

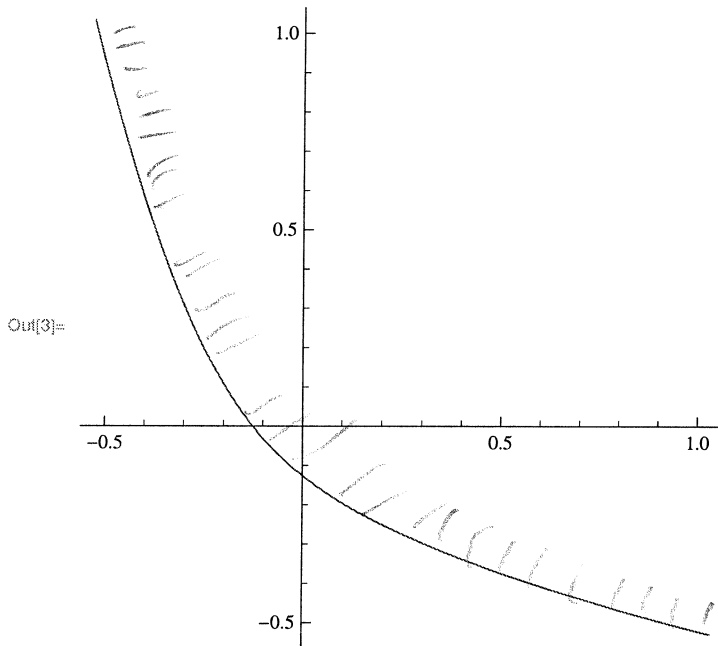
```
In[1]:= Expand[(x^2 - r^2 y^2)^2 (x^2 + y^2 / r^4)]
```

$$\text{Out[1]} = x^6 + \frac{x^4 y^2}{r^4} - 2 r^2 x^4 y^2 - \frac{2 x^2 y^4}{r^2} + r^4 x^2 y^4 + y^6$$

```
In[2]:= Coefficient[%, {x^4 y^2, x^2 y^4}]
```

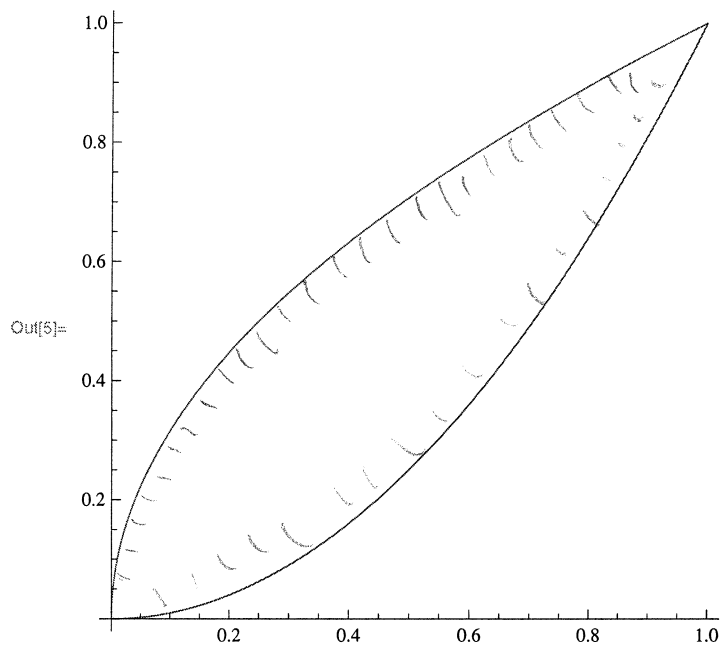
$$\text{Out[2]} = \left\{ \frac{1}{r^4} - 2 r^2, -\frac{2}{r^2} + r^4 \right\}$$

```
In[3]:= ParametricPlot[%2 / 15, {r, .5, 2}]
```



The boundary of the section of $P_{\{2,6\}}$

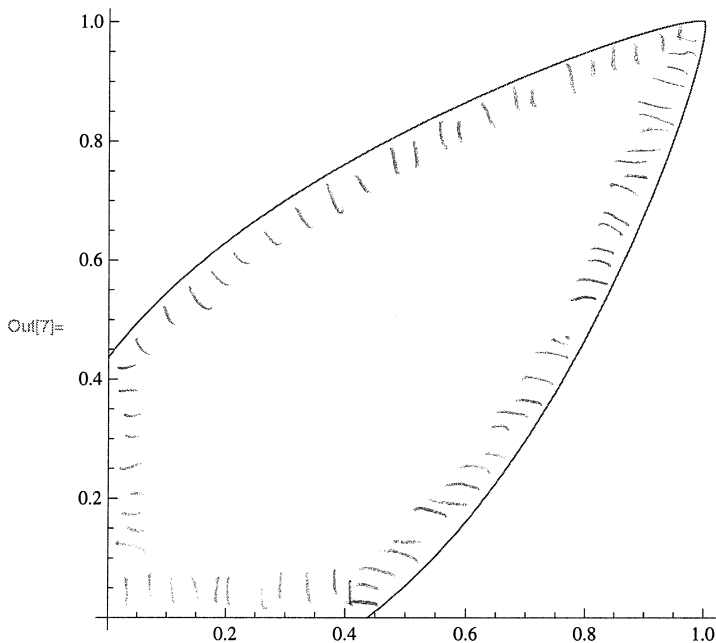
```
In[5]:= Plot[{x^2, Sqrt[x]}, {x, 0, 1}, AspectRatio -> 1]
```



The two parabolas on the boundary of the section of $Q_{\{2,6\}}$

```
In[6]:= Phi[r_] :=
  (1 - r)^(2/3) (1 + r)^(1/3) (1 + 2 r) / ((1 + 5 r + 10 r^2)^(2/3) (1 - 5 r + 10 r^2)^(1/3))
```

```
In[7]:= ParametricPlot[{Phi[r], Phi[-r]}, {r, -1/2, 1/2}]
```



The funny section of $K_{\{2,6\}}$; there are line segments along the axes from the origin to $(a, 0)$ and $(0, a)$ with $a^3 = 1/18$. The point $(1, 1)$ has a tangent, but infinite curvature.