} x(t) &= -\frac{E_0}{4\omega_0^2} [4 \cos \phi_1 - 4\omega_0 t \sin \phi_1 - 4 \cos(\omega_0 t + \phi_1) \\ &\quad - \cos(2\omega_0 t + \phi_2) + \cos \phi_2 - 2\omega_0 t \sin \phi_2], \\ y(t) &= -\frac{E_0}{4\omega_0^2} [4 \sin \phi_1 + 4\omega_0 t \cos \phi_1 - 4 \sin(\omega_0 t + \phi_1) \\ &\quad - \sin(2\omega_0 t + \phi_2) + \sin \phi_2 + 2\omega_0 t \cos \phi_2]. \end{aligned} \quad (10)$$

Maximizing kinetic energy  $K_e$  with respect to  $\phi_1$  and  $\phi_2$  gives the net optimal CEP condition  $\phi = \phi_1 - \phi_2 = n\pi + \omega_0 t/2$ . Inserting this condition into  $K_e$ , Eq. (4), and maximizing the resulting  $K_e$  with respect to  $\omega_0 t_c$  gives the result for  $n = 0$ ,  $\omega_0 t_c = 2\pi/3$ , and  $\phi = \pi/3$ , whereas for  $n = 1$ ,  $\omega_0 t_c = 4\pi/3$ , and  $\phi = -\pi/3$ .

For  $n = 0$  the choice of phases  $\omega_0 t_c = 2\pi/3$  and  $\phi = \phi_1 - \phi_2 = \pi/3$  ( $n = 0$ ) gives, respectively, the following components of  $K_e$ , where  $U_p = E_0^2/4\omega_0^2$ :

$$\begin{aligned} K_{ex} &= \frac{1}{2} \dot{x}^2(t_c) = \frac{9}{32} \left(\frac{E_0}{\omega_0}\right)^2 (\sqrt{3} \cos \phi_2 + 3 \sin \phi_2)^2, \\ K_{ey} &= \frac{1}{2} \dot{y}^2(t_c) = \frac{9}{32} \left(\frac{E_0}{\omega_0}\right)^2 (3 \cos \phi_2 - \sqrt{3} \sin \phi_2)^2, \\ K_e &= K_{ex} + K_{ey} = \frac{1}{2} [\dot{x}^2(t_c) + \dot{y}^2(t_c)] = 13.5U_p. \end{aligned} \quad (11)$$

The second choice for  $n = 1$ ,  $\omega_0 t_c = 4\pi/3$  and  $\phi = \phi_1 - \phi_2 = -\pi/3$ , corresponds to replace  $\phi_2$  by  $-\phi_2$  in Eq. (11). Equation (11) shows that the total  $K_e$  is independent of  $\phi_2$  for both optimal CEPs  $\phi = \pm\pi/3$ . In Figs. 1(a) and 1(b) we show  $K_e$  as a function of  $\phi_1$  and  $\phi_2$ . Maximum  $K_e = 13.5U_p$  occurs for  $\phi_1 = \pm\pi/3 + \phi_2$  as predicted by Eq. (11). However, the different velocities and displacements are functions of  $\phi_2$  [Figs. 1(c)–1(f)]. We show an unusual symmetry in Figs. 1(c) and 1(d) for  $\phi = +\pi/3$  and  $-\pi/3$ . The corresponding  $x$  and  $y$  components of  $K_e$  alternate in phase.

At intensity  $I_0 = 2 \times 10^{14}$  W/cm<sup>2</sup> ( $E_0 = 0.0755$  a.u.) and  $\lambda = 400$  nm ( $\omega_0 = 0.114$  a.u.), the electron displacements (transfer distances)  $x(t_c)$  and  $y(t_c)$  for  $\omega_0 t_c = 2\pi/3$  and  $\phi = \pi/3$  ( $n = 0$ ) and for  $\omega_0 t_c = 4\pi/3$  and  $\phi = -\pi/3$  ( $n = 1$ ) are shown in Figs. 1(e) and 1(f), respectively. With  $\omega_0 t_c = 2\pi/3$ , for example, for phases  $\phi_1 = \pi/3$  and  $\phi_2 = 0$ , the electron displacements are  $x(t_c) = -0.35$  a.u. and  $y(t_c) = -18.5$  a.u. and for  $\phi_1 = 0$  and  $\phi_2 = -\pi/3$ , the electron displacements are  $x(t_c) = -16.2$  a.u. and  $y(t_c) = -8.9$  a.u. from Eq. (10). Maximum efficiency of the MHOHG process is obtained for the smallest  $x(t_c)$  or  $y(t_c)$  which corresponds to near direct (head-on) collision with a neighboring nucleus. Thus at  $\lambda = 800$  nm ( $\omega_0 = 0.057$  a.u.), the corresponding electron displacements are, respectively,  $x(t_c) = -1.4$  a.u. and  $y(t_c) = -74$  a.u. and  $x(t_c) = -64.6$  a.u. and  $y(t_c) = -35.7$  a.u. We conclude hence that short wavelengths (e.g.,  $\lambda = 400$  nm) and

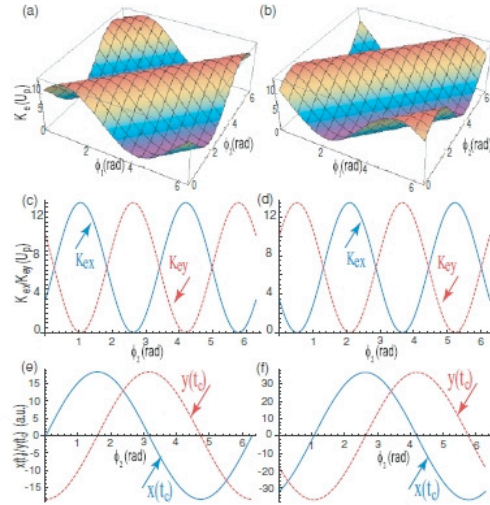


FIG. 1. (Color online) Total kinetic  $K_e$  as a function of phases  $\phi_1$  and  $\phi_2$  (radian) for the cases (a)  $n = 0$  and  $\omega_0 t_c = 2\pi/3$  and (b)  $n = 1$  and  $\omega_0 t_c = 4\pi/3$ . The CEPs  $\phi = \phi_1 - \phi_2 = \pi/3$  and  $\phi = -\pi/3$  give the maximum  $K_e = 13.5U_p$ , respectively. The corresponding kinetic energies  $K_{ex}$  and  $K_{ey}$ , Eq. (11) (c–d), and displacements  $x(t_c)$  and  $y(t_c)$ , Eq. (10) (e–f), for the maximum  $K_e$  with a bichromatic circularly polarized laser pulse at  $I_0 = 2 \times 10^{14}$  W/cm $^2$  ( $E_0 = 0.0755$  a.u.),  $\lambda_1 = 400$  nm ( $\omega_0 = 0.114$  a.u.), and  $\lambda_2 = 200$  nm ( $\omega_0 = 0.228$  a.u.) as a function of  $\phi_2$ .

phases  $\phi_1 = \pi/3$  and  $\phi_2 = 0$  give the best collision conditions with neighboring ions, thus increasing MHOHG efficiencies.

### III. COMPUTATIONAL METHODS

We consider the  $H_2^+$  molecular ion at a fixed internuclear separation  $R$  (Born-Oppenheimer approximation) interacting with a circularly polarized laser pulse  $E(t)$ . The corresponding 2D (plane) TDSEs

$$i \frac{\partial}{\partial t} \Psi(\mathbf{r}, t) = H(\mathbf{r}, t) \Psi(\mathbf{r}, t), \quad (12)$$

$$H(\mathbf{r}, t) = H_0(\mathbf{r}) + \mathbf{r} \cdot \mathbf{E}(t), \quad (13)$$

$$H_0(\mathbf{r}) = -\frac{1}{2} \nabla_{\mathbf{r}}^2 + V(\mathbf{r}), \quad (14)$$

where  $r = x$  and  $y$ ,  $V(\mathbf{r})$  is the two-center Coulomb potential, and the matter-field interaction is treated in the length gauge, are solved numerically by a three-point difference combined with higher-order split-operator methods [26,27]. A temporal slowly varying envelope  $\sin^2(\pi t/10\tau)$ , where one optical cycle (o.c.)  $\tau = 2\pi/\omega_0$ , is adopted. The MHOHG power spectrum  $P_r(\omega)$  is obtained from the absolute square of the Fourier transforms (FT) of the dipole acceleration  $\langle \ddot{r}(t) \rangle$ :

$$P_r(\omega) = \left| \int \exp(-i\omega t) \langle \ddot{r}(t) \rangle dt \right|^2 \quad (15)$$

with the laser-induced electron acceleration obtained from the exact time-dependent electron wave function  $\Psi(\mathbf{r}, t)$ ,

$$\langle \ddot{r}(t) \rangle = \langle \Psi(\mathbf{r}, t) | -\partial H(\mathbf{r})/\partial \mathbf{r} | \Psi(\mathbf{r}, t) \rangle. \quad (16)$$

For the ten-optical-cycles pulse used here, the HHG spectra calculated from the FT of dipole moment, velocity, and acceleration forms give nearly the same results [28].

To describe the polarization properties of the emitted MHOHG [29], the relevant physical quantities are introduced (see, for example, Fig. 1 in [22]). The complex integral in Eq. (15) has two  $x$  and  $y$  components, thus allowing us to extract the dependence of the phase difference  $\delta$  between the polarized component of the emitted harmonics on the angular frequency  $\omega$  [30]. The ellipticity  $\varepsilon$  and the orientation angle  $\varphi$ , the angle between the major axis of the ellipse and the  $y$  axis, are defined, respectively, as

$$\varepsilon = \tan \chi \quad (17)$$

and

$$\tan(2\varphi) = \tan(2\gamma) \cos \delta, \quad (18)$$

where

$$\sin(2\chi) = \sin(2\gamma) \sin \delta, \quad (19)$$

$$\tan \gamma = \sqrt{P_x/P_y}. \quad (20)$$

### IV. NUMERICAL RESULTS AND DISCUSSIONS

The numerical results in Fig. 2 based on solutions of the  $x$ -aligned  $H_2^+$  TDSE, Eqs. (12)–(14), with a single circularly polarized laser pulse confirm our conclusion in Eq. (5) where maximum harmonic energy  $I_p + 8U_p$  is induced. For wavelength  $\lambda = 400$  nm ( $\omega_0 = 0.114$  a.u.) and intensity  $I_0 = 2.1 \times 10^{14}$  W/cm $^2$  ( $E_0 = 0.077$  a.u.), Fig. 2 shows the corresponding MHOHG spectrum at the internuclear distance  $R = 22$  a.u. corresponding to  $R_n = 3.72E_0/\omega_0^2$ , Eq. (6) with  $n = 0$ . The maximum harmonic order  $N_m = (I_p + 8U_p)/\omega_0$

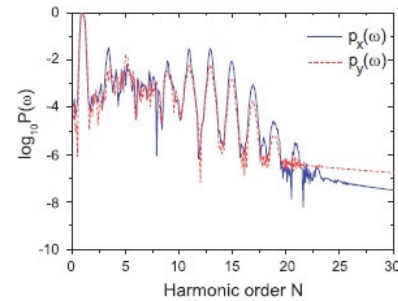


FIG. 2. (Color online) The  $x$  (solid blue line) and  $y$  (dashed red line) components of  $x$ -aligned  $H_2^+$  MHOHG at  $R = x(t_c) = 22$  a.u. for  $\lambda = 400$  nm,  $I_0 = 2.1 \times 10^{14}$  W/cm $^2$ , and  $\phi = \tan^{-1}(-\pi/2)$  circularly polarized light. The cutoff order  $N_m = (I_p + 8U_p)/\omega_0 \approx 13$ .



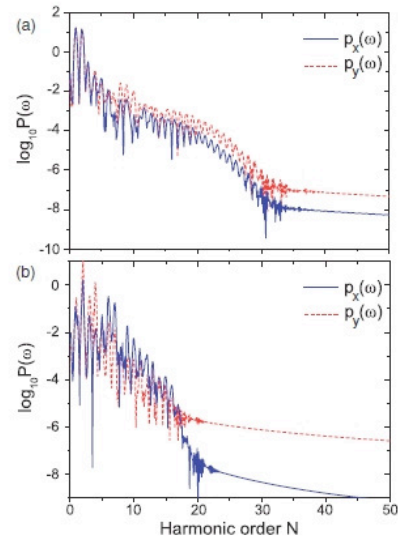


FIG. 3. (Color online) MHOHG spectra of  $y$ -aligned  $H_2^+$  with a bichromatic circularly polarized laser pulse at  $I_0 = 2 \times 10^{14}$  W/cm $^2$ ,  $\lambda_1 = 400$  nm,  $\lambda_2 = 200$  nm,  $\phi_1 = \pi/3$ , and  $\phi_2 = 0$  (a) at  $R = -y(t_c) = 19$  a.u. and (b) at  $R_e = 2$  a.u. The cutoff order  $N_m = (I_p + 13.5U_p)/\omega_0 \approx 18$  for  $n = 0$ ,  $\omega_0 t_c = 2\pi/3$ , and  $\phi = \phi_1 - \phi_2 = \pi/3$ .

occurs around  $N_m = 13$  in both  $x$  and  $y$  directions, with a decrease in intensity for orders larger than  $N_m$ . We reemphasize that for equilibrium  $H_2^+$  ( $R_e = 2$  a.u.) *no* harmonics are appreciably produced and observed numerically and *none* for the H atom since the ionized electron never collides with the parent ion.

Figure 3(a) illustrates the MHOHG spectrum obtained for  $H_2^+$  aligned with the  $y$ -axis such that  $y(t_c) = -R = -19$  a.u. and  $x(t_c) = -0.35$  a.u. at  $I_0 = 2 \times 10^{14}$  W/cm $^2$  ( $E_0 = 0.0755$  a.u.),  $\lambda_1 = 400$  nm ( $\omega_0 = 0.114$  a.u.),  $\lambda_2 = 200$  nm ( $2\omega_0 = 0.228$  a.u.), and  $\phi_1 = \pi/3$  and  $\phi_2 = 0$  ( $\phi = \pi/3$ ). A plateau is obtained between harmonic orders 10 and 20 with a cutoff (decrease) around the harmonic energy  $I_p + 13.5U_p$ . Figure 4(a) shows, with the same pulses but phases  $\phi_1 = 0$  and  $\phi_2 = \pi/3$  ( $\phi = -\pi/3$ ), a similar MHOHG spectrum obtained but  $y(t_c) = -R = -37$  a.u. and  $x(t_c) = -0.35$  a.u. at collision. In Fig. 5(a), at the same intensity but longer wavelengths  $\lambda_1 = 800$  nm ( $\omega_0 = 0.057$  a.u.) and  $\lambda_2 = 400$  nm ( $2\omega_0 = 0.114$  a.u.) and phases  $\phi_1 = \pi/3$  and  $\phi_2 = 0$  ( $\phi = \pi/3$ ), the same maximum harmonic order is obtained:  $N_m = (I_p + 13.5U_p)/\omega_0$  but now  $y(t_c) = -R = -74$  a.u. and  $x(t_c) = -1.4$  a.u. at collision with the neighbor. In Figs. 3(b), 4(b), and 5(b) we show the MHOHG spectrum at the equilibrium distance  $R_e = 2$  a.u. We see the absence of a long plateau with high efficiencies since now collision with neighboring nuclei *does not* occur, but rather the  $H_2^+$  molecule at  $R_e = 2$  a.u. appears like a one-center atom to the ionized electron at larger  $x$  and  $y$ . We reemphasize that at

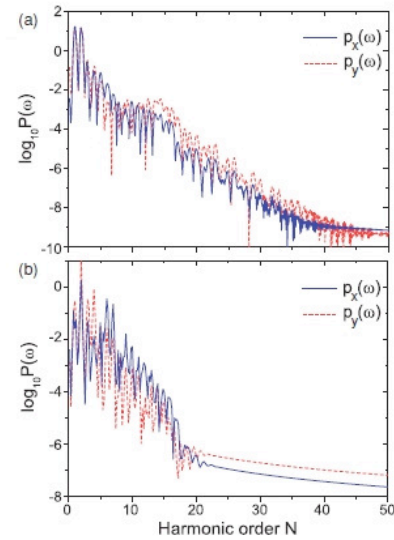


FIG. 4. (Color online) MHOHG spectra of  $y$ -aligned  $H_2^+$  with a bichromatic circularly polarized laser pulse at  $I_0 = 2 \times 10^{14}$  W/cm $^2$ ,  $\lambda_1 = 400$  nm,  $\lambda_2 = 200$  nm,  $\phi_1 = 0$ , and  $\phi_2 = \pi/3$  (a) at  $R = -y(t_c) = 37$  a.u. and (b) at  $R_e = 2$  a.u. The cutoff order  $N_m = (I_p + 13.5U_p)/\omega_0 \approx 18$  for  $n = 1$ ,  $\omega_0 t_c = 4\pi/3$ , and  $\phi = \phi_1 - \phi_2 = -\pi/3$ .

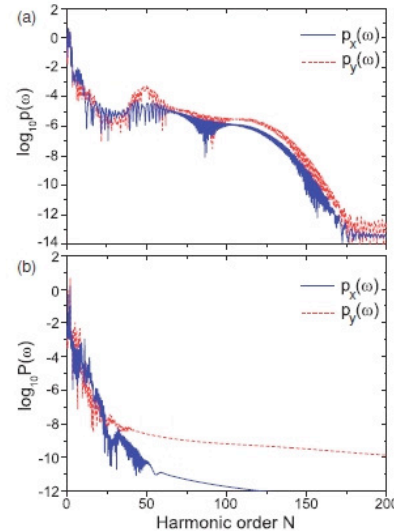
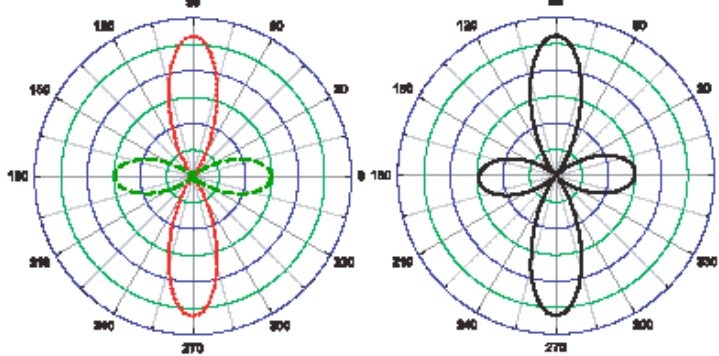
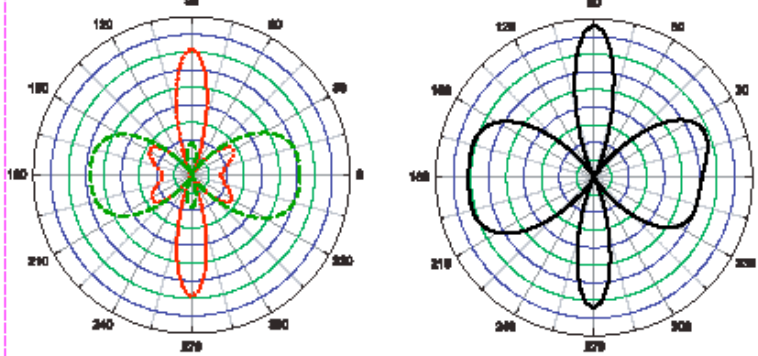


FIG. 5. (Color online) MHOHG spectra of  $y$ -aligned  $H_2^+$  with a bichromatic circularly polarized laser pulse at  $I_0 = 2 \times 10^{14}$  W/cm $^2$ ,  $\lambda_1 = 800$  nm,  $\lambda_2 = 400$  nm,  $\phi_1 = \pi/3$ , and  $\phi_2 = 0$  (a) at  $R = -y(t_c) = 74$  a.u. and (b) at  $R_e = 2$  a.u. The cutoff order  $N_m = (I_p + 13.5U_p)/\omega_0 \approx 120$  for  $n = 0$ ,  $\omega_0 t_c = 2\pi/3$ , and  $\phi = \phi_1 - \phi_2 = \pi/3$ .

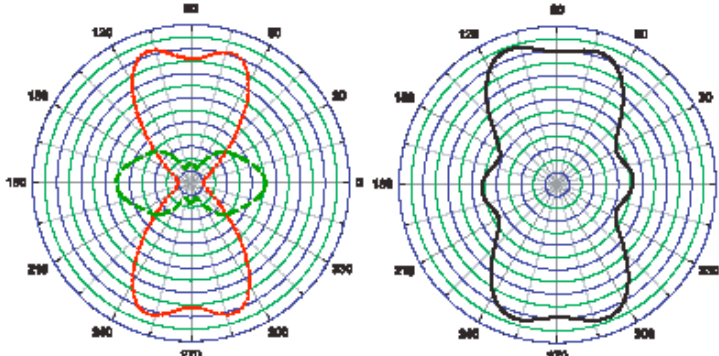
(a)  $X^1\Sigma_g^+$  ( $\lambda_e=2.75$  a.u.)  $\lambda=10$  nm,  $Re=1.675$  a.u.



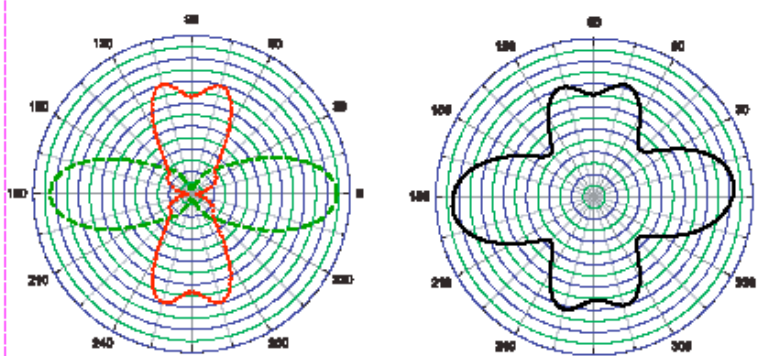
(b)  $X^1\Sigma_g^+$  ( $\lambda_e=1.65$  a.u.)  $\lambda=5$  nm,  $Re=1.675$  a.u.



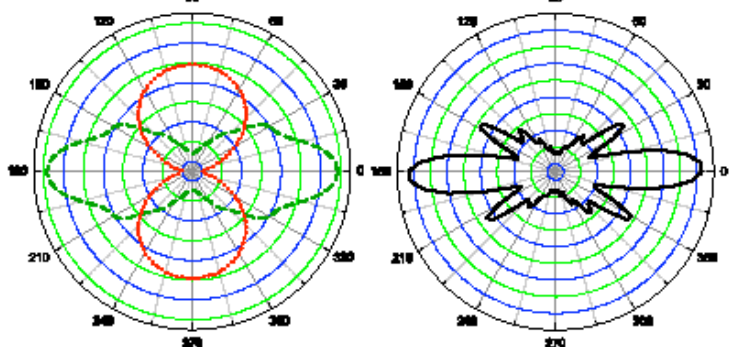
$A^3\Sigma_u^+$  ( $\lambda_e=2.58$  a.u.)



$A^3\Sigma_u^+$  ( $\lambda_e=1.62$  a.u.)

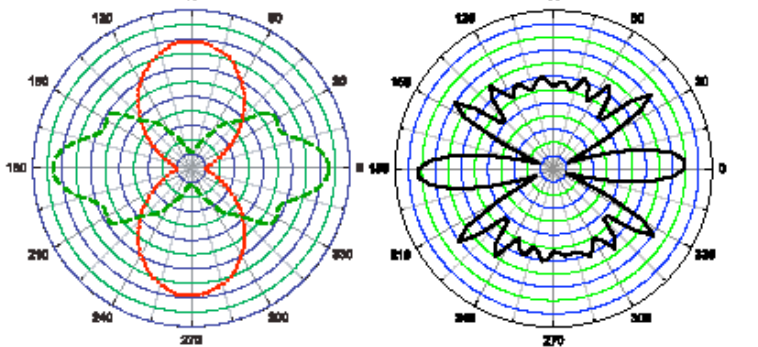


(c)  $X^1\Sigma_g^+$  ( $\lambda_e=2.44$  a.u.)



$\lambda=10$  nm,  $R=10$  a.u.

$A^3\Sigma_u^+$  ( $\lambda_e=2.44$  a.u.)





116%

Find

## HIGHLIGHTS

DOI: 10.1002/cphc.200800770

# The Molecular Cat

Maddalena Pedio<sup>[b]</sup> and Majed Chergui\*<sup>[a]</sup>

One of the often-claimed advantages of core-shell spectroscopic techniques is that they can probe valence orbitals—which are responsible for bond formation and are therefore delocalized over the entire molecular edifice—from atomic-like levels. The initial state of the transition is a (core) orbital that is local-

ions. So, would symmetry be conserved in this case?

To answer this question, the authors used a subtle approach.<sup>[1]</sup> Core levels decay in many cases by emission of an Auger electron, while an electron from a higher orbital fills the initially created core hole. The lifetime of the latter is

tion coincidence spectroscopy (APECS) they used, and other coincidence techniques (such as double photoemission<sup>[8]</sup>) to “condensed matter” systems (i.e. clusters, surfaces, and solids). In this context, the localization or delocalization of the core hole becomes an issue.

Most core-level spectroscopic studies

# Attosecond photoionization of a coherent superposition of bound and dissociative molecular states: effect of nuclear motion

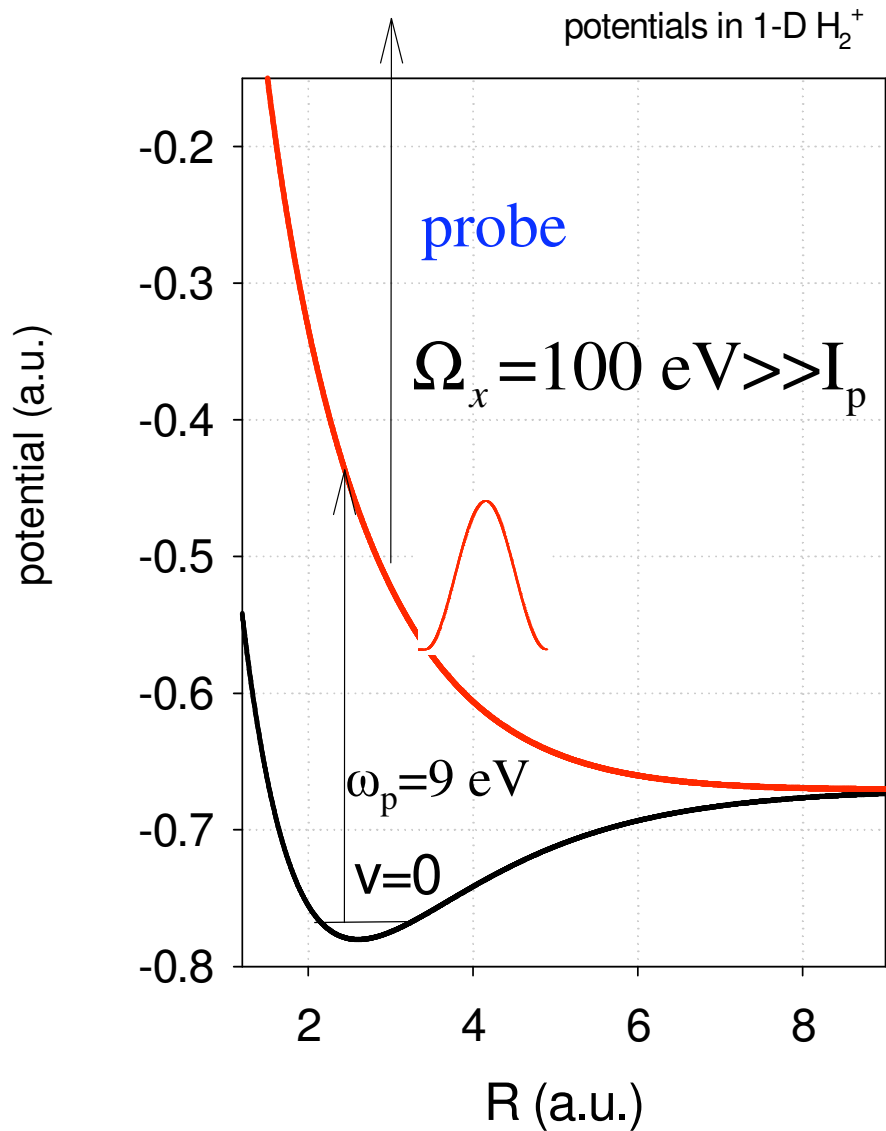
by

**André D. Bandrauk,**

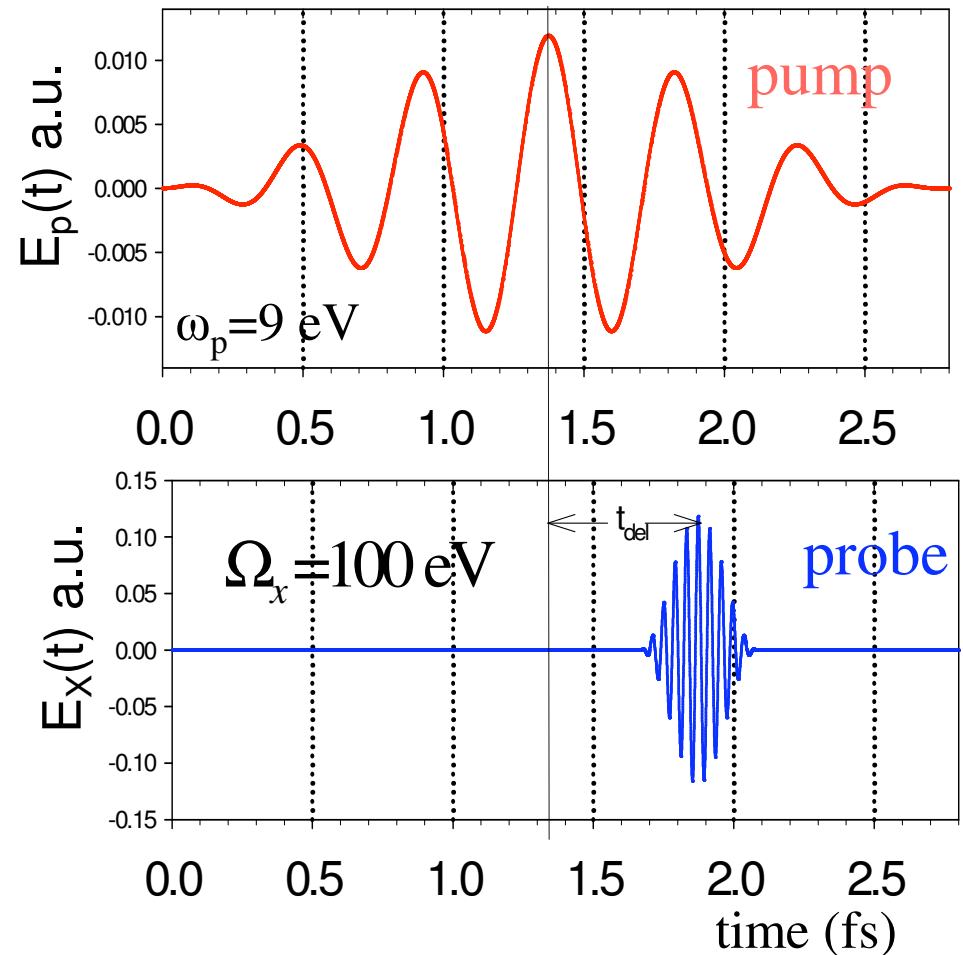
**with S.Chelkowski, G.L. Yudin,**  
Université de Sherbrooke, Canada

**P.B. Corkum (Ottawa),  
J. Manz (Berlin)**

J Phys B 42,134001 (2009)

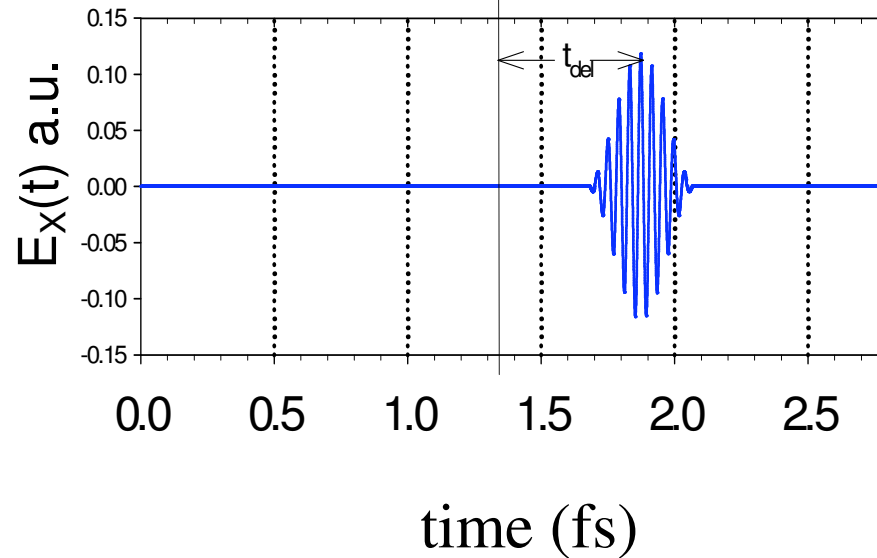
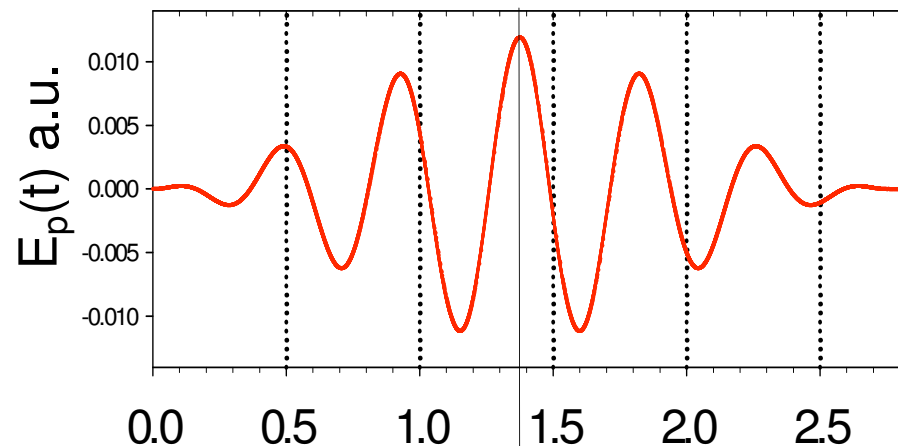
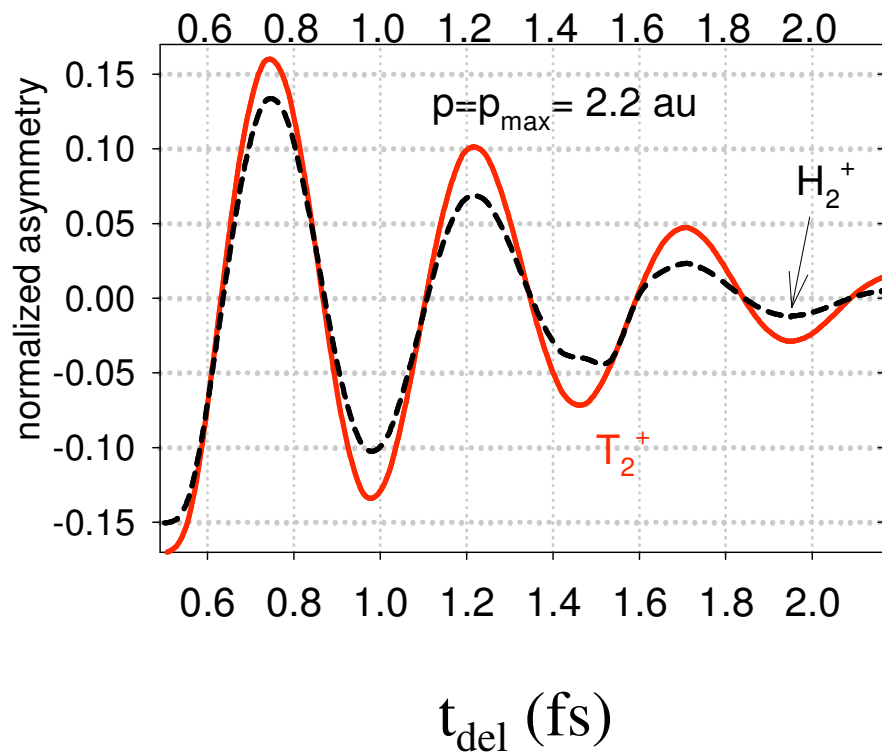
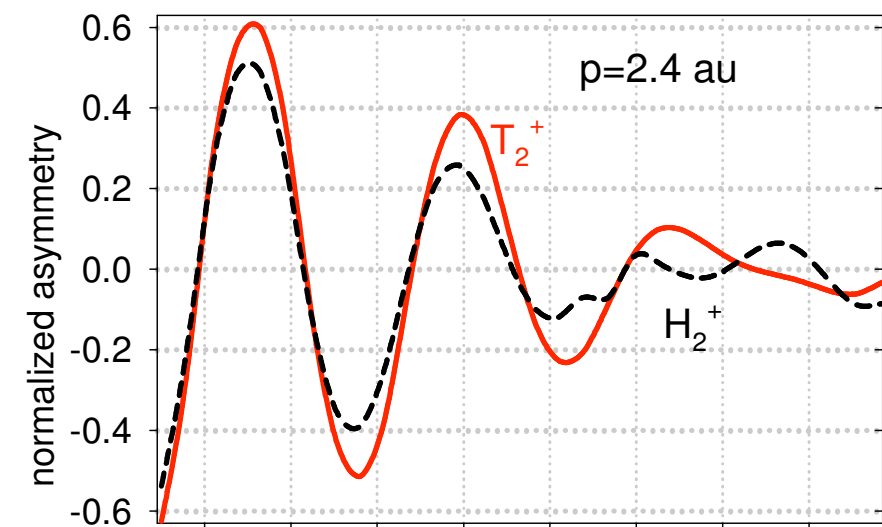


Electric field of a pump pulse  $E_p$   
and of an attosecond probe  $E_x$



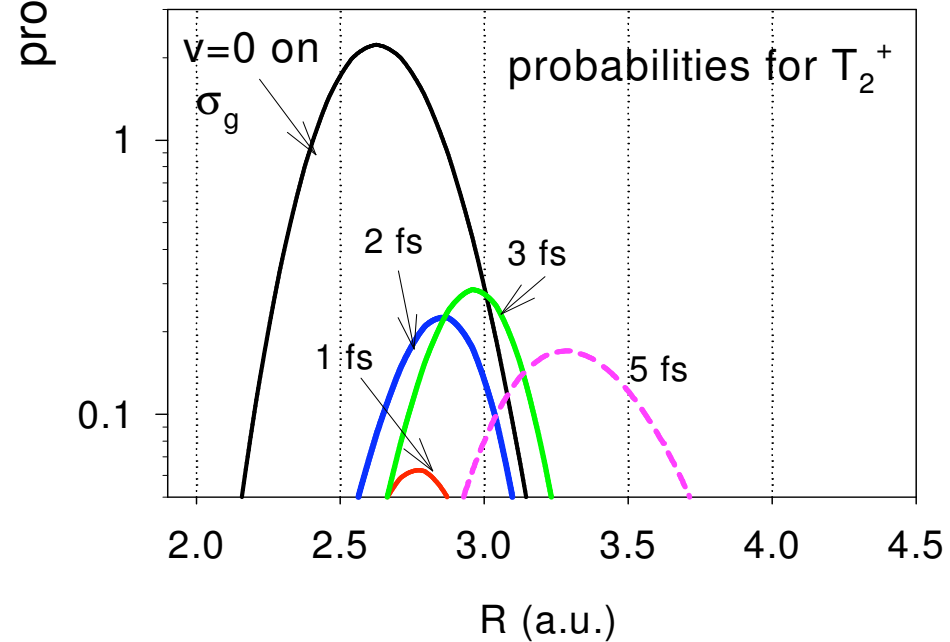
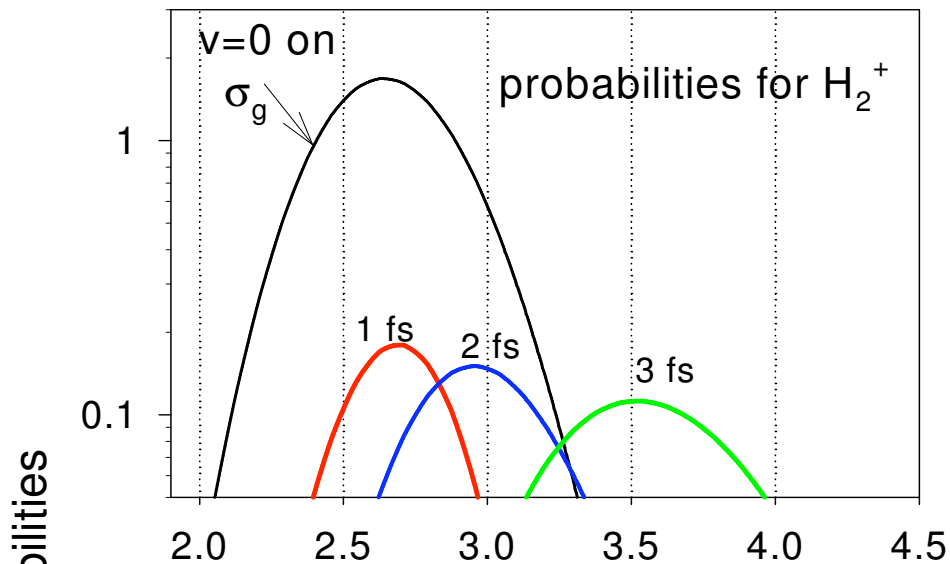
We solved the TDSE for a series of delays:  $t_{\text{del}} = 0.5 \text{ fs} + k T_1 / 8$ ,  
 $k=0,1,\dots$   $T_1 = 2\pi/\omega_p$ . We calculated the forward and backward)  
 photoelectron spectra  $S(p)$   $T_1/8 = 0.46 \text{ fs}$

Moving  $H_2^+$  and  $T_2^+$

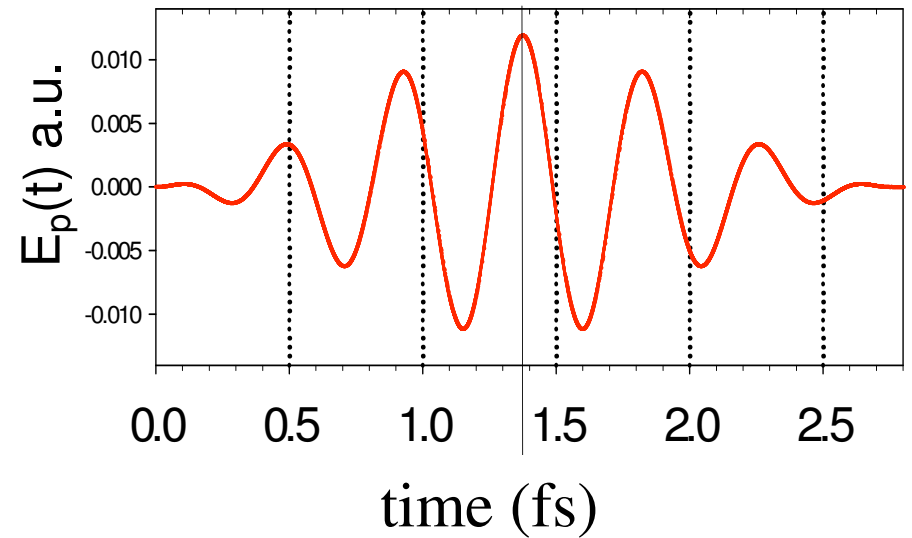


$$\text{asymmetry} = \frac{S_{\text{forw.}}(p) - S_{\text{backw.}}(p)}{S_{\text{forw.}}(p) + S_{\text{backw.}}(p)}$$





Wave packet motion induced by the pump shown below:



We show the initial  $v=0$  vibrational state and the dissociating packets on  $\sigma_u$ .

Conclusion: at  $t > 3$  fs ( $t_{del} > 1.5$  fs) we lose the overlap in  $H_2^+$ . This agrees with the attenuation seen in the previous slide

Decoherence?: see Zurek, PRD 47,488(1993)

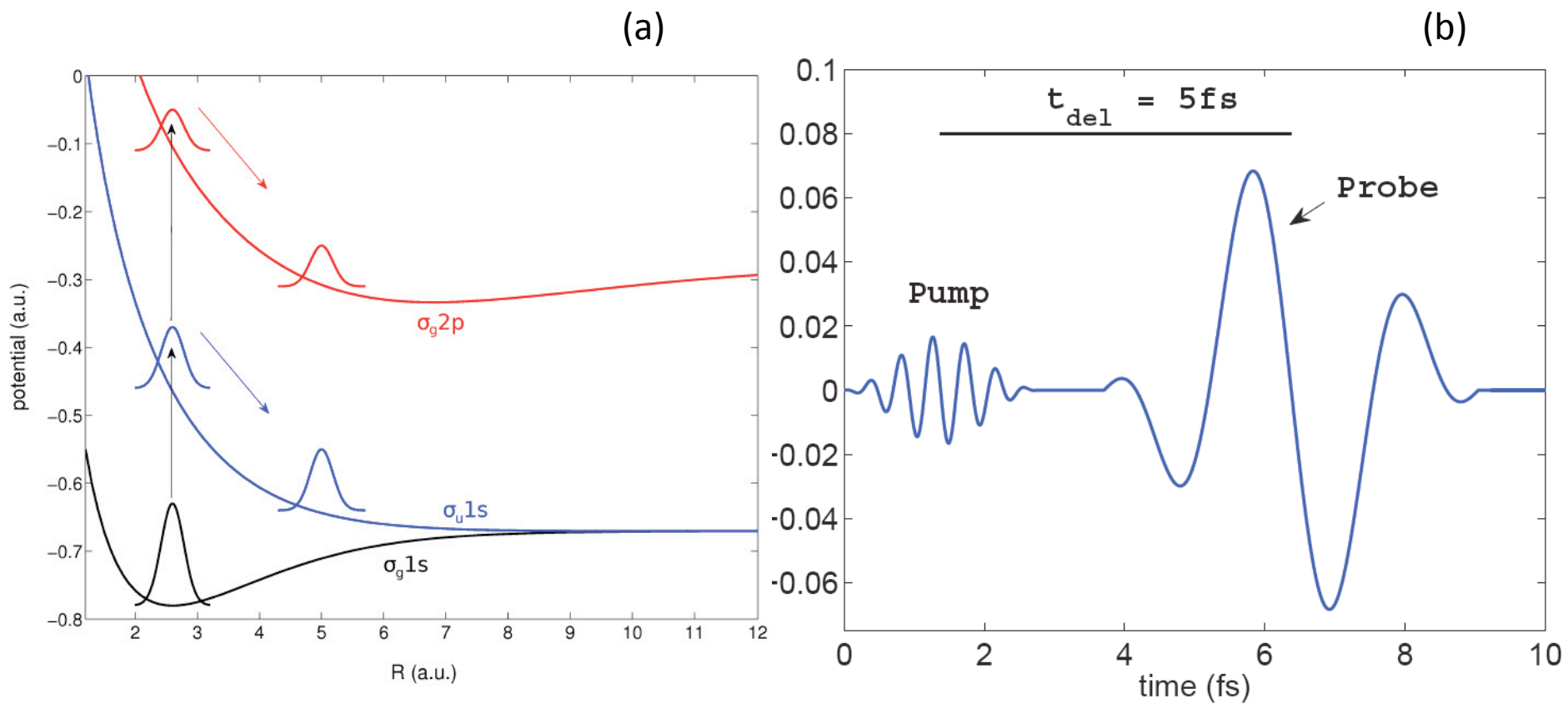


Fig.1. Illustration of the pump-probe scheme.

T Bredtmann,(FU Berlin),S Chelkowski,ADB

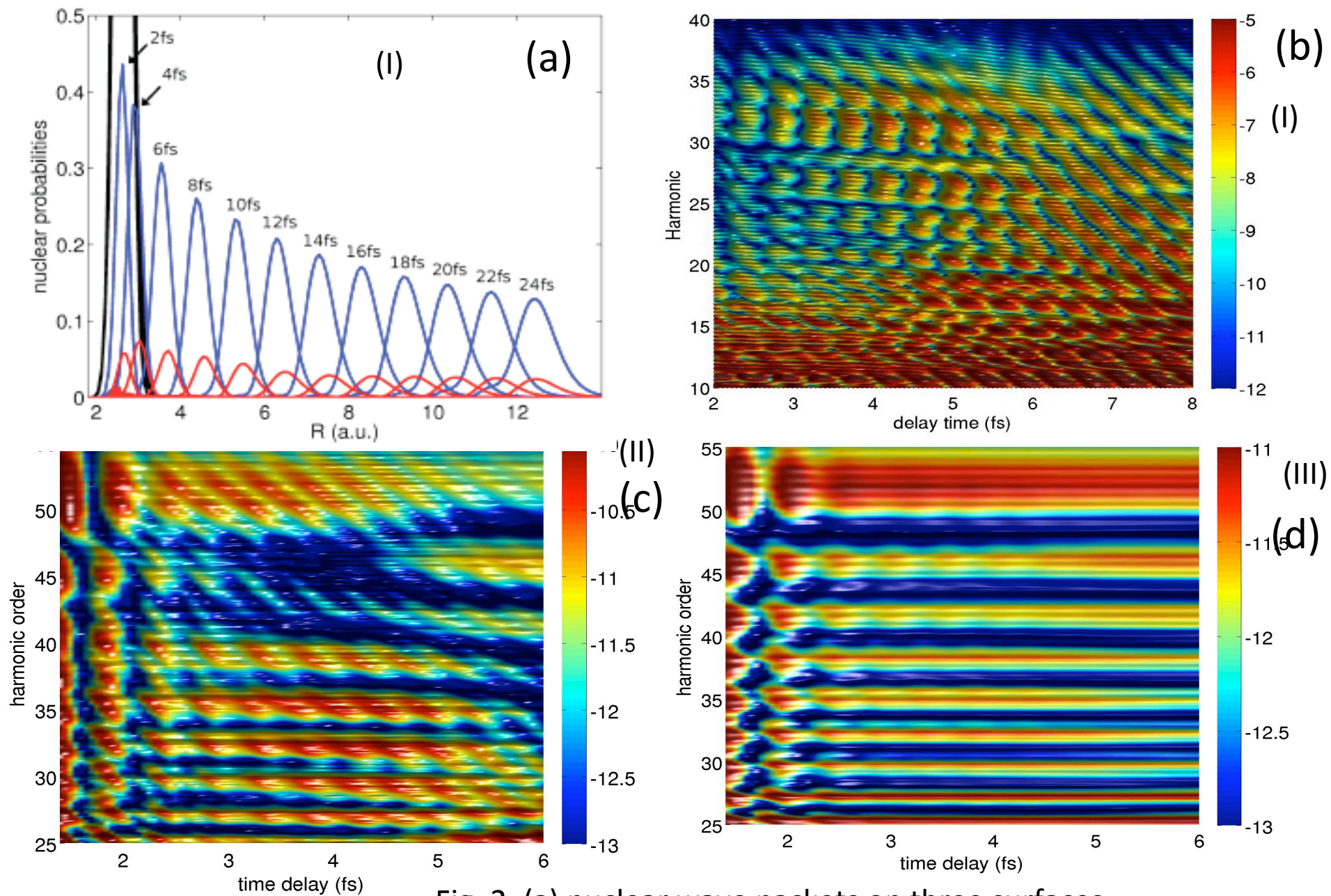
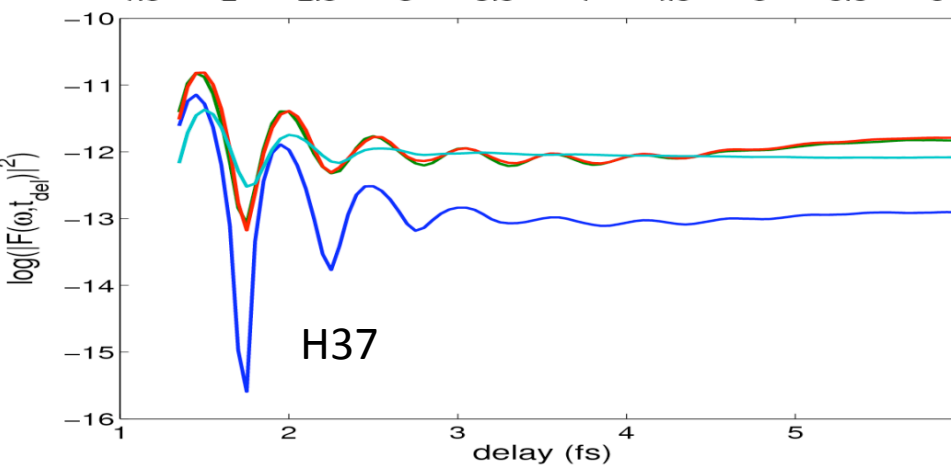
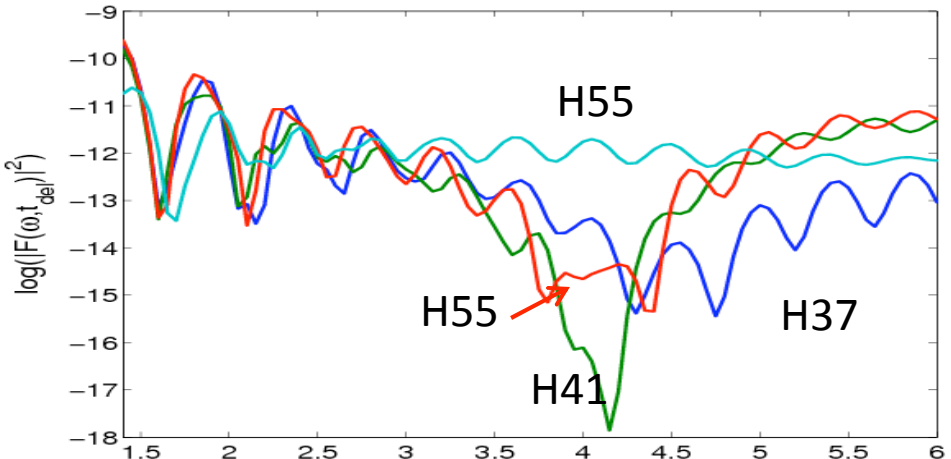
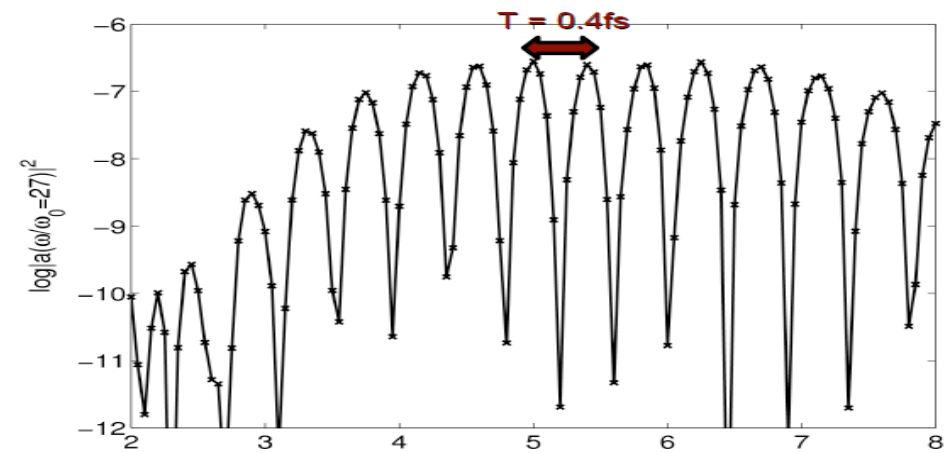


Fig. 2. (a) nuclear wave packets on three surfaces. (b)-(c) Harmonic spectra as function of the delay time  $t_{\text{del}}$



(I)

(II)

(III)

Fig.3. Intensity of selected harmonics as function of time delay  $t_{del}$  .



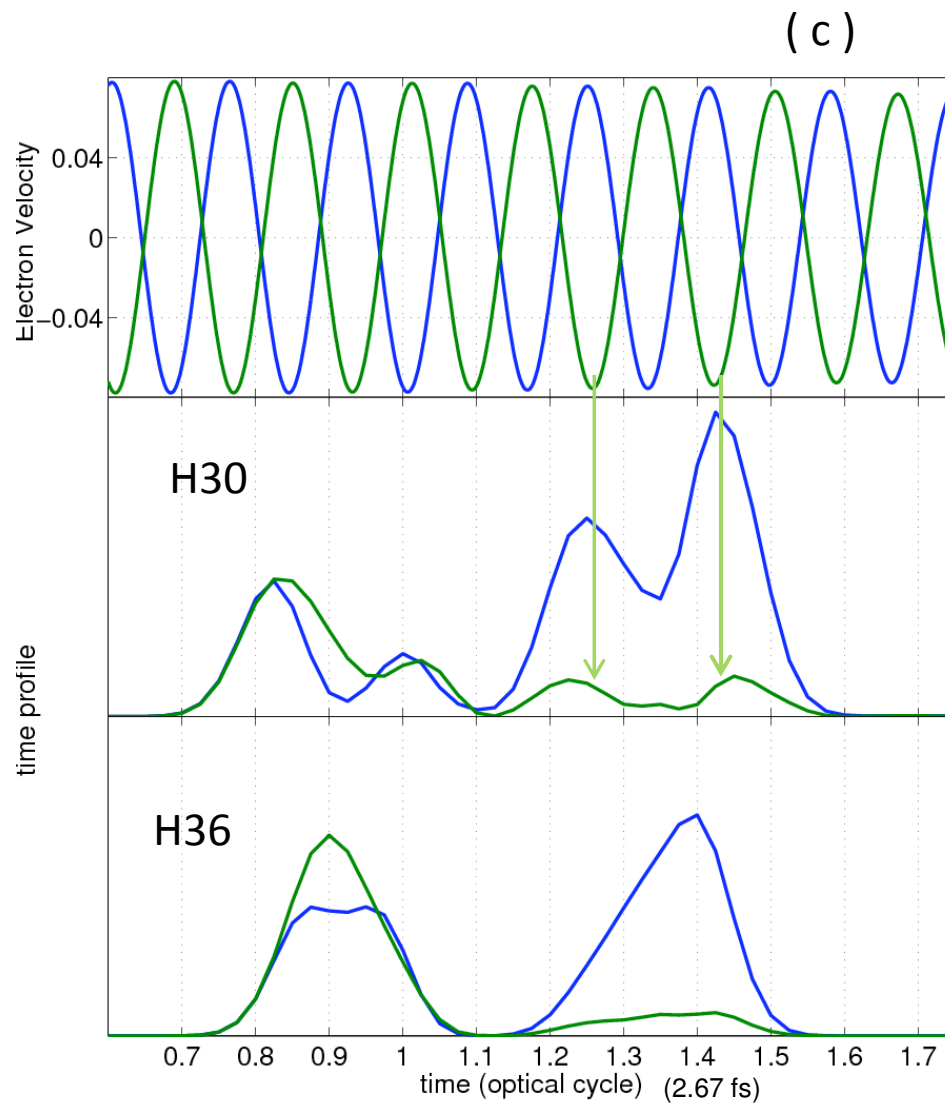
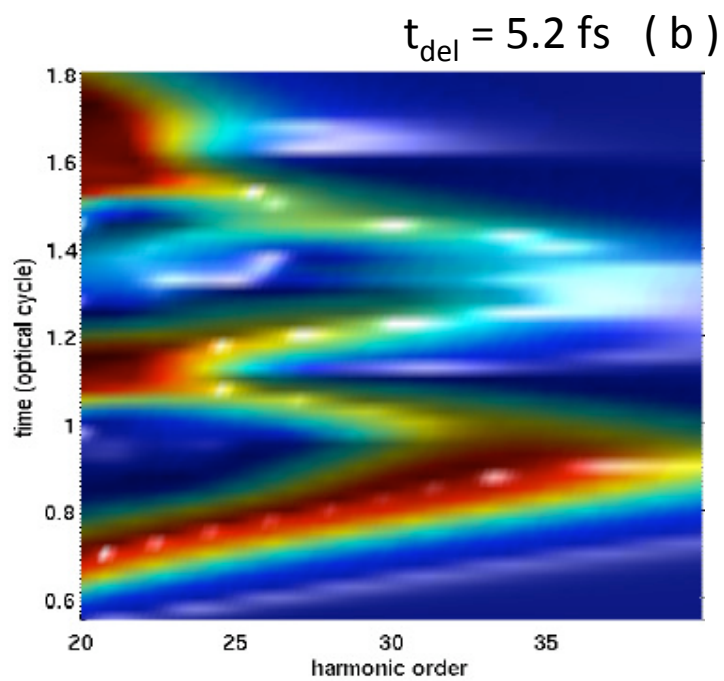
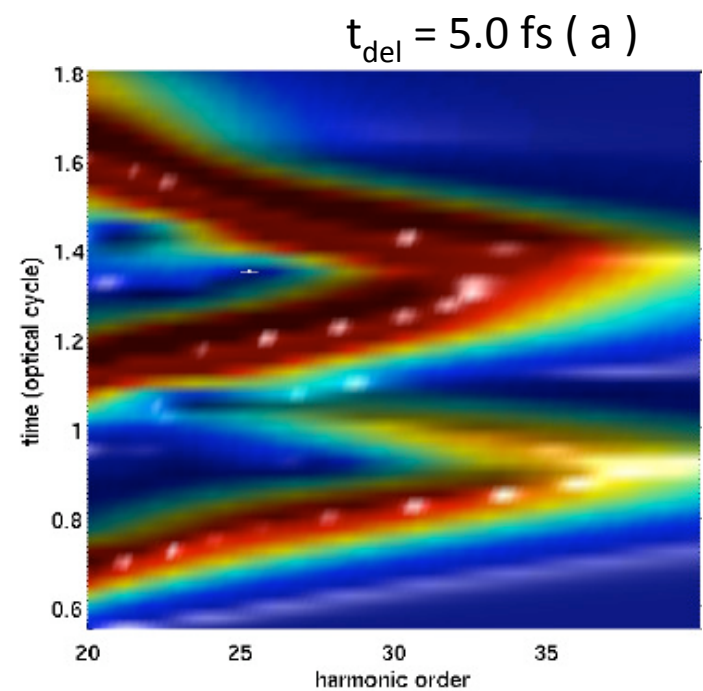


Fig.4 Time-profiles for the scheme (I) , blue -  $t_{\text{del}}=5.0$ , green-  $t_{\text{del}}=5.2\text{fs}$

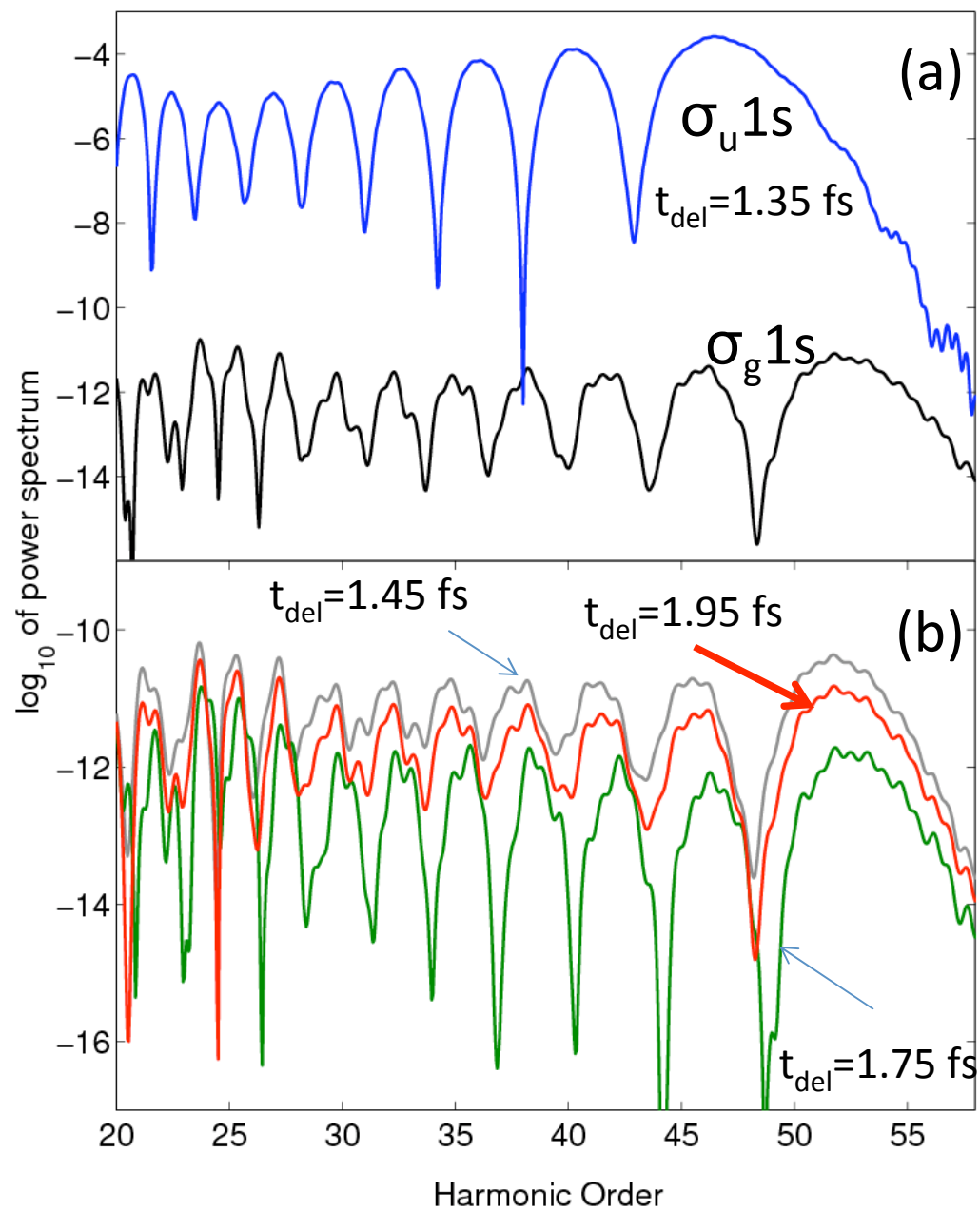


Fig.5 Harmonic spectra for  $I_{probe} = 4 \times 10^{14} \text{ W/cm}^2$  generated from :  
 (a)  $\sigma_g 1s$  (red) and  $\sigma_u 1s$  (blue), and from  
 : (b) coherent  
 superposition at delays 1.45, 1.75 and 1.95 fs (scheme III) .



# Nuclear fusion from explosions of femtosecond laser-heated deuterium clusters

T. Ditmire, J. Zweiback, V. P. Yanovsky, T. E. Cowan, G. Hays & K. B. Wharton

Laser Program, L-477, Lawrence Livermore National Laboratory, Livermore, California 94550, USA

As a form of matter intermediate between molecules and bulk solids, atomic clusters have been much studied<sup>1</sup>. Light-induced processes in clusters can lead to photo-fragmentation<sup>2,3</sup> and Coulombic fission<sup>4</sup>, producing atom and ion fragments with a few electronvolts (eV) of energy. However, recent studies of the photoionization of atomic

cluster) are ionized, electrons undergo rapid collisional heating for the short time ( $< 1$  ps) before the cluster disassembles in the laser field<sup>19</sup>. Through various collective and nonlinear processes, the laser rapidly heats the electrons to a non-equilibrium state (with mean

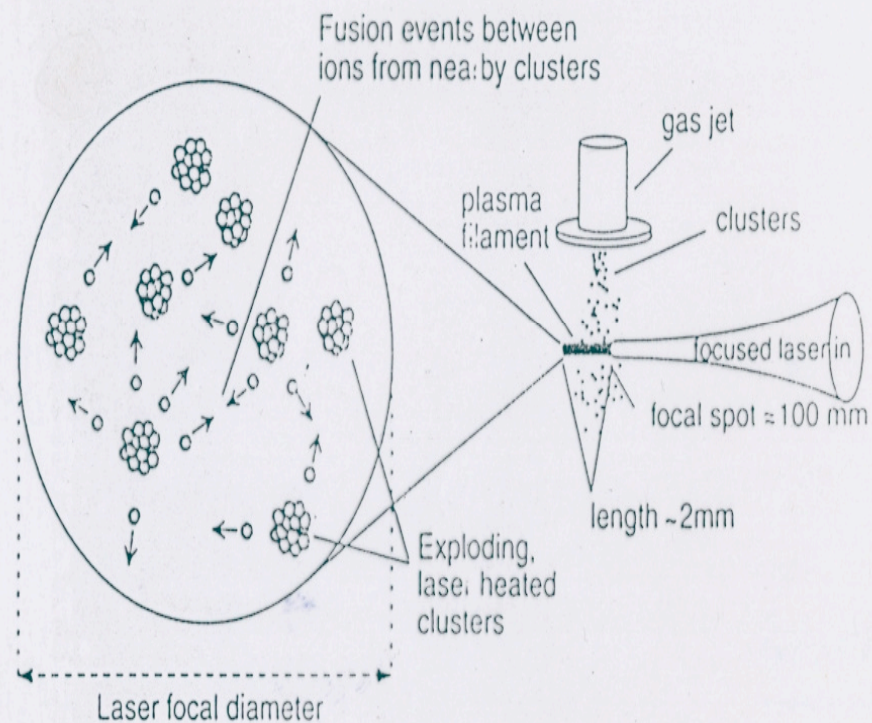
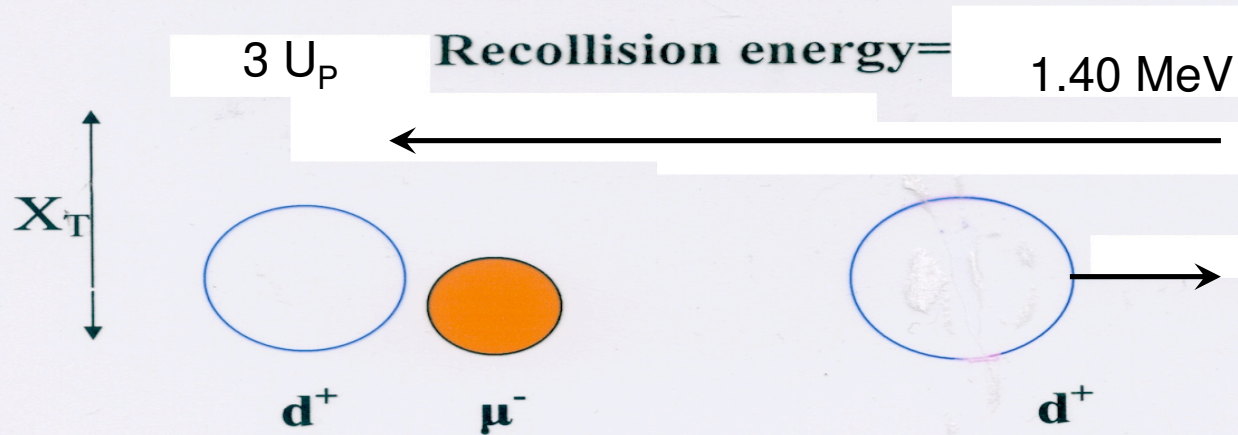


Figure 1 Layout of the deuterium cluster fusion experiment.



RECOLLISION OF  $d^+$  WITH A  $\mu d$  ATOM INITIATED BY A SUPER-INTENSE LASER



$X_T = 0.9 \text{ \AA}$

ELECTRIC FIELD  $E(t)$  OF THE LASER

$\lambda = 800 \text{ nm}$

THUS THE LASER CAN INITIATE

A NUCLEAR REACTION ,e.g:

$I - 3 \times 10^{22} \text{ W/cm}^2$



or



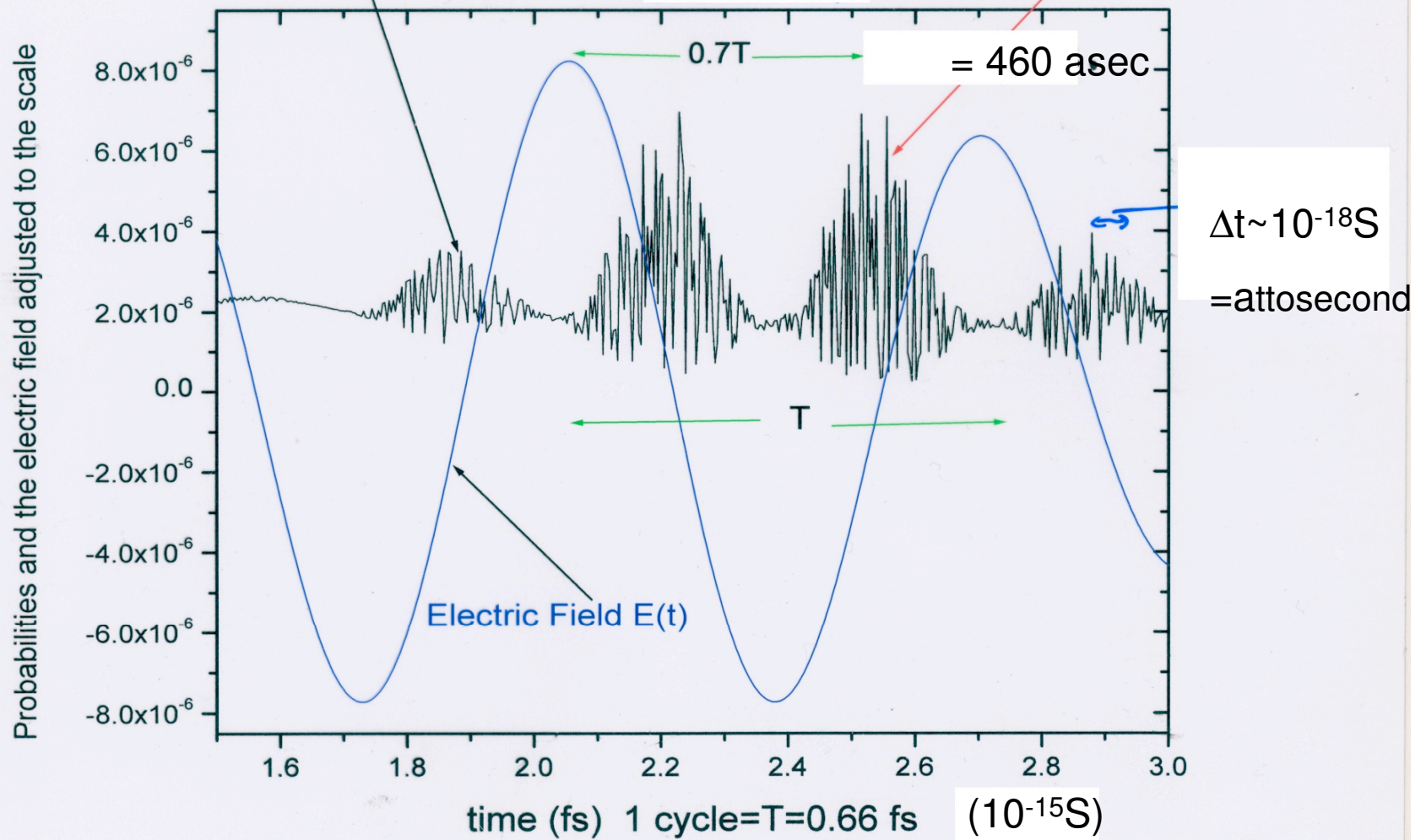


d- $\mu$ -d molecule dissociating in  
200 nm,  $I=10^{22}$  W/cm<sup>2</sup> laser field

deuterium returns back !

probability for  $R < 0.25 \mu$  un. ( $1 \mu$  un. = 0.0026 Angstrom)  
 $26 \times 10^{-14}$  m)

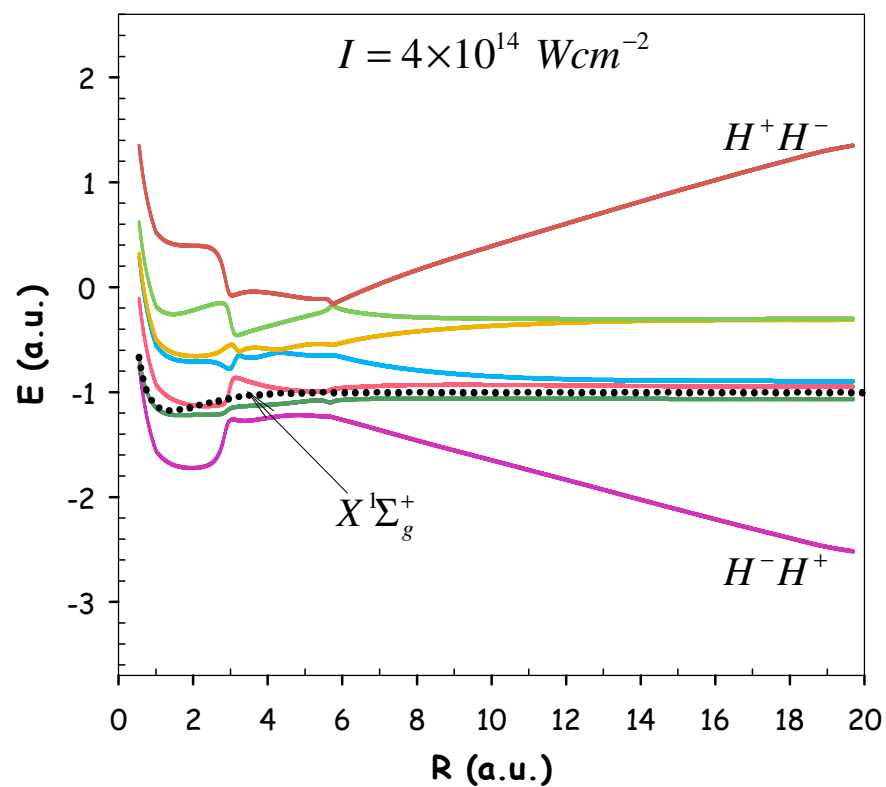
$E \sim 1/2$  MeV



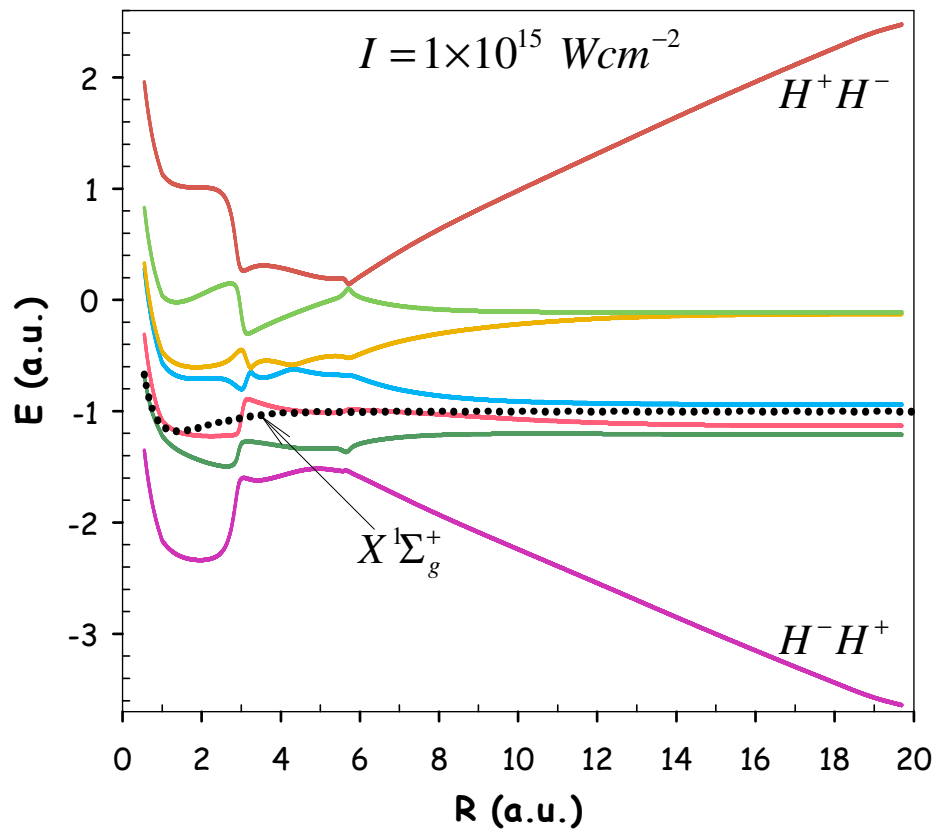
PRL 93,083602(2004) ; ADB,G Paramonov,AIP Conf Proc,1209,7(2010)

# Dressed Potential Energies for H<sub>2</sub> molecule in static laser field

$e=0.106299$  a.u.



$e=0.168073$  a.u.





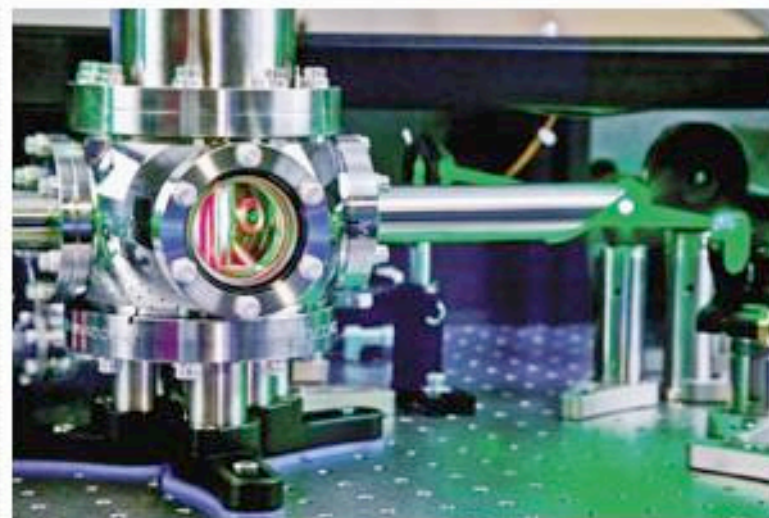
## Tracking Electrons

**Attosecond science opens the door to real-time observation and control of electron dynamics**

Jyllian Kemsley

TEN YEARS AGO, Ahmed H. Zewail won the Nobel Prize for using femtosecond spectroscopy to study atomic motions during chemical reactions. Emerging now from Zewail's pioneering work is the ability to use femtosecond laser pulses to monitor attosecond-scale electron dynamics, which was the focus of a Division of Physical Chemistry symposium on attosecond science at the American Chemical Society national meeting in Salt Lake City last month.

"There's a whole class of processes associated with electron dynamics that occur at a femtosecond timescale or less," Daniel M. Neumark, a chemistry professor at the University of California, Berkeley, said at the meeting. "These are electron dynamics processes that don't require nuclear motion. To probe them you need attosecond-scale pulses."



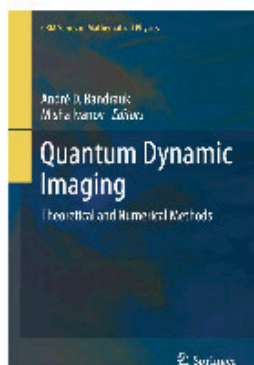
Gary Larson © 2004

**ULTRAFAS**T A cryostat contains a cooled Ti:sapphire laser amplifier crystal that is used to generate high-power femtosecond pulses for attosecond experiments.

# Mathematical Problems


1. High order SOM
2. Multiscale time frequency analysis
3. Infinite D Optimal Control theory  
(Bartels, Murnane, Rabitz, PRA 70,043404(2004) ; ADB et al, PRA 69,041802(2004))
4. High order NLSE
5. Relativistic QM
6. Molecular movies  
(Dynamic Imaging of Electrons-Nuclei)





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## Quantum Dynamic Imaging

### Theoretical and Numerical Methods

#### Editors:

**André D. Bandrauk**, Université de Sherbrooke, QC, Canada

**Misha Ivanov**, Imperial College London, UK

Studying and using light or "photons" to image and then to control and transmit molecular information is among the most challenging and significant research fields to emerge in recent years. One of the fastest growing areas involves research in the temporal imaging of quantum phenomena, ranging from molecular dynamics in the femto ( $10^{-15}$ s) time regime for atomic motion to the atto ( $10^{-18}$ s) time scale of electron motion. In fact, the attosecond "revolution" is now recognized as one of the most important recent breakthroughs and innovations in the science of the 21st century. A major participant in the development of ultrafast femto and attosecond temporal imaging of molecular quantum phenomena has been theory and numerical simulation of the nonlinear, non-perturbative response of atoms and molecules to ultrashort laser pulses. Therefore, imaging quantum dynamics is a new frontier of science requiring advanced mathematical approaches for analyzing and solving spatial and temporal multidimensional partial differential equations such as Time-Dependent Schrodinger Equations (TDSE) and Time-Dependent Dirac equations (TDDEs for relativistic phenomena). These equations are also coupled to the photons in Maxwell's equations for collective propagation effects. Inversion of the experimental imaging data of quantum dynamics presents new mathematical challenges in the imaging of quantum wave coherences on subatomic (subnanometer) spatial dimensions and multiple timescales from atto to femto and even nanoseconds.

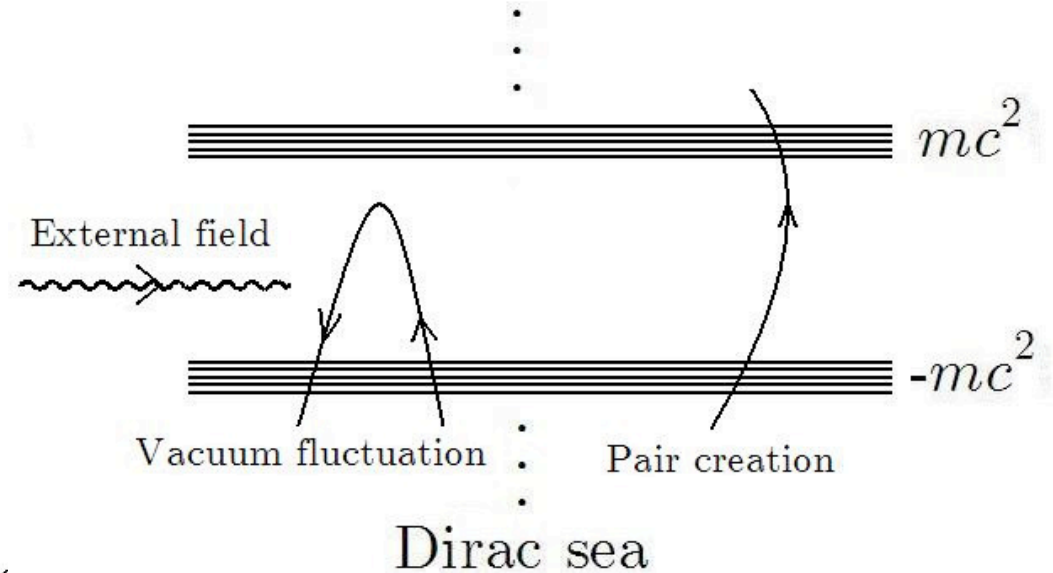
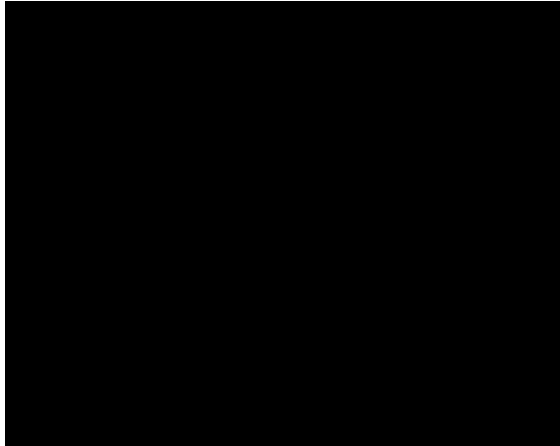
In *Quantum Dynamic Imaging: Theoretical and Numerical Methods*, leading researchers discuss these exciting state-of-the-art developments and their implications for R&D in view of the promise of quantum dynamic imaging science as the essential tool for controlling matter at the molecular level.

#### Key Features:

- Presents the latest research results in ultrafast imaging of quantum phenomena
- Demonstrates the wide-ranging potential of quantum dynamic imaging for R&D in areas as diverse as optoelectronics, materials science, and quantum information
- Edited and written by international leaders in the field

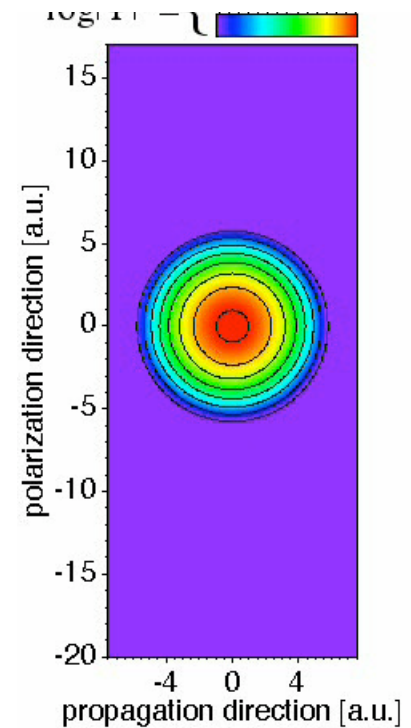
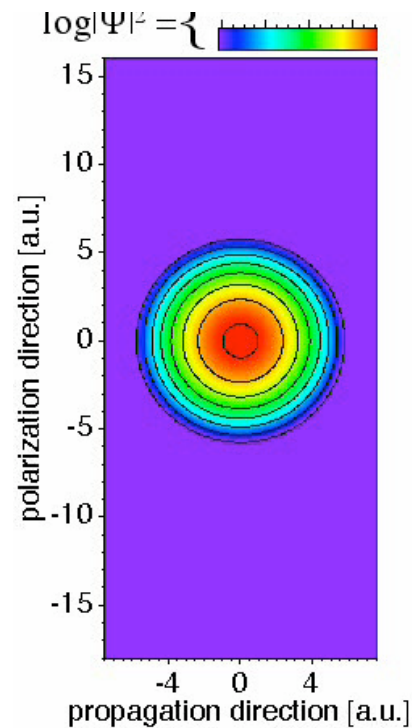
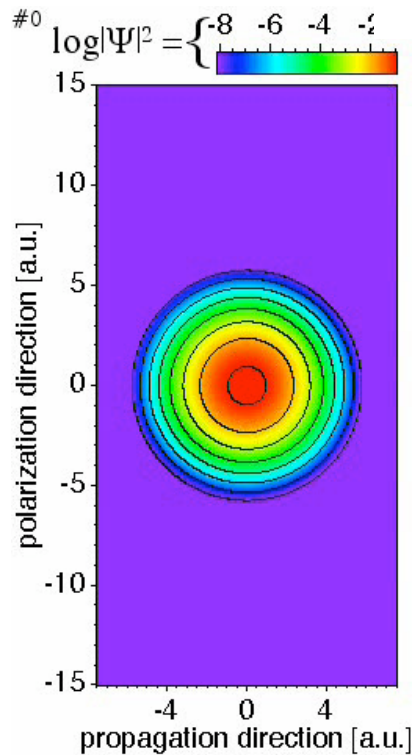
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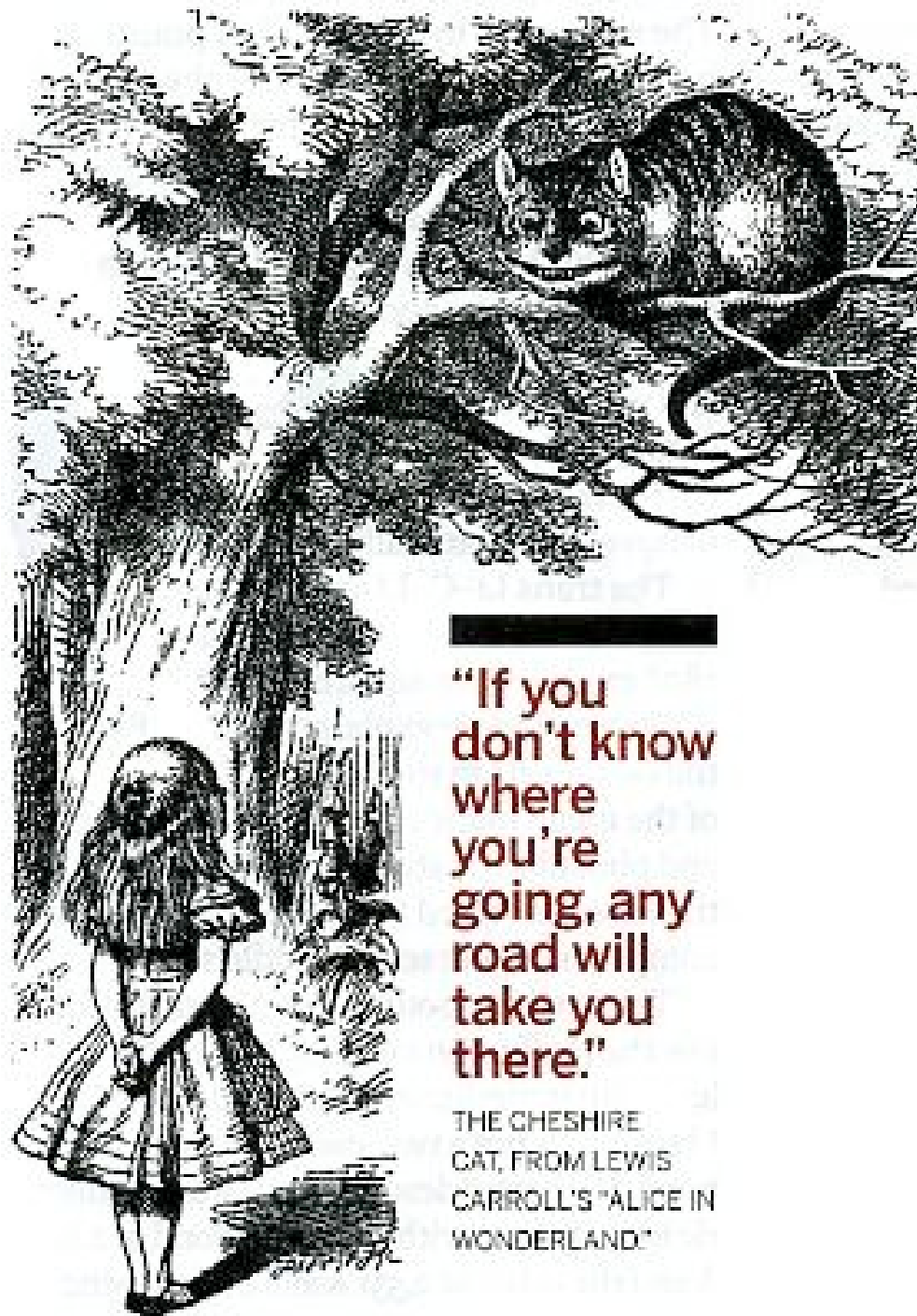
# High-Energy QED: Real and Virtual Pairs



Courtesy of  
CH Keitel(MPI,hdb)

Dirac dynamics of  
an electron with  
negative energy in  
crossed laser beams:  
pairs from  $10^{26}$  W/cm<sup>2</sup>





**“If you  
don't know  
where  
you're  
going, any  
road will  
take you  
there.”**

THE CHESHIRE  
CAT, FROM LEWIS  
CARROLL'S "ALICE IN  
WONDERLAND."



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**Published Online:** 19 Oct 2004

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## Article

### Theoretical approach to reactions of polyatomic molecules

L. Zülicke, A. Merkel

Akademie der Wissenschaften der DDR, Zentralinstitut für physikalische Chemie, DDR-1199 Berlin, German Democratic Republic

#### ABSTRACT

A scheme for systematic reduction of the theoretical treatment of elementary reactions involving polyatomic molecules is described; it consists of (1) limitation to the energetically relevant regions of the nuclear configuration space (the reaction path and its near environs) and (2) restriction to the dynamically relevant subspace of the nuclear configuration space (the active modes). Starting from a generalized reaction path Hamiltonian of Nauts and Chapuisat allowing for the use of arbitrary curvilinear coordinates and several large-amplitude modes, the realization of the above-sketched scheme is discussed. A compilation of recent work along these lines, mostly based on the simplified Miller-Handy-Adams reaction path Hamiltonian, is given with particular emphasis on applications of a statistical adiabatic model.

Received: 14 February 1989; Accepted: 4 July 1989

**DIGITAL OBJECT IDENTIFIER (DOI)**

10.1002/qua.560380214 [About DOI](#)





## Association francophone pour le savoir – Acfas

### 209 - Science Laser Ultrarapide-Femto-Atto-Zeptoseconde-FAZS

#### Responsables

Andre BANDRAUK, Université de Sherbrooke  
François LÉGARÉ, INRS

#### Informations sur le colloque

Catégorie : Colloque

#### Description du colloque :

La science laser moderne a subi une révolution par la génération d'impulsion ultracourte (quelques cycles optiques) et intense ( $>10^{15}$  W/cm<sup>2</sup>). Ceci permet l'étude de l'interaction laser-matière dans un nouveau régime hautement nonlinéaire et non-perturbatif. Le Québec est très actif et dominant dans ce domaine grâce à des laboratoires comme ALLS (Advanced Laser Light Source) situé à l'INRS-EMT, le Centre d'Optique, Photonique et Laser (COPL) de l'Université Laval, et l'équipe Atto-Québec financé par le FQRNT, etc. Un réseau de calcul de haute performance, RQHP, membre de Calcul Canada permet d'exécuter des simulations de haut niveau pour guider les expérimentateurs. Ce colloque propose donc de rassembler les acteurs principaux du Québec en plus quelques sommités internationales (françaises) pour adresser les questions importantes d'applications futures à de nouvelles technologies importantes pour la société de l'avenir.

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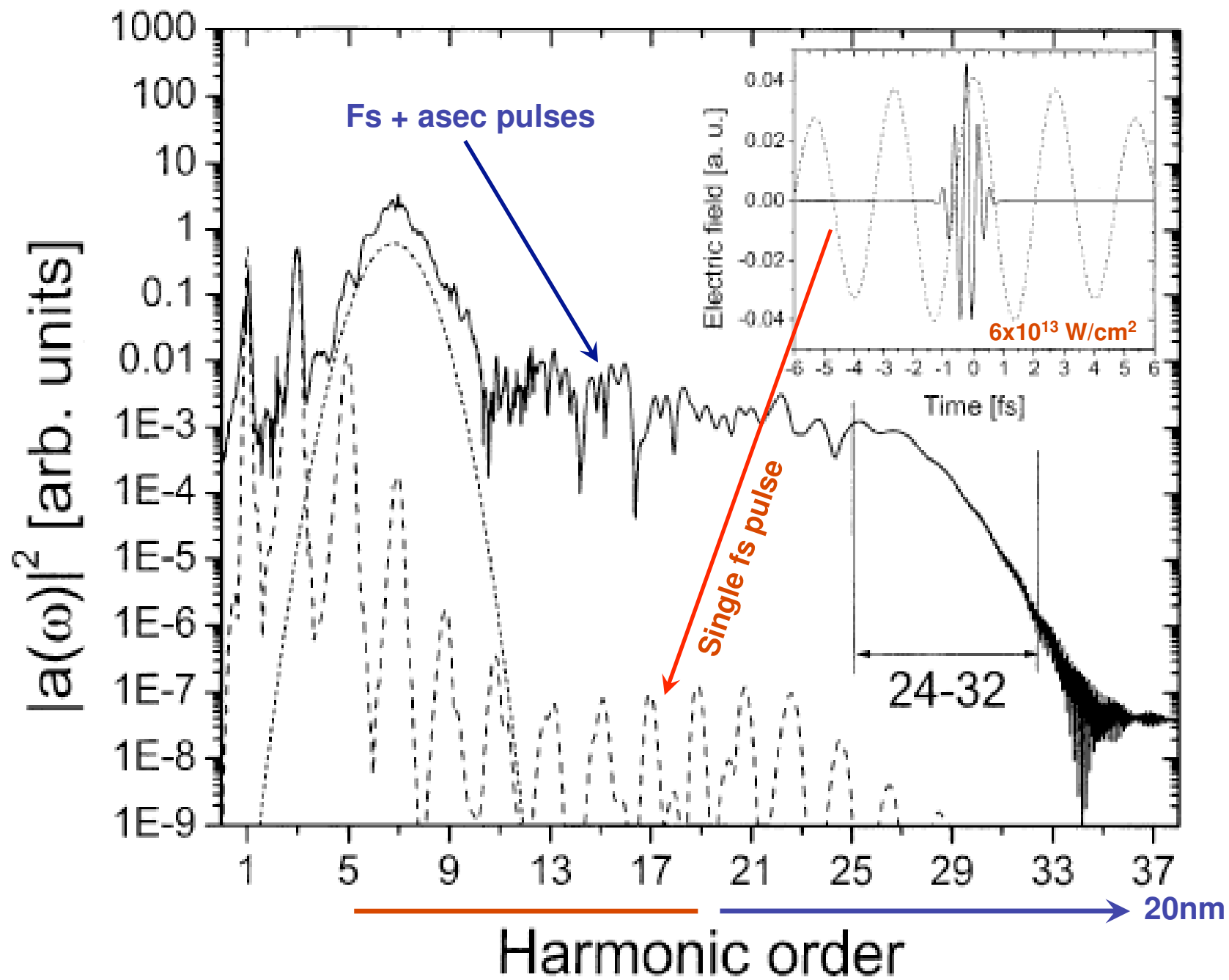
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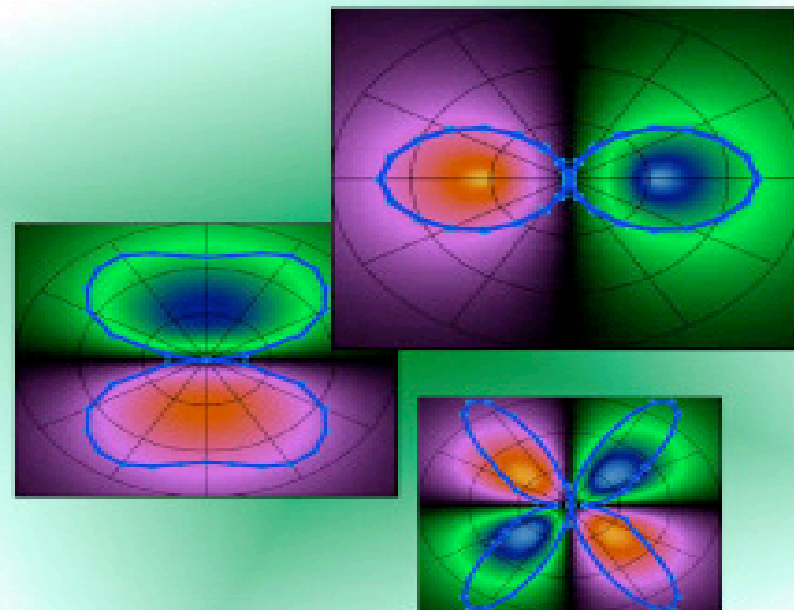
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